

**Performance Management and Measurement
with Data Envelopment Analysis**

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Evaluation of electricity distribution sector in Iran using parametric and non-parametric methods

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ABSTRACT

This paper conducts a comparative technical efficiency analysis of 36 Electricity Distribution firms using data of 2007-2008 and two stochastic frontiers Production Function (DFPP) and Data Envelopment Analysis (DEA). The results of DEA and DFPP Analysis are compared with correlation method. This comparison indicates a relatively good correlation.

Keywords: Electricity Distribution Sector, Parametric Method, DEA

INTRODUCTION

This study applies two techniques of efficiency measurement in a sample of electricity distribution firms in Iran.

The aim of this paper is to compare the relative efficiency of 36 firms working in the Electricity Distribution Sector in Iran. For this purpose, DEA and DFPP models are applied to evaluate the efficiency of the firms.

Detailed statistics from Iranian Electricity consumption for the years 2007-2008 was used as the source of information for the variable of models.

PREVIOUS STUDIES

Callinan et al. (2008) tested the hypothesis that the economic transition toward a market economy increases the efficiency of firms. They studied 32 polish electricity distribution companies between 1997 and 2002 by applying common benchmarking methods to the panel, the non-parametric data envelopment analysis (DEA), the free disposal hull (F.D.H), and as a parametric approach, the stochastic frontier analysis (SFA). They found that the technical efficiency of the companies has indeed increased during the transition, while allocative efficiency has deteriorated.

Hatori (2001) conducted U.S.-Japan comparison of performance of electric utilities during 1982 through 1991, but it focuses on electricity distribution and used stochastic Frontier Analysis to estimate technical efficiency of the utilities.

Jamshid and Pollitt (2001) reported an efficiency of 63 European electricity distribution utilities to assess the potential of and issues involved in the use of cross-country analysis as input incentive regulation process.

The sample includes utilities from the UK, Norway, Netherlands, Portugal, Italy and Spain. They used the authors used DEA, SFA and COLS method with Diftusion models specifications to a set of data from 1997-8.

Martillo-Zambrano L.R. et al. (2001) reported that, parametric frontier models and non-parametric methods have monopolized the recent literature on productive efficiency measurement.

Park, Seo-UK and J.B. Luenard (2000) compared the efficiency of conventional fuel power plants in south Korea by comparison of parametric and non-parametric approaches.

DATA

Using data are three inputs and one output for 36 firms in Electricity distribution sector in Iran. In the models inputs and output are as follows:

- X_1 = number of professional employees
- X_2 = low voltage line (km)
- X_3 = capacity of transformers (MVA)
- Y = Total Electricity sales (MWh)

MODELS

The Parametric and Non-Parametric methods have been applied to measure efficiency in electricity distribution sector by researchers.

In this study, the CCR input oriented model is used to measure relative technical efficiency with constant return to scale (CRS).

In modeling deterministic frontier production function (DFPP) for electricity distribution sector, it was assumed that total Electricity sales (Y) is produced by three inputs, X_1, X_2, X_3 . A Cobb-Douglas functional form was first applied as follows:

$$y^j = \alpha_0 (\alpha_1^{\beta_1}) (\alpha_2^{\beta_2}) (\alpha_3^{\beta_3})$$

The deterministic frontier production that has not a random error function is estimated by using the Linear Programming Model as follows (Aigner et al., 1977):

$$\text{Min } Z = \alpha_0 + \alpha_1 \tau_1 + \alpha_2 \tau_2 + \dots + \alpha_n \tau_n$$

$$s.t.:$$

$$\alpha_0 + \alpha_1 (\ln X_{1j}) + \alpha_2 (\ln X_{2j}) + \dots$$

$$+ \alpha_n (\ln X_{nj}) > \ln (Y_j) \quad j = 1, \dots, n$$

$$\alpha_0, \alpha_1, \alpha_2, \dots, \alpha_n \geq 0$$

Where, $X_j = \sum_{i=1}^n \ln X_{ij} / n$

$$\bar{X}_1 = \sum_{j=1}^n \ln X_{1j} / n$$

$$\bar{X}_2 = \sum_{j=1}^n \ln X_{2j} / n$$

$$\bar{X}_n = \sum_{j=1}^n \ln X_{nj} / n$$

$$\alpha_0 = \ln A$$

The estimated model is as follows:

$$y^j = A_0 (\alpha_1^{\beta_1}) (\alpha_2^{\beta_2}) (\alpha_3^{\beta_3})$$

Where, $\alpha_0 = e^{-\ln A} = 1/A$

$$\alpha_1 = 0.0$$

$$\alpha_2 = 0.0$$

$$\alpha_3 = 0.0397$$

The coefficient of professional employees and low voltage line are zero, therefore in the final model, only capacity of transformers included.

In parametric model, the efficiencies are computed as follows:

$$\text{Efficiency of firm } j = y_j / \hat{y}_j$$

Where:

$$\hat{y}_j = \text{the actual output of firm } j$$

$$\alpha_0 = 0.0397$$

$$\hat{y}_j = \text{the function output of firm } j$$

$$j = 1, 2, \dots, 36$$

RESULTS

Results in terms of both Non-parametric (CCR) and parametric (deterministic frontier production function) efficiencies are given in Table (1).

The comparison of correlation coefficient ($\rho = 0.824$) indicates a good correlation between two approaches. In this case a null hypothesis (no difference in efficiencies average as evidenced by two approaches) can not be rejected at the significant level of 0.05.

The efficiency measures generated by the different approaches have similar results.

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Table (1): Efficiency results

#	EFF1	EFF2	#	EFF1	EFF2
1	0.867	0.860	19	0.647	0.420
2	0.678	0.670	20	0.896	0.850
3	0.687	0.720	21	1.0	1
4	0.630	0.570	22	0.813	0.770
5	0.830	0.870	23	0.560	0.570
6	0.722	0.840	24	0.563	0.530
7	0.604	0.550	25	0.491	0.430
8	0.815	0.750	26	0.599	0.610
9	0.609	0.630	27	0.708	0.720
10	0.568	0.570	28	0.814	0.710
11	0.781	1.0	29	0.750	0.770
12	0.679	0.630	30	0.603	0.570
13	0.872	0.930	31	0.580	0.620
14	0.904	0.990	32	0.525	0.580
15	0.884	0.750	33	0.520	0.490
16	0.624	0.540	34	0.519	0.520
17	1.0	0.740	35	1.0	0.760
18	0.797	0.760	36	0.905	0.900

#: Number of firm
 EFF1: CCR efficiency (with constant returns to scale)
 EFF2: Parametric efficiency (deterministic frontier production function)

Comparison: T-test results, paired samples statistics

Pair	Mean	N	Std. Deviation	Std. Error Mean
EFF1	0.7234	36	0.15117	0.02530
EFF2	0.6997	36	0.15947	0.02658

Paired Samples Correlations

Pair	N	Correlation	Sig.
EFF1 & EFF2	36	0.824	0.000

Paired Samples Test

	Mean	Std. Deviation	Std. Error Mean	95% confidence interval of the Difference		t	df	Sig. (2-tailed)
				Lower	Upper			
Pair EFF1-EFF2	0.02372	0.09241	0.1540	-0.00754	0.05499	1.154	35	0.132

EFF1: CCR efficiency
 EFF2: Parametric efficiency