© Indian Academy of Sciences

PRAMANA — journal of physics Vol. 69, No. 4 October 2007 pp. 661–668

# Electron transport through SWNT/trans-PA/ SWNT structure (the role of solitons): A t-matrix technique

S A KETABI<sup>1</sup>, H MILANI MOGHADDAM<sup>2,3</sup> and N SHAHTAHMASEBI<sup>2</sup>

<sup>1</sup>School of Physics, Damghan University of Basic Sciences, Damghan, Iran
<sup>2</sup>Department of Physics and Center for Nanotechnology Researches, Ferdowsi University of Mashhad, Mashhad, Iran
<sup>3</sup>Department of Physics, University of Mazandaran, Babolsar, Iran

E-mail: saketabi@dubs.ac.ir; saketabi@yahoo.com

MS received 9 July 2006; revised 4 February 2007; accepted 12 July 2007

**Abstract.** Using a tight-binding model and a transfer-matrix technique, we numerically investigate the effects of the coupling strength and the role of solitons on the electronic transmission through a system in which *trans*-polyacetylene (*trans*-PA) molecule is sandwiched between two semi-infinite single-walled carbon nanotubes (SWNT). We rely on Landauer formalism as the basis for studying the conductance properties of this system. Our calculations show that the solitons play an important role in the response of this system causing a large enhancement in the conductance. Also our results suggest that the conductance is sensitive to the CNT/molecule coupling strength.

Keywords. Trans-polyacetylene; t-matrix; carbon nanotube; electronic transmission; soliton.

PACS Nos 73.23.-b; 72.10.-d; 85.65.+h

# 1. Introduction

Substantial progress has been made on the rapidly developing field of molecular scale electronics [1–4]. The study of electron transport in nanoscale molecular devices has become the center of attraction of the theoretical and experimental researches in recent years [5–8]. This is due to the wide applications of these systems in the nano and molecular electronics and also fundamental importance of the electronic structure in the low-dimensional structures [9,10]. The typical systems considered are usually organic or polymer molecular device is mainly affected by (i) the quantum nature of molecular states in these systems, (ii) electronic properties of the electrodes near the Fermi energy level, (iii) the strength of the molecule/electrode coupling and (iv) the geometrical structure of the molecule and



Figure 1. A schematic representation of the CNT/*trans*-PA/CNT structure as described in the text.

electrodes. Doping of conjugated polymers give rise to geometrical defects in their structure. In trans-PA these defects are 'solitons' and may effectively affect the electronic conduction through the polymer [11]. As a model, we numerically investigate the conductance properties of trans-PA molecule in the CNT/trans-PA/CNT structure, where the nanocontact is considered as the armchair (l, l) single-walled carbon nanotubes (SWNT). In general, there are M atomic positions over the interfacial end-atoms of the tubes. For an armchair (l, l) SWNT topology imposed, the number of carbon sites at the interface is M = 2l. In our model (figure 1) the number of hybridization contacts between a tube and the molecule is set 1 (single contact case). Also it is shown that SWNT may be used as quasi-one-dimensional electrodes to construct CNT/(single)molecule/CNT structure with molecular scale width and channel length, such as single electron molecular transistors [12–14]. Our results suggest that the solitons in trans-PA play an important role in enhancing the conductance of the CNT/trans-PA/CNT structure. The procedures we have used in this work are based on two powerful numerical methods particularly suitable to treat the electron transmission through the large systems, the Landauer formalism and transfer-matrix (t-matrix) technique, where the solution of the Schrödinger equation is obtained by means of a product of  $2 \times 2$  matrices. The outline of the paper is as follows: In §2 the methodology to calculate the t-matrices and the transmission coefficient are described. The results and discussion are presented in  $\S3$  followed by a summary in  $\S4$ .

#### 2. Methodology

We use the following generalized Hamiltonian for the description of the CNT/molecule/CNT structure:

$$H = H_{\rm CNT} + H_{\rm SSH} + H_{\rm C},\tag{1}$$

where  $H_{\text{CNT}}$ ,  $H_{\text{SSH}}$  and  $H_{\text{C}}$  describe the semi-infinite CNT nanocontacts, the wellknown SSH Hamiltonian [11] for the *trans*-PA molecule and the couplings of the contacts to the molecule, respectively. The SWNT is modeled within the tightbinding Hamiltonian with only one  $\pi$ -orbital per atom [15,16]. This Hamiltonian can describe reasonably well the band structure of a nanotube especially near the Fermi level which is zero in this case since the on-site energy is assumed to be zero and each orbital is half-filled,

Pramana – J. Phys., Vol. 69, No. 4, October 2007

Electron transport through SWNT/trans-PA/SWNT structure

$$H_{\rm CNT} = \sum_{j} \varepsilon_j c_j^+ c_j - \sum_{j} t_{j+1,j} (c_{j+1}^+ c_j + c_j^+ c_{j+1}), \qquad (2)$$

where  $c_j(c_j^+)$  is the annihilation(creation) operator of an electron at the *j*th site. For the semi-infinite CNT contacts we set  $\varepsilon_j = \varepsilon_0$  for all *j* and  $t_{j,j\pm 1} = t_{\text{CNT}}$  between all *j* and  $j \pm 1$  for the nearest-neighbor hoppings. The electronic part of  $H_{\text{SSH}}$  is given as follows [17]:

$$H_{\rm SSH} = -\sum_{n} t_{n+1,n} (c_{n+1}^{+} c_{n} + c_{n}^{+} c_{n+1}), \qquad (3)$$

in which  $t_{n+1,n}$  is the nearest-neighbor transfer integral and is given as

$$t_{n+1,n} = t_0 + \alpha (u_n - u_{n+1}), \tag{4}$$

where  $t_0$  is the hopping integral of an undimerized chain,  $\alpha$  is the electron-phonon coupling constant and  $u_n$  is the displacement of the *n*th carbon atom from its equilibrium position. The reference energy is chosen such that the carbon atom onsite energy is zero. For perfectly dimerized *trans*-PA,  $u_n$  and bandgap are given as  $u_n = (-1)^n u_0$  and  $2\Delta_0 = 8\alpha u_0$ , respectively. Throughout this study for  $2\Delta_0 = 1.4$ eV, we shall use the parameters of ref. [11], so  $\alpha = 4.1 \text{ eV/Å}$  and  $t_0 = 2.5 \text{ eV}$ . These correspond to an equilibrium dimerization amplitude  $u_0 \approx 0.04 \text{ Å}$ .

In *trans*-polyacetylene a soliton corresponds to a phonon field configuration that minimizes the total energy. In the presence of solitons the displacements of cabon atoms are determined in such a way to minimize the total energy and to give optimum shape for the soliton. Accordingly, the displacements of the carbon atoms are modeled as [18,19]

$$u_n = (-1)^n u_0 \prod_m \tanh\left[\frac{(n-m)a}{\xi}\right],\tag{5}$$

where  $2\xi \cong 14a$ , with a = 1.22 Å (lattice constant), is the width of a soliton, ma is the location of the *m*th soliton center on the chain. Finally  $H_{\rm C}$  is given as

$$H_{\rm C} = -t_{\rm C} (c_{\rm L}^+ c_1 + c_1^+ c_{\rm L} + c_{\rm R}^+ c_{\rm N} + c_{\rm N}^+ c_{\rm R}).$$
(6)

We consider a *trans*-PA molecule with N = 56 carbon atoms and with one state per site. In eq. (6),  $t_{\rm C}$  denotes the interaction between single electron state 1(N)in *trans*-PA molecule and the electron state in the left (L) and right (R) electrodes, respectively. Here we present a short description of the t-matrix technique and Landauer formalism which we have applied to calculate the electronic transmission through the CNT/*trans*-PA/CNT structure. Let us start by considering a general Hamiltonian as

$$H = \sum_{i} \left( |i\rangle \varepsilon_i \langle i| + t_{i,i+1} |i\rangle \langle i+1| + t_{i,i-1} |i\rangle \langle i-1| \right), \tag{7}$$

where  $\varepsilon_i$  is the on-site energy of the site *i* and  $t_{i,i\pm 1}$  are the nearest-neighbor hopping integrals between the sites *i* and  $i \pm 1$ . The electronic properties of this system is then studied through the following Schrödinger equation:

Pramana – J. Phys., Vol. 69, No. 4, October 2007 663

S A Ketabi, H Milani Moghaddam and N Shahtahmasebi

$$t_{i,i-1}\psi_{i-1} + (\varepsilon_i - E)\psi_i + t_{i,i+1}\psi_{i+1} = 0,$$
(8)

where  $\psi_i$  is the probability amplitude at site *i*. Solving for  $\psi_{i+1}$  we find the t-matrix formulation as

$$\begin{pmatrix} \psi_{i+1} \\ \psi_i \end{pmatrix} = \begin{pmatrix} \frac{E-\varepsilon_i}{t_{i,i+1}} & -\frac{t_{i,i-1}}{t_{i,i+1}} \\ 1 & 0 \end{pmatrix} \begin{pmatrix} \psi_i \\ \psi_{i-1} \end{pmatrix} = M_i(E) \begin{pmatrix} \psi_i \\ \psi_{i-1} \end{pmatrix},$$
(9)

where  $M_i(E)$  is the local t-matrix associated with site *i*. Defining  $U_i = \begin{pmatrix} \psi_i \\ \psi_{i-1} \end{pmatrix}$ and  $M(E) = \prod_{i=1}^N M_i(E)$  as the global t-matrix of the system, eq. (9) is generalized as follows:

$$\begin{pmatrix} \psi_{N+1} \\ \psi_N \end{pmatrix} = \begin{pmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{pmatrix} \begin{pmatrix} \psi_1 \\ \psi_0 \end{pmatrix} = \prod_{i=1}^N M_i(E) \begin{pmatrix} \psi_1 \\ \psi_0 \end{pmatrix},$$
(10)

where

664

$$M(E) = \begin{pmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{pmatrix}.$$
 (11)

We see that t-matrices depend on energy E. If the eigenenergies and  $U_1$  are known, then all the eigenfunctions will easily be calculated from the t-matrices. Now, we proceed to calculate the transmission coefficient T(E), whose magnitude is directly related to the conductance through the Bütticker–Landauer formula [20],

$$G = \frac{2e^2}{h}T(E).$$
(12)

In the absence of non-coherent elastic transport [21], inelastic scattering and electron-electron correlations, Landauer theory provides a general framework for calculations of the electronic current through mesoscopic conductors coupled to single or multi-channel quasi-one-dimensional leads. It relates the electronic current to the transmission probability for an electron incident from the source lead scattered elastically through the conductor into the drain. By connecting the *trans*-PA molecule to two semi-infinite carbon nanotubes, then T(E) is identical to the probability that an incident electron with energy E in the left-hand CNT emerges in the right-hand one. Using eq. (10), the transmission coefficient is given by [22-24]

$$T(q) = \frac{4(1-q^2)}{(Z+qY)^2 + (1-q^2)X^2},$$
(13)

where the dimensionless parameters q, X, Y and Z are given as follows:

$$q = 1 - \frac{E}{2t_{\text{CNT}}}; \ X = m_{22} + m_{11};$$
  

$$Y = m_{22} - m_{11}; \ Z = m_{21} - m_{12}.$$
(14)

 $t_{\text{CNT}} = 3 \text{ eV}$  is the hopping integral of semi-infinite CNTs and  $m_{ij}(i, j = 1, 2)$  are the matrix elements of the global t-matrix, M(E) of the system.

Pramana – J. Phys., Vol. 69, No. 4, October 2007

Electron transport through SWNT/trans-PA/SWNT structure



**Figure 2.** A plot of the electronic DOS vs. the dimensionless parameter Energy/ $t_{\text{CNT}}$  for the CNT/*trans*-PA/CNT system with the parameters of  $t_{\text{CNT}} = 3 \text{ eV}$  and  $t_{\text{C}} = 0.3 \text{ eV}$  as described in the text. Plots (a) and (b) show the results for the *trans*-PA molecule with N = 56 carbon atoms without soliton and with three solitons, respectively.

# 3. Results and discussion

Based on the formalism described in §2, we have investigated the electronic conduction properties of CNT/trans-PA/CNT structure in the presence of solitons. Figure 2 illustrates the electronic density of states (DOS) of the CNT/trans-PA/CNT system in the absence and in the presence of solitons (see panels (a) and (b), respectively). The plots show that the presence of solitons induces electronics states within the bandgap and causes a large enhancement in the conductance of the system. In figure 3 the conductance of the system is shown which corresponds to figure 2. In these figures the strength of CNT/trans-PA coupling is fixed. Similar calculations were performed for the system with different values of  $t_{\rm C}$ , and the results are shown in figure 4. This plot suggests that any increase in  $t_{\rm C}$  considerably enhances the conductance of the system. Also the order parameter  $\varphi_n = -(-1)^n u_0$ for three solitons in *trans*-PA molecule is shown in figure 5. For a fully dimerized chain  $u_n = (-1)^n u_0$ , with  $u_0 \approx 0.04$  Å and for doped samples, in the presence of solitons,  $u_n$  is given by eq. (5). The order parameter is an easy way to observe different soliton distributions along the trans-PA chains, since  $\varphi_n = 0$  means a soliton has been located at the nth site.

Pramana – J. Phys., Vol. 69, No. 4, October 2007

665

 $S\ A\ Ketabi,\ H\ Milani\ Moghaddam\ and\ N\ Shahtahmasebi$ 



**Figure 3.** The logarithm of conductance in units of  $G_0$  vs. the dimensionless parameter Energy/ $t_{\rm CNT}$  for the CNT/*trans*-PA/CNT structure with  $t_{\rm CNT} = 3$  eV and  $t_{\rm C} = 0.3$  eV. Plots (a) and (b) show the results for the *trans*-PA molecule with N = 56 carbon atoms without soliton and with three solitons, respectively.



Figure 4. Conductance in units of  $G_0$  vs.  $t_{\rm C}$ , the CNT/molecule coupling strength for the CNT/*trans*-PA/CNT structure with  $t_{\rm CNT} = 3$  eV, N = 56 carbon atoms and three solitons.

Pramana - J. Phys., Vol. 69, No. 4, October 2007



Figure 5. Order parameter,  $\varphi_n$ , for *trans*-PA molecule with N = 56 carbon atoms and three solitons.

# 4. Summary

In brief, we have studied in details the role of solitons and the CNT/molecule coupling strength on the conductance in the CNT/trans-PA/CNT structure. We have applied some well-known numerical procedures and models such as transfer-matrix technique, Landauer formalism as well as SSH Hamiltonian model to investigate the electron conduction through the CNT/trans-PA/CNT structure. Our results show that (i) the presence of solitons induces electronic states within the bandgap which give rise to large enhancement in the conductance and (ii) the conductance is sensitive to the CNT/trans-PA coupling, i.e., any increase in  $t_{\rm C}$  considerably increases the conductance of the system.

# References

- S Datta, W Tian, S Hong, R Reifenberger, J I Henderson and C P Kubiak, *Phys. Rev. Lett.* 79, 2530 (1997)
- [2] M P Samanta, W Tian, S Datta, J I Henderson and C P Kubiak, Phys. Rev. B53, R7626 (1996)
- [3] M Kemp, A Roitberg, V Mujica, T Wanta and M A Ratner, J. Phys. Chem. 100, 8349 (1996)
- [4] C Joachim and J F Vinuesa, Europhys. Lett. 33, 635 (1996)
- [5] V Mujica, M Kemp, A Roitberg and M Ratner, J. Chem. Phys. 104, 7296 (1997)
- [6] M Magoga and C Joachim, Phys. Rev. B56, 4722 (1997)
- [7] S N Yaliraki, M A Ratner, J. Chem. Phys. 109, 5036 (1998)
- [8] S P Hänggi, M Ratner and S Yaliraki, Chem. Phys. 281(2-3), 111 (2002)
- [9] J M Tour, Chem. Res. **33**, 791 (2000)
- [10] C Joachim, J K Gimzewski and A Aviram, Nature (London) 408, 541 (2000)
- [11] W P Su, J R Schrieffer and A J Heeger, *Phys. Rev.* **B22**, 2099 (1980)
- [12] N Nemec, D Tomanec and G Cuniberti, Phys. Rev. Lett. 96, 076802 (2006)
- [13] B Shan and K Cho, Phys. Rev. **B70**, 233405-I (2004)

Pramana – J. Phys., Vol. 69, No. 4, October 2007

- [14] J J Palacios, A J Perez-Jimenez, E Louis, E S Fabian and J A Verges, Phys. Rev. Lett. 84, 4693 (2000)
- [15] W Fa, J Chen, H Liu and J Dong, Phys. Rev. B69, 235413 (2004)
- [16] X Yang and J Dong, *Phys. Lett.* A330, 238 (2004)
- [17] A J Heeger, S Kivelson, J R Schrieffer and W P Su, Rev. Mod. Phys. 60, 781 (1988)
- [18] V M Agranvich and A A Maradudim, in Solitons (North-Holland, Amsterdam, 1986)
- [19] S Stafstrom and K A Chao, Phys. Rev. B30, 2098 (1984)
- [20] M Büttiker, Y Imry, R Landauer and S Pinhas, Phys. Rev. B31, 316207 (1985)
- [21] S Datta, Electronic transport in mesoscopic systems (Cambridge University Press, Cambridge, 1995) p. 102
- [22] E Macia and F D-Adame, Phys. Rev. Lett. 76, 2957 (1996)
- [23] X Wang, U Grimm and M Schreiber, Phys. Rev. B62, 14020 (2000)
- [24] E Macia and F D-Adame, Phys. Rev. Lett. 79, 5301 (1997)