## Abstracts of


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# Abstracts of the 41 ${ }^{\text {st }}$ Annual Iranian Mathematics Conference 

12-15 September 2010, University of Urmia,

Urmia, Iran

Department of Mathematics
Urmia University, Urmia-Iran

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| V. D. Breaz | Romania |
| A. Dujella | Croatia |
| A. Ebadian | Iran |
| T. Ghasemi Honary | Iran |
| K. Ivaz | Iran |
| M. Kuzucuoglu | Turkey |
| S. E. Mahmoodian | Iran |
| A. Mohammadpour | Iran |
| H. Mohebi | Iran |
| A. Razavi | Iran |
| A. Salemkar | Iran |
| M. M. Shikare | India |

## Preface

The 41st Annual Iranian Mathematics Conference is to be held in Urmia University at one of the most beautiful cities in Iran. On behalf of the organizing committee as well as the scientific committee, it is my pleasure to welcome all participants, especially the speakers. I would also thanks the invited speakers from home and abroad.

We have received about 1200 articles in English and Farsi of which 600 were accepted in the various fields of pure and applied mathematics. Typos and grammatical errors are due to authors. We have tried to provide the best for you from the least provided us. Anyway, I apologize in advance for any possible inconveniences will come and wish you a good time during the conference. Support from the following gratefully acknowledged: Ministry of Science, Technology and Research; Iranian Mathematical Society; organizing committee and scientific committee; Department of Mathematics of Tabriz University, especially Dr. Parviz Darania.

H. Behravesh<br>Secretary of the Scientific Committee

## Invited Speakers

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> From Invariant Theory To Almost Zero Modules Title Second Line 

Mohsen Asgharzadeh<br>Institute For Research In Fundamental Sciences (IPM)<br>Tehran, Iran.


#### Abstract

The aim of this expository talk is to introduce some of the homological conjectures to the participants. We start with the Hochster-Roberts theorem by which a ring of invariants of a linearly reductive group is Cohen-Macaulay. Then we recall the notion of tight closure as an auxiliary tool in the proof of Hochster-Roberts theorem. Our next aim is to define almost zero modules as a generalization of tight closure theory which was introduced and studied by Faltings.


Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# An Invitation To Hilbert $C^{*}$-modules 

Damir Bakic<br>University of Zagreb, Zagreb, Croatia


#### Abstract

A Hilbert $C^{*}$-module is a (right) module over a $C^{*}$-algebra A equipped with an A -valued inner product that is complete in the corresponding norm. The concept is introduced by I. Kaplansky in 1953. Since the definition naturally generalizes that of a Hilbert space, one might expect that many of the results from Hilbert space theory extend to this broader context. Although some generalizations of that kind are obtained, it turns out that many of some standard, even basic facts from Hilbert spaces do not hold for Hilbert $C^{*}$-modules. On the other hand, a consequence of allowing the inner product to take values in a $C^{*}$ algebra instead in the field of complex numbers is that some concepts and results for $C^{*}$-algebras generalize naturally to Hilbert $C^{*}$-modules. The talk will be devoted to selected topics from general theory of Hilbert $C^{*}$-modules. We shall emphasize some similarities as well as some drawbacks of the theory in comparison to the theory of Hilbert spaces and $C^{*}$-algebras, respectively. Some old and some new results will be presented. In particular, we shall touch upon the following subjects:


Kasparov's stabilization theorem,
Representations of Hilbert $C^{*}$-modules,
Extensions of Hilbert $C^{*}$-modules,
Hilbert $C^{*}$-modules over $C^{*}$-algebras of compact operators,
Frames in Hilbert $C^{*}$-modules.
In the final part of the talk we shall discuss some recent results from a joint work with Ljiljana Arambasic and Mohammad Sal Moslehian.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Elliptic Curves 

Andrej Dujella

University of Zagreb,
Zagreb, Croatia.


#### Abstract

Elliptic curves are important objects in many areas, such as number theory, algebraic geometry, complex analysis and public key cryptography. In this talk, we will give an introduction to elliptic curves over the rationals and describe basic algorithms for obtaining information on Mordell-Weil group. We will briefly mention cryptographic applications of elliptic curves over finite fields.


Mathematics Subject Classification: Primary 11G05; Secondary 14H52.
Keywords: Elliptic curves, rank, torsion group.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# High Rank Elliptic Curves Induced By Diophantine Triples And Congruent Numbers 

Andrej Dujella<br>University of Zagreb, Zagreb, Croatia.


#### Abstract

We describe methods used in construction of elliptic curves with relatively high rank in several interesting families of elliptic curves (e.g. curves with prescribed torsion group, congruent number curves, $\theta$-congruent curves and curves induced by Diophantine triples and quadruples).


Mathematics Subject Classification: Primary 11G05; Secondary 14H52.
Keywords: Elliptic curves, Diophantine m-tuples, Congruent numbers, $\theta$-congruent

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On Certain Special Families Of Univalent Analytic Functions <br> A. Ebadian 

Department of Mathematics,
Faculty of Science,
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Urmia,Iran


#### Abstract

We denote by $\mathcal{A}$ the class of all analytic functions f in the unit disc $\Delta=\{z \in \mathbf{C}:|z|<1\}$ with the normalization $f(0)=f^{\prime}(0)-1=0$. For a positive number $\lambda>0$, we denote by $U_{3}(\lambda)$ the class of all $f(z)=$ $z+\sum_{n=2}^{\infty} a_{n} z^{n} \in \mathcal{A}$ such that $a_{3}-a_{2}^{2}=0$ and satisfies the condition $$
\left|\left(\frac{z}{f(z)}\right)^{2} f^{\prime}(z)-1\right|<\lambda, \quad z \in \Delta
$$

A function $f \in \mathcal{A}$ is said to be in $\mathcal{S R}(\gamma)$ if $\left|\arg f^{\prime}(z)\right|<\frac{\pi \gamma}{2}$. In this paper, we find conditions on $\lambda, \alpha$ and $\gamma$ such that $U_{3}(\lambda)$ is included in $\mathcal{S}^{*}(\alpha)$ or $\mathcal{S S}(\gamma)$ or $\mathcal{S R}(\gamma)$. Here $\mathcal{S}^{*}(\alpha)$ and $\mathcal{S S}(\gamma)$ denote the class of all starlike functions of order $\alpha$, and the class of all strongly starlike of order $\gamma$, respectively.


Mathematics Subject Classification:Primary 30C45; Secondary 30C80.
Keywords: Coefficient inequality, analytic, univalent, close-to-starlike and starlike functions.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Module Homomorphisms On Fréchet Algebras Title Second Line 

T. Ghasemi Honary<br>H. Shayanpour<br>Tarbiat Moallem University,<br>No. 50 Taleghani Avenue, Tehran, I.R.Iran


#### Abstract

Let $A$ be a unital Fréchet algebra. We first present some results on the automatic continuity of $A$-module homomorphisms $\theta: X \rightarrow Y$, where $X, Y$ are Fréchet $A$-modules. Then we show that if there exists a continued bisection of the identity for $A$, then $\theta$ is automatically continuous, under certain condition on $X$. In particular, every homomorphism $\theta: A \rightarrow B$ is continuous for certain Fréchet algebras $B$ (or any Banach algebra $B$ ). Finally, we show that every unital Fréchet algebra, with a continued bisection of the identity, is functionally continuous.


Mathematics Subject Classification:Primary 46H40, Secondary 46H05.
Keywords: Automatic continuity, Continued bisection of the identity, Fréchet algebras, Module homomorphism, Homomorphism, Semisimple.

# On The Automatic Continuity Of n-Homomorphisms And Homomorphisms 

T. Ghasemi Honary

Tarbiat Moallem University, Tehran, I.R. Iran.


#### Abstract

Let $A, B$ be Banach algebras and $\theta: A \rightarrow B$ be a homomorphism. A theorem due to C.E. Rickart asserts that when B is strongly semisimple and $\theta$ is dense range, then $\theta$ is automatically continuous. Another well known theorem, due to B.E. Johnson, asserts that if $B$ is semisimple and $\theta$ is surjective, then $\theta$ is automatically continuous.

An $n$-homomorphism between two algebras $A$ and $B$ is a linear map $\theta: A \rightarrow B$ such that $\theta\left(a_{1} a_{2} \cdots a_{n}\right)=\theta\left(a_{1}\right) \theta\left(a_{2}\right) \cdots \theta\left(a_{n}\right)$ for all elements $a_{1}, a_{2}, \ldots, a_{n} \in A$. This notion is an extension of a homomorphism.

In this talk we obtain some results on the automatic continuity of $n$ homomorphisms between certain topological algebras as well as Banach algebras. In particular, we extend the results of Rickart and Johnson for $n$-homomorphisms, under certain conditions.


Mathematics Subject Classification: Primary 46H40, 46H05;
Secondary 47B48, 46L05, 46J05.
Keywords: Automatic continuity, Semisimple and strongly semisimple, Homomorphism and $n$-homomorphism, Dense range, Q-algebra, Fréchet algebra, lmc algebra, Factorizable algebra.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Universal Groups And Regular Limit Groups 

M. Kuzucuoglu

Middle East Technical University,<br>Ankara, TURKEY.


#### Abstract

We will give basic properties of countable locally finite universal groups constructed by P. Hall and the regular limit groups constructed by O. H. Kegel. We discuss the centralizers of bounded subgroups in regular limit groups.

Mathematics Subject Classification: Primary 20F50, ; Secondary


 20D06.Keywords: Locally finite Groups, Universal groups, regular limit groups.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Defining Sets Everywhere: Problems And Motivations 

Ebadollah S. Mahmoodian<br>Sharif University of Technology, Tehran, I.R. Iran.


#### Abstract

We present as examples, some problems which motivate undergraduates, or even high school students, to do research in mathematics. These problems are related to the speaker's research activity. They have been presented in the past to recruit very bright students. In this talk we will go through the roots of some these problems and elaborate the research topics behind them.


Keywords:Inequality

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Parametric Independent Component Analysis Of Stable Random Vectors 

Mohammadreza Ameri, Adel Mohammadpour, Vahid Nassiri and Mona Shokripour

Amirkabir University of Technology, Tehran, Iran.


#### Abstract

Consider the model $\mathbf{X}=A \mathbf{S}$, suppose that $\mathbf{X}$ is observed and we are interested in learning the mixing matrix $A$ such that the components of $\mathbf{S}$ become as independent as possible, this problem is known as independent component analysis (ICA). Many famous and efficient algorithms have been developed in order to solve this problem. As we know making the observed vector uncorrelated is an old problem in statistics and some solutions like principal component analysis (PCA) are used for it. These methods use the covariance matrix in order to decorrelate the observed vector. As we know, independence is a stronger property than uncorrelatedness, therefore, it is usual to use higher order statistics in order to achieve independence in the case of ICA. These methods work pretty well but until we have finite higher order moments.


Mathematics Subject Classification: Primary 60E07.
Keywords: Independent component analysis, $\alpha$-stable class of distributions, sub-Gaussian class of distributions, discrete spectral measure

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Criteria For Maximal Abstract Monotonicity With Applications In Optimization 

Hossein Mohebi<br>Shahid Bahonar University of Kerman,<br>Kerman, Iran


#### Abstract

In this paper, we develop a theory of monotone operators in the framework of abstract convexity. Indeed, by using an additivity constraint qualification, we prove a generalization of Fenchel's duality theorem in the framework of abstract convexity, and give criteria for maximal abstract monotonicity. Finally, we present necessary and sufficient conditions for maximality of abstract monotone operators.


Mathematics Subject Classification:Primary 47H05, 47H04, 52A01, 26A51; Secondary 26B25.

Keywords: Constraint qualification, Generalized Fenchel's duality, Monotone operator, Abstract monotonicity, Abstract convex function, Abstract convexity.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Generalizations Of Symmetric Spaces 

Asadollah Razavi<br>Amirkabir University of Technology, Tehran, Iran.


#### Abstract

Symmetric spaces are Riemannian manifolds together with a special structure, they were first defined and studied by E. Cartan [Ca1], and have been generalized to to s-manifolds by A.J. Ledger [Le1] and to reflection spaces by O.Loos [Lo1].Later they have been generalized to Sigma spaces by A. J. Ledger ,O. Loos and the author ([Lo2],[LR3]) . Also they have been generalized to projectively symmetric spaces by F. Podesta [Po1] and to weakly symmetric spaces by A. Selberg [Se1].All these generalization are for Riemannian case. Symmetric Finsler spaces have been defined and studied by S. Deng and Z. Hou [DH1] and D. Latifi and the author [LR1] and recently generalized to Finsler s-manifolds [HR1] and weakly symmetric Finsler spaces [HR2] by P. Habibi and the author.


Mathematics Subject Classification:53C60, 53C35.
Keywords: Finsler homogeneous space, Symmetric space,s-manifold, Symmetric Finsler space,Weakly Symmetric space,Weakly Symmetric Finsler space,Symmetric Finsler s-manifold, $\Sigma$-space.

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> The Index Complex Of Maximal Subalgebras In Finite Dimensional Lie Algebras 

Ali Reza Salemkar<br>Shahid Beheshti University, G.C., Tehran, Iran


#### Abstract

Let $M$ be a maximal subalgebra of a finite dimensional Lie algebra $L$. A subalgebra $C$ of $L$ is said to be a completion of $M$ in $L$ if $C$ is not contained in $M$ but every proper subalgebra of $C$ which is an ideal of $L$, is contained in $M$. The set $I(M)$ of all completions of $M$ is called the index complex of $M$ in $L$. This is analogous to the concept of the index complex of a maximal subgroup of a finite group, which has been studied by a number of authors. We use this concept to study the influence of the maximal subalgebras on the structure of a finite dimensional Lie algebra. In particular, we give some characterizations of solvable and supersolvable Lie algebras.


Mathematics Subject Classification: 17B05, 17B20, 17B30, 17B50.
Keywords: Lie algebras, index complex, solvable, supersovable.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Various Splitting Operations For Graphs, Binary Matroids And Their Applications 

Maruti Mukinda Shikare

University of Pune,
Maharashtra (India)


#### Abstract

Four types of splitting operations in Graph Theory have been studied on large scale y graph theorists. They include the splitting operation due to H. Fleischner [Eulerian Graphs and Related Topics, Part 1, Vol. 1, North Holland, Amesterdam (1990)], the -point splitting, and the nline splitting due to P. J. Slater [A classification of 4- onnected graphs, J. Combinatorial Theory, 17 (1974), 281-298] and the splitting of operations due to L. Lovasz [Combinatorial Problems and Exercises, North Holland, Amesterdam (1979)]. These operations have important applications in graph theory. We take review of these operations in graphs. These operations and a few related results have been extended from graphs to inary matroids [Raghunathan et. al., Splitting in a binary matroid, Discrete Math- matics, 184 (1997), 261-271]. Several results involving these operations in matroids ave been investigated. We discuss these results and also consider some of the appli- ations of these operations to matroid theory.


## Speakers

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran 

# Linearly ordered $P^{ \pm}$-spaces 

F. Azarpanah<br>Department of Mathematics, Chamran University, Ahvaz, Iran<br>M. Etebar<br>Department of Mathematics, Chamran University,<br>Ahvaz, Iran.


#### Abstract

In a linearly ordered topological space (LOTS), $P^{+}$-points, $P^{-}$points and naturally $P^{+}$-space and $P^{-}$-space are defined and an example of a $P^{+}$-space without $P^{-}$-points, which is also an example of a LOTS almost $P$-space without $P$-points is given. Using these concepts, we show that in the category of linearly ordered topological spaces, quasi $F$-spaces and almost $P$-spaces coincide. We also show that a LOTS is sequentially disconnected if and only if it is either disconnected or it has at least one almost $P$-point.


Keywords: Almost $P$-point, quasi $F$-space, $P^{+}\left(P^{-}\right)$-space, sequential space, sequentially connected space, tightness.

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# Some results on prime submodules of modules 

F. Arasteh

Department of Mathematics, Tehran-North Branch, Islamic Azad University, Tehran, Iran.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Solution of full interval linear equation 

# $A_{2 n \times n} X_{n \times 1}=b_{2 n \times 1}$ <br> based on Kaucher arithmetic 

N. Ardin ${ }^{1}$<br>Department of Mathematics, Qaemshar Branch, Islamic<br>Azad University, Qaemshahr, Iran.

## M. Adabitabar Firozja


#### Abstract

In this paper, first, we proposed Kaucher arithmetic for interval number and then solving the system $A_{2 n \times n} X_{n \times 1}=b_{2 n \times 1}$ where $a_{i j}=$ $\left[\underline{a_{i, j}}, \overline{a_{i, j}}\right]$ such that $\underline{a_{i, j}} * \overline{a_{i, j}}>0$ and $x_{j}=\left[\underline{x_{j}}, \overline{x_{j}}\right]$ and $b_{i}=\left[\underline{b_{i}}, \bar{b}_{i}\right]$.


Keywords: interval number, Kaucher arithmetic, linear system.

[^0]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

## ON MATRIX VARIATE t-DISTRIBUTION

## A. Iranmanesh

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## S. Armanfar

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#### Abstract

In this paper we consider the matrix variate $t$-distribution as generalization of multivariate $t$-distribution. A representation of this family is shown. Subsequently some important statistical properties are given.


Mathematics Subject Classification: 62H99
Keywords: Matrix variate normal distribution, matrix variate t-distribution, Wishart Distribution

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# Some extensions of Birkhoff polytope 

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#### Abstract

Let $\mathbf{M}_{n}$ be the algebra of all $n \times n$ real matrices. A matrix $D \in \mathbf{M}_{n}$ with nonnegative entries is called doubly stochastic if $D e=D^{t} e=e$, where $e=(1, \ldots, 1)^{t} \in \mathbb{R}^{n}$. The Birkhoff polytope $\Omega_{n}$ is the set of all $n \times n$ doubly stochastic matrices. In this paper we study some subpolytopes of Birkhoff polytope. Also we introduce some extensions of Birkhoff polytope and we investigate their properties.


Mathematics Subject Classification: Primary 15A04, 15A21, Secondary 15A51.

Keywords: Doubly stochastic matrix, Majorization; g-majorization, Polytope.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Some Necessary Conditions on the Support Sizes in $t$-Designs 

M. Ariannejad ${ }^{1}$<br>Department of Mathematics, University of Zanjan, P. O. Box 45195-313, Zanjan, Iran.


#### Abstract

We present some necessary conditions on the structure of support in t -designs. Some of these conditions are about the number and the range of occurrences of $i$-sets $(1 \leq i \leq t)$, some others are about the rage and the bounds for the support sizes.


Mathematics Subject Classification: 05B05, 05B07.
Keywords: t-Design, Support Size.

[^1]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference
12-15 September 2010, University of Urmia, Urmia-Iran

# The properties of (1,2)-pseudo Singer generator elements in general linear groups 

A. Azad ${ }^{1}$<br>Department of Mathematics, Arak University, P. O. Box 38156-879, Arak, Iran.


#### Abstract

In this paper we introduce (1,2)-pseudo Singer generator elements in finite three dimensional general linear groups and give some of its properties.


Mathematics Subject Classification: 20 D60.
Keywords: General linear group, non-commuting subset of finite groups.

[^2]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Pathological Properties of Operators with Weakly Dens Orbits 

A. Farokhinia<br>Department of Mathematics, Shiraz Azad University, Shiraz, Iran.<br>S. Aghashiri ${ }^{1}$<br>Department of Mathematics, Shiraz Azad University, Shiraz, Iran.


#### Abstract

In this paper we will study the lineability and spaceability of weakly hypercyclic and weakly supercyclic operators on a separable Banach Space $X$.


Mathematics Subject Classification: Primary 47A16, Secondary 47L10.

Keywords: Pathological Properties, Weakly Dense Orbits, Weakly Hypercyclic, Weakly Supercyclic.

[^3]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# SPECIAL WEYL PROJECTIVE CURVATURE ON FINSLER MANIFOLDS 

SAMANEH AMOZEGAR ${ }^{1}$

BEHZAD NAJAFI

[^4]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Characterization of Different Types of Foliations on the Tangent Bundle of a Finsler Manifold 

M. Nadjafikhah<br>Department of Mathematics, Iran University of Science<br>and Technology<br>F. Ahangari ${ }^{1}$<br>Department of Mathematics, Iran University of Science and Technology


#### Abstract

As the geometric structures that exist in Finsler geometry depend on both point and direction, the tangent bundle of a Finsler manifold is of special importance. In this paper, we have studied the different foliations on the tangent bundle of a Finsler manifold. We have mentioned some results about the vertical foliation. We have also shown that in some particular cases, the horizontal distribution is involuting. As a main result, we have showed that the integrability of the horizontal distribution, leads to a new type of foliation on the tangent bundle. This foliation is created by the set of vector fields which are symmetries of the vertical projector. We have proved that it can be regarded as a Riemannian foliation on the tangent bundle.


Mathematics Subject Classification: 53C12, 53C15, 53C22.
Keywords: Finsler manifold, foliation, vertical projector, holonomy, symmetry, bundle-like metric.

[^5]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Some Results on Linear Preserving Maps 

S. EBRAHIMI ${ }^{1}$<br>Department of Mathematics, Payame Noor University of Tehran, P. O. Box 11111, Tehran, Iran.


#### Abstract

Let $H$ be an infinite dimensional separable Hilbert space and $B(H)$ the algebra of bounded operators on $H$. In this paper we show if $\phi$ : $B(H) \rightarrow B(H)$ preserves ascent and discent of operators and preserves the essential spectrum also $\phi\left(T^{n}\right)=\phi(T)^{n}, \forall T \in B(H)$ and $\forall n \in N$ then $\phi$ preserves the set of Browder operators if and only if it preserves the set of polar operators if and only if it preserves the set of Fredholm and consequently the set of Weyl operators.


Keywords: Fredholm, Weyl, Browder, polar, essential spectrum

[^6]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> The First Survey for abilities of DEA in Solving SILP Problems 

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H.R.Sahebi

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## M.Zorroshd

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#### Abstract

We consider a model for data envelopment analysis with infinitely many decision- making units. The determination of the relative efficiency of a given decision-making unit amounts to the solution of a semi-infinite optimization problem. We show that a decision-making unit of maximal relative efficiency exists and that it is 100 Moreover, this decision-making unit can be found by calculating a zero of the semi- infinite constraint function. For the latter task we propose a bilevel algorithm. We apply this algorithm to a problem from chemical engineering and present numerical results.


Keywords: Flat module, C(X), zero-set, Tensor Product,Torsion free.

[^7]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# An Introduction to System Signatures 

F. Ebrahimi<br>Department of Mathematics, Azad Islamic University of Damavand, Damavand, Iran.


#### Abstract

The signature of a system with independent and identically distributed i.i.d.) component lifetimes is a vector whose $i$ th element is the probability that $i$ th component failure is fatal to the system. System signatures have been found to be quite useful tools in the study and comparison of engineered systems.


Keywords: Coherent system, Signature, Order statistics, Reliability, $k$ -out-of- $n$ system.

# A Study on the Free Oscillation of Pendulum Using Variational Approach Method and Comparison with Exact solution 

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#### Abstract

In this article, He's Variational Approach Method is applied to free oscillation of pendulum. We illustrate that the variational approach method does not require linearization or small perturbation. Comparison of the results which is obtained by this method with the obtained results by the exact solution reveals that the He's variational approach is very effective and convenient and can be easily extended to other nonlinear systems and can therefore be found widely applicable in mathematics, engineering and other sciences.


Mathematics Subject Classification: 00B05, 34A34, 34K13.
Keywords: Inequality, Oscillation of Pendulum, Nonlinear differential equation, Variational Approach Method, Approximate Analytical Solution, Exact Solution.

[^8]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# CHARACTER INNER AMENABILITY OF $A \hat{\otimes} B$ 

H.R. Ebrahimi Vishki ${ }^{1}$

## A.R. Khoddami


#### Abstract

We investigate the notion of character inner amenability for the projective tensor product of Banach algebras.


[^9]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Best Approximation for Convex Cones in 2-Inner Product Spaces 

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#### Abstract

In this article, we get some theorems to finding the best approximation elements in 2-inner product spaces.


Mathematics Subject Classification: Primary 41A65, Secondary, 41A15.
Keywords: 2-inner product spaces, 2-normed spaces, b-best approximation, b-proximinal, b-Chebyshev, b-dual cone.

[^10]
# Application of degenerate kernel method for a class of singular nonlinear integral equations 

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#### Abstract

A degenerate kernel method is applied to nonlinear integral equations on real line by approximating the kernel of integral equation by wavelets and pre-wavelets. Convergence rate of the approximate solution is proved in terms of the kernel decay rate and number of dilations and shifts used in approximation of the kernel.


Mathematics Subject Classification: 45G05, 65T60
Keywords: Nonlinear Singular Integral Equations, Wavelets.

[^11]
# Maximal Ideal Space of Extended Rational Functions Algebras 

A. Ebadian<br>Department of Mathematics, Urmia University,<br>M. A. Abolfathi ${ }^{1}$<br>Department of Mathematics, Urmia University,


#### Abstract

Let $K$ and $X$ be compact subset of $\mathbb{C}$ such that $K \subseteq X$. Set $R(X, K)=\left\{f \in C(X):\left.f\right|_{K} \in R(K)\right\}$ where $R(K)$ is the uniform closure of $R_{0}(K)$, the algebra of all rational functions with poles off $K$. In this paper, we obtain the maximal ideal space of $R(X, K)$.


Mathematics Subject Classification: 46J10, 46 J 15.
Keywords: Banach function algebra, Differentiable Lipschitz algebras, Extended Lipschitz algebra, Maximal ideal space, Rational functions.

[^12]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On Proper actions on anti de Sitter space $H^{1,2}$ 

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S.M.B. Kashani

Department of Mathematics, Faculty of Sciences, Tarbiat Modares University, P. O. Box 14115-157, Tehran, Iran.


#### Abstract

In this paper we study the anti de Sitter space $H^{1,2}$ under the action of a closed Lie subgroup $G$ of the isometry group Iso $\left(H^{1,2}\right)$. When the action is proper with an orbit of codimension one, we determine the acting group up to conjugacy, the orbits up to isometry and the orbit space up to homeomorphism, and we find some equivalent conditions on the orbits and the acting group.


Mathematics Subject Classification: 53C30, 57S25.
Keywords: Proper action, anti de Sitter space.

[^13]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> population models with diffusion , strong Allee effect and constant yield harvesting 

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FATEMEH AHMADI BALEF ${ }^{1}$
M.Sc. Student of Mathematics and member of Mathematics association, Islamic Azad University- Ghaemshahr Branch.


#### Abstract

The main purpose of this paper is the study of positive solutions distribution of reaction diffusion equations with strong Allee effect type growth and constant yield harvesting ( semipositone) via the method of sub super solution.


Mathematics Subject Classification: 54E70, 54H25.
Keywords: semipositione, Allee effect, Harvesting.

[^14]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference
12-15 September 2010, University of Urmia, Urmia-Iran

# Fibonacci Length Of an Efficiently Persented Metabelian $p$-Group 

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Department of Mathematics,
Islamic Azad University, Tabriz Branch Iran

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference
12-15 September 2010, University of Urmia, Urmia-Iran

# Homotopy Analysis Method for Computing Eigenvalues of Schrodinger Equation 

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## D. Ahmadian ${ }^{1}$

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#### Abstract

In this paper, we apply Homotopy Analysis Method (HAM) for computing the eigenvalues of Schrodinger problems.


Mathematics Subject Classification: Primary 65L15, Secondary 65L99, 34L10.

Keywords: Homotopy Analysis Method, Eigenvalues of Schrodinger Equation

[^15]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Varitational iteration method for solving mth-order boundary value problems 

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#### Abstract

In this paper, the variational method is applied to solve mth-order boundary value problems. Only one iteration is needed, and the obtained solutions are of remarkable accuracy. By giving three examples and comparing with the exact solution, the efficiency of the method will be shown.


Keywords: variational iteration, boundary-value problems, approximate solution, nonlinear problems.

[^16]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Quasi-multipliers on $F$-algebras 

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#### Abstract

In this paper we consider the notion of quasi-multipliers on an $F$ algebra $A$, not necessarily normed or locally convex. We study their bilinearity and joint continuity under some suitable conditions. We also consider the strict and quasi-strict topologies on the algebra $Q M(A)$ of all bilinear and jointly continuous quasi-multipliers of $A$ having a minimal approximate identity and extend several known results to this general setting.


Mathematics Subject Classification: Primary 46H05, Secondary 46A16, 47D30, 47B47.

Keywords: Quasi-multiplier, multiplier, $F$-norm, $F$-algebra, minimal approximate identity, ultra-approximate identity, factorable algebra, strongly factorable topological algebra, completeness, uniform boundedness principle..

[^17]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On Extension Of A Binary Matroid 

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#### Abstract

In this paper, we extend the notion of a point-addition operation from graphs to binary matroids. This operation can be expressed in terms of element-addition operation and splitting operation. We consider a special case of this construction and study its properties. We call the resulting matroid of this special case a $\Gamma$-extension of the given matroid. We characterize circuits and independent sets of the resulting matroids.


Mathematics Subject Classification: 05B35.
Keywords: Binary matroid, $Г$-Extension, Point-Addition.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference
12-15 September 2010, University of Urmia, Urmia-Iran

# An application of minimal ideals of finite semigroup 

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#### Abstract

In this paper we give an application of minimal ideal semigroup and its relationship with group kernel. In fact minimal ideal of semigroup is equal with group kernel. Of course if exist minimal ideal. As studied by L.-C. Kappe in 1999, the group


$G p(\pi)=<a, b, c \mid a b=b a c, b c=c b, a c=c a, a^{2^{\alpha}}=1, b^{2^{\beta}}=1, c^{2^{\gamma}}=1>$
where,
$\alpha \geq \beta \geq \gamma>1$ is finite and its order is $2^{\alpha+\beta+\gamma}$. Now we let
$S g(\pi)=<a, b, c \mid a b=b a c, b c=c b, a c=c a, a^{2^{\alpha}+1}=a, b^{2^{\beta}+1}=b, c^{2^{\gamma}+1}=c>$
where, $\alpha \geq \beta \geq \gamma>1$. We prove $S g(\pi)$ is finite and:

$$
|S g(\pi)|=|G p(\pi)|+2^{\alpha}+2^{\beta}+2^{\gamma}+2^{\alpha+\beta}+2^{\beta+\gamma}+2^{\alpha+\gamma} .
$$

Mathematics Subject Classification: Primary 20M05, Secondary 20D15.

Keywords: Minimal Ideal.

[^18]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran<br>\title{ Isometric copies of $\ell^{1}$ and $\mathbf{j}$-type mappings }<br>Zahra Eram<br>Department of Mathematics, University of Kurdestan, P. O. Box 416, Sannandaj, Iran.


#### Abstract

In this talk we discuss the existence of a fixed point for several classes of mappings (mappings admitting a center, nonexpansive mappings, asymptotically nonexpansive mappings) defined on the closed convex subsets of a Banach space satisfying some proximinality conditions. Furthermore, we discuss the closed bounded convex subsets of $\ell^{1}$ that fails the fixed point property for nonexpansive mappings.


Mathematics Subject Classification: 47H10, 47H09, 46B20. Keywords: j-type mapping, admitting a center, fixed point.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran<br>$\left(q, q_{1}\right)$-contraction of $(\epsilon, \lambda)$-type<br>P. Azhdari<br>Department of Statistics, Islamic Azad University -Nort<br>Tehran Branch, Tehran, Iran.


#### Abstract

In this paper, we obtain two fixed point theorems for $\left(q, q_{1}\right)$-contraction of ( $\epsilon, \lambda$ )-type and generalized $C$-contraction.


Mathematics Subject Classification: Primary 00X00; Secondary 00X00, 00X00.

Keywords: Probabilistic metric space, $\left(q, q_{1}\right)$-contraction of $(\epsilon, \lambda)$-type, generalized $C$-contraction, fixed point.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Stability Analysis of an HIV/AIDS Epidemic Model with Treatment Presented by Fractional Differential Equation 

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#### Abstract

In this article, we investigate the behavior of the equilibrium points of an HIV/AIDS epidemic model with treatment presented by Fractional Differential Equation. Then we compare the numerical solutions of this system with those found for integer order counterpart for some values of the parameters exist in the system.


Mathematics Subject Classification: 37N25, 65P99.
Keywords: HIV/AIDS Epidemic Model- Fractional Differential EquationReproduction Number

[^19]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> ON THE CARDINALITY OF NON-ISOMORPHIC MATROIDS 

H. Azanchilar<br>Department of Mathematics, Urmia University, P. O. Box 57135, Urmia, Iran.<br>\section*{S. Ahsani}<br>Department of Mathematics, Sahand University of Technology, P. O. Box 51335, Tabriz, Iran.

## Z. Assadi Golzar ${ }^{1}$

Department of Mathematics, Urmia University, P. O. Box 57135, Urmia, Iran.


#### Abstract

In this paper we have assessed the asymptotic number of non-isomorphic binary $n$-matroids and we have also determined that the cardinality of the set of non-isomorphic $(n+m)$-matroids is less or equal than the multiple of the cardinality of the set of non-isomorphic $n$-matroids and the cardinality of the set of non-isomorphic $m$-matroids


Mathematics Subject Classification: 05B35
Keywords: matroid, binary matroid, isomorphisms, equivalence, code, lattice, duality, minor, extention.

[^20]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On new scalar product in the vector space 

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#### Abstract

In this paper we define a scalar product on the vector space. If $H$ is pre-Hilbert space we study the relation of the old and new scalar product. We give a necessary and sufficient condition for which that the linear operator has a closed range.


Mathematics Subject Classification: 46C20, 47B07, 47A30.
Keywords: Hilbert space, closed operator, compact operator.

[^21]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran 

## Spectral Frames

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#### Abstract

In this paper we introduce the concept of spectral frames which is related to the concept of spectral measure and present some basic results and theorems about these frames. Also, we discuss about duals of spectral frames, perturbation of spectral frames and robustness of these frames to erasure of some elements.


Mathematics Subject Classification: 42C15, 41A58
Keywords: Lebesque integral, Hilbert space, Spectral measure, Borel set, frame Theory.

[^22]
# Some results on Suzuki generalized nonexpansive mappins 

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#### Abstract

We consider a single valued and a multivalued mapping on a uniformly convex Banach space $X$. Under the assumptions that the mappings satisfy the Suzuki condition, we shall prove a common fixed point for them. In this way, we generalize some earlier results of Dhompongsa et al.


Mathematics Subject Classification: 47H10, 47H09.
Keywords: nonexpansive mapping, multivalued mapping, common fixed point.

[^23]
# A theorem on globally Symmetric Finsler spaces 

R. Chavosh Khatamy<br>Department of Mathematics, Faculty of Sciences, Islamic<br>Azad University Tabriz Branch, Iran<br>M. Eslamian ${ }^{1}$<br>Department of Mathematics, Faculty of Sciences, Payem Noor University, Ahar Branch, Iran


#### Abstract

We consider a single valued and a multivalued mapping on a uniformly convex Banach space $X$. Under the assumptions that the mappings satisfy the Suzuki condition, we shall prove a common fixed point for them. In this way, we generalize some earlier results of Dhompongsa et al.


Mathematics Subject Classification: 47H10; 47H09.
Keywords: Finsler Spaces, Locally and globally symmetric

[^24]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Investigation of a boundary layer for an equation with inhomogeneous boundary conditions 

Siamak Ashrafi<br>Department of Mathematics, Maragheh Branch, Islamic Azad University-Maragheh - Iran.


#### Abstract

The investigation of the forming of the boundary layer is usually carried out by Euler scheme. The limit value is calculated for the obtained solution by tending small quantity to zero. If this value doesn't satisfy to the boundary conditions the boundary layer is formed in this point. Here, we consider a problem under non local boundary condition, that is suggested as an open problem in the paper [1].


Mathematics Subject Classification: 34E05,34E10,34e15
Keywords: Boundary layer,general non-local boundary condition, perturbed differential equation, Euler scheme.

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Simultaneous Confidence Intervals for the Parameters of Extreme Value Distribution Based on Records 

A. Asgharzadeh ${ }^{1}$<br>Department of Statistics, Faculty of Basic Science, University of Mazandaran, Post code 47416-1467,<br>Babolsar, Iran.

M. Abdi


#### Abstract

In this paper, we consider the simultaneous confidence intervals for the parameters of extreme value distribution based on record statistics. A numerical example with a simulated data set is presented to illustrate the proposed method.


Mathematics Subject Classification: 62F25, 65E15.
Keywords: Upper record, Simultaneous confidence intervals, Extreme value distribution.

[^25]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Finite Operator-valued tight Frames 

Mohammad Sadegh Asgari<br>Department of Mathematics, Faculty of Science, Islamic<br>Azad University, Central Tehran Branch,<br>Simayeiran St., Farahzadi Ave., West town, Tehran, Iran.


#### Abstract

In this paper we study the operator-valued frame potential on operatorvalued frames for finite-dimensional Hilbert spaces. We show that if the operator-valued frame potential restrict to suitable sets of operatorvalued frames, the local minimizers of this potential is a tight operatorvalued frame.


Mathematics Subject Classification: 42C15, 47C15, 46C05, 46L05.
Keywords: operator-valued frame, Bessel operator-valued sequence, operatorvalued frame potential.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# The Dissipative Zakharov-Kuznetsov Equation 

Amin Esfahani<br>School of Mathematics and Computer Science, Damghan<br>University, Damghan, Iran, Postal Code 36716-41167


#### Abstract

In this work we consider the generalized dissipative Zakharov-Kuznetsov equation. We will study the associated initial value problem in Sobolev spaces $H^{s}\left(\mathbb{R}^{n}\right)$ and some weighted spaces $\mathbf{F}_{r}^{s, p}$. We also prove an illposedness result in the anisotropic Sobolev spaces $H^{s, r}\left(\mathbb{R}^{2}\right)$ in two dimensional case.


Mathematics Subject Classification: 35Q35, 35K55, 35Q53. Keywords: Nonlinear PDE, Initial Value Problem, Dissipation.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Linearly ordered $P^{ \pm}$-spaces 

## F. Azarpanah

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#### Abstract

In a linearly ordered topological space (LOTS), $P^{+}$-points, $P^{-}$points and naturally $P^{+}$-space and $P^{-}$-space are defined and an example of a $P^{+}$-space without $P^{-}$-points, which is also an example of a LOTS almost $P$-space without $P$-points is given. Using these concepts, we show that in the category of linearly ordered topological spaces, quasi $F$-spaces and almost $P$-spaces coincide. We also show that a LOTS is sequentially disconnected if and only if it is either disconnected or it has at least one almost $P$-point.


Mathematics Subject Classification: Primary 54C40.
Keywords: Almost $P$-point, quasi $F$-space, $P^{+}\left(P^{-}\right)$-space, sequential space, sequentially connected space, tightness.

[^26]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> fuzzy coprimary submodules 

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#### Abstract

Let $R$ be a commutative ring with non-zero identity and $M$ a nonzero unitary $R$-module. This paper deals with the concept of fuzzy coprimary submodules. We define this notion and study some of its basic results. The behavior of this concept with fuzzy localization will be studied.


Mathematics Subject Classification: 08A72.
Keywords: fuzzy coprimary submodules, fuzzy attached primes, fuzzy prime and primary ideals

[^27]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# The stability analysis of meshless method for Schrödinger-KdV equation 

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#### Abstract

This paper presents analysis of the stability of RBF collocation scheme using matrix method for the coupled Schrödinger-KdV equations. Dependency of stability to eigenvalues of collocation matrices, time step size and other parameters for a fixed number of collocation points are discussed.


Mathematics Subject Classification: 41A21, 41A30, 41A63.
Keywords: Schrödinger-KdV equation, Radial basis functions.

[^28]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference
12-15 September 2010, University of Urmia, Urmia-Iran

# An Adaptive Retrospective Trust Region Method for Unconstrained Optimization 

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## M. Reza Peyghami

Department of Mathematics, K. N. Toosi University of Tech, P. O. Box 16315-1618, Tehran, Iran.


#### Abstract

In this paper, we present a new trust region method for unconstrained optimization which is a combination of an adaptive trust region method with the RTR method introduced by Bastin et al. in 2008 [?]. Using some standard assumptions on the problem, the global convergence and the first and second order optimality conditions have been provided on limit points of the sequence generated by the new algorithm. Numerical results of the new algorithm on CUTEr problems have been also reported and compared with the result of the RTR and adaptive trust region method.


Mathematics Subject Classification: 65K05, 65K10.
Keywords: Unconstrained optimization, adaptive trust region method, RTR.

[^29]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# finite element method and surface elliptic equations 

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#### Abstract

In this study we consider a new finite element method for discretization of elliptic equations on surfaces. The idea of this approach is to use finite element spaces that are induced by triangulations of an outer domain to discretize the partial differential equations (PDE) on surface. It has been shown that the method has optimal order of convergence both in the $H^{1}$ - and $L^{2}-$ norm.


Mathematics Subject Classification: 65N30, 65N12, 65N15.
Keywords: Finite element, Convergence, Error bounds.

[^30]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Differential Polynomial Rings over Weak-Armendariz Rings 

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## A. Moussavi

Department of Pure Mathematics, Faculty of Mathematical Sciences Tarbiat Modares University, P. O. Box: 14115-134, Tehran, Iran.


#### Abstract

Let $\delta$ be a derivation on a ring $R$ and $R[x ; \delta]$ be the differential polynomial ring over $R$. We introduce $\delta$-weak Armendariz rings which are a generalization of weak-Armendariz rings, and investigate their properties. We show that if $R$ is semi-commutative and $\delta$-compatible, then $R$ is $\delta$-weak Armendariz if and only if $R[x ; \delta]$ is weak-Armendariz. As a consequence we extend related results of [3].


Mathematics Subject Classification: Primary 16S36, Secondary $16 D 25$.

Keywords: weak-Armendariz ring, semicommutative ring, $\delta$-compatible ring, differential polynomial ring.

[^31]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

## LS[9](2,4,29) Exists

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#### Abstract

The existence of some family of large sets of size nine are investigated. We employ the Kramer-Mesner matrix to construct the missing case $L S[9](2,4,29]$. We also show that in cases $L S[9](2,3, v)$ and $L S[9](2,4, v)$ the trivial necessary existence conditions are sufficient.


Mathematics Subject Classification: Primary 05B05, Secondary 05B07
Keywords: t-design, large set.

[^32]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> $\tau$-Lifting and Strongly $\tau$-Lifting Modules 

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T. Amoozegar ${ }^{1}$


#### Abstract

In this article we introduce the notions of $\tau$-lifting and strongly $\tau$ lifting modules. The $\tau$-lifting modules generalize lifting modules but strongly $\tau$-lifting modules give a specialization of lifting modules. Necessary and sufficient conditions for finite direct sum of $\tau$-lifting (respectively strongly $\tau$-lifting) modules to be $\tau$-lifting (respectively strongly $\tau$-lifting) are obtained.


Mathematics Subject Classification: 16D90, 16S90.
Keywords: $\tau$-Lifting modules, Strongly $\tau$-Lifting modules.

[^33]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Pullback diagram in Hilbert $C^{*}$-modules 

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## M. Chakoshi

Department of Mathematics, Faculty of science, Islamic
Azad University-Mashhad Branch, Mashhad 91735, Iran.


#### Abstract

In this talk we study certain morphisms of linking algebras of Hilbert $C^{*}$-modules and extend some known results to generalized linking algebras. We also investigate pullback diagrams in Hilbert $C^{*}$-modules.


Mathematics Subject Classification: 46C50, 47L08.
Keywords: linking algebra, extension of Hilbert $C^{*}$-algebra, pullback.

[^34]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Short proofs of two known theorems on group coloring of graphs 

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#### Abstract

Lai and Zhang [Graphs Combin. 18 (2002), 147-154] proved that the group chromatic number of a simple $K_{5}$-minor free graph is at most 5. In addition, Lai and Li [Graphs Combin. 21 (2005), 469-474] gave the same result for a simple $K_{3,3}$-minor free graph. In this paper, we give a short proof of 5 -group choosability of $H$-minor free graphs, where $H \in\left\{K_{5}, K_{3,3}\right\}$.


Mathematics Subject Classification: 05C15, 05C20.
Keywords: Group choosability, $K_{5}$-minor free graphs, $K_{3,3}$-minor free graphs.

[^35]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# MAXIMUM AND MINIMUM OF THE SUM OF ELEMENT ORDERS OF FINITE GROUPS OF THE SAME ORDERS 

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#### Abstract

Given a finite group $G$, let $\psi(G)=\sum_{g \in G} o(g)$, where as usual, $o(g)$ is the order of the element $g$. In this paper we will show that the maximum value of $\psi$ on the set of groups of order $n$, where $n$ is a positive integer, will occur at the cyclic group $C_{n}$. We also investigate the minimum value of $\psi$ on the set of groups of the same order.


Mathematics Subject Classification: 20D60.
Keywords: Element Orders, Finite Groups.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Variational iteration method for solving non linear integral equations 

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#### Abstract

In this paper, we use a technique for solving integral equations which is based on He's variational iteration method. In this approach, at first, we turn the given integral equation to the integro-differential equation and next we apply the He's variational iteration method to get the values of approximate solutions. An example is solved to show the efficiency and accuracy of the method.


Mathematics Subject Classification: Primary 35A15, Secondary 45G10
Keywords: Variational iteration method, Non linear integral equations.

[^36]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Bifurcation of Hill Regions in Restricted Collisional $\mathrm{N}+1$-Body problem 

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#### Abstract

For restricted collisional N+1-body problem, we show the existance and describe regions in physical and configurational space where motion cannot occure. These regions are found by Hill in restricted three-body problem which is stablished as a model for three body system sun-earthmoon.


Keywords: celestial mechanics, restricted problems ,collision, bifurcation, jaccobian integral.

[^37]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Variational Iteration Method For Solving Non Linear Integral Equations 

J. Saberi-Nadjfi, M. Amin Khah AND R. Amiri

Department of Mathematics,
Ferdowsi university of Mashhad, Mashhad, Iran.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Multiplicity results for a critical quasilinear elliptic system with concave- convex nonlinearites 

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M. Amini ${ }^{1}$

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$$
\begin{gathered}
\text { Abstract } \\
\text { In this paper, we consider a quasilinear elliptic system } \\
\left\{\begin{array}{lr}
-\Delta_{p} u=\lambda|u|^{q-2} u+\frac{p \alpha}{\alpha+\beta}|u|^{\alpha-2} u|v|^{\beta} & \text { in } \Omega, \\
-\Delta_{p} v=\mu|v|^{q-2} v+\frac{p \beta}{\alpha+\beta}|u|^{\alpha}|v|^{\beta-2} v & \text { in } \Omega, \\
u=v=0 & \text { on } \partial \Omega,
\end{array}\right.
\end{gathered}
$$

Where $\lambda, \mu>0,1<q<p<N, \Delta_{p} u=\operatorname{div}\left(|\nabla u|^{p-2} \nabla u\right)$ is the $p$ Laplacian, $\alpha>1, \beta>1$ satisfy $\alpha+\beta=p^{*}$ and $p^{*}=\frac{p N}{N-p}$ denotes the critical sobolev exponent. By variational methods, we study multiplicity results of positive solutions.

Mathematics Subject Classification: 35j65, 35j50, 35 j 55.
Keywords: Elliptic system; Nehari manifold, Concave- convex, Critical sobolev exponet, Variational methods.

[^38]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On Bayesian Inference for Multivariate Normal Distribution 

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## N. khosravi


#### Abstract

In this talk we propose some characteristics of inverted matrix variate gamma distribution. Further Bayes estimators for multivariate normal distribution, using conjugate prior knowledge under square error and Kullback Leibler divergence loss functions, are also derived.


Mathematics Subject Classification: 62H99
Keywords: Bayes estimator, Conjugate prior distribution, Inverted matrix variate gamma distribution, Kullback Leibler divergence loss function, Multivariate normal distribution, Square error loss function

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> relations between dual of Bass numbers, Bass numbers and Betti numbers 

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#### Abstract

Let $R$ be a commutative Noetherian ring and $M$ be an $R$-module. For a prime ideal $\mathfrak{p}$ of $R$ the invariants $\pi_{i}(\mathfrak{p}, M)$ has been studied using the minimal flat resolution of $M$ over Gorenstein rings. In this study we will give some results about the numbers $\pi_{i}(\mathfrak{p}, M)$. Then some relations between Bass numbers, $\pi_{i}(\mathfrak{p}, M)$ and $\beta_{i}(M)$ will be investigated.


Mathematics Subject Classification: 13C11, 13E05.
Keywords: Bass number, dual of Buss number, Betti number.

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Delta-shape basis functions for solving RLW equation 

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## R. Mokhtari

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N.G. Chegini


#### Abstract

A meshfree technique based on a global collocation method using the Delta-shape basis functions for the numerical solution of the regularized long wave (RLW) equation is presented. Accuracy of the method is tested in terms of L2 and L $\infty$ error norms, propagation of single solution is simulated and conservation properties of mass, energy and momentum of the RLW equation are reported.


Mathematics Subject Classification: 65M70, 35C08.
Keywords: Delta-shape basis functions, RLW equation.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# AN ADJOINT BETWEEN POINTED AND POWER SET ALGEBRAS 

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S. N. HOSSEINI

[^39]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A new IDEA method for priority determination in AHP 

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#### Abstract

The estimation of the relative weights of criteria $\backslash$ alternatives plays an important role in the Analytical Hierarchy Process (AHP). In a conventional pairwise comparison matrix, 1-9 ratio scales are used to elicit exact comparisons. However due to uncertainty involved in real world, it is sometimes unrealistic and infeasible to acquire exact judgments. It is easier to provide interval judgments in a pairwise comparison matrix but sometimes our judgments are fixed points in an interval i.e. they are set data. In this paper we enter set data into a pairwise comparison matrix and propose a new imprecise data envelopment analysis (IDEA) method to deal with this situation.


Mathematics Subject Classification: Primary 00X00; Secondary 00X00.

Keywords: AHP, DEAHP, IDEA, $C C R-\varepsilon$, Assurance Region, Rank Reversal, set data, set efficiency.

[^40]
# HAWAIIAN GROUPS OF HAWAIIAN EARRINGS 

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#### Abstract

In this talk we intend to determine the structure of the n_dimensional Hawaiian group of the m-dimensional Hawaiian earring space, where $m, n \geq 1$. Also, we show that similar to homotopy functors, Hawaiian group functors preserve product, and for $n \geq 2$, Hawaiian groups are abelian.


Mathematics Subject Classification: Primary 55Q05, Secondary 55Q20, 54F15.

Keywords: Hawaiian group, Hawaiian earring, weak join.

[^41]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Generalized mean value theorem to Hadamard manifolds 

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#### Abstract

By using Clarke's subdifferential the Lebourg's mean value theorem is generalized to Hadamard manifolds. Then, some applications are introduced.


Mathematics Subject Classification: Primary 34A55, Secondary 34B24.
Keywords: Hadamard manifolds, locally Lipschitz functions, Mean value theorem.

[^42]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Inverse Minisum Location Problems with Variable Coordinates 

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#### Abstract

In this work, we consider the inverse minisum location problem with variable coordinates in $d$-dimensional real space in which the aim is to increase or decrease the coordinates of a set of given points at minimum total cost with respect to modification bounds such that a predetermined point becomes a minisum location. We develop polynomial time and pseudo-polynomial time solution algorithms for the problem under the rectilinear, the squared Euclidean and the Chebyshev distance norms. Moreover, we discuss the NP-hardness of the models under investigation.


Mathematics Subject Classification: Primary 90C27; Secondary 90B80, 90B85.

Keywords: location problems, Combinatorial optimization, Inverse optimization.

[^43]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On endomorphism ring of $*-$ prime modules 

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#### Abstract

An open problems about *-prime module stated in [?]. He asks for an example of a $*$-prime module whose endomorphism ring is not prime. We will try to answer to this open problem.


Mathematics Subject Classification: Primary 16S50, Secondary 16D10, 16D60, 16D80.

Keywords: *-prime modules.

[^44]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Locally graded groups with a Bell condition on infinite subsets 

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#### Abstract

Given an integer $n \neq 0,1$.let $\beta_{n}$ be the variety of $n$-Bell groups defined by the low $\left[x^{n}, y\right]=\left[x, y^{n}\right]$, and let $\beta_{n}^{*}$ be the class of all groups $G$ in which, for any infinite subsets X and Y of G , there exist $x \in X$ and $y \in Y$ such that $\left[x^{n}, y\right]=\left[x, y^{n}\right]$. We prove that every infinite $\beta_{n}^{*}$-group G is n -Bell in the following cases: G is finitely generated and locally graded; G is locally soluble; G is locally graded and $|n|$ or $|n-1|$ is equal to $2^{a} p^{b}$ (where p is a prime, and $\mathrm{a}, \mathrm{b}$ are non-negative integers).


Mathematics Subject Classification: 90C27; 90B80, 90 B 85.
Keywords: locally graded, $n$-Bell group, $v$-group.

[^45]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Derivation on Generalized Triangular Matrix Rings 

## M. Nader Ghosseiri and N. Baghershahi

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Sanandaj, Iran.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Coinvariants of quasi-Hopf bimodules over quasi-Hopf algebras as Hom-functor 

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#### Abstract

For a Hopf algebra $H$ and a right $H$-Hopf module $M \in \mathbb{M}_{H}^{H}$, the coinvariants submodule $M^{\mathrm{coH}}$ has been considered by Larson and Sweedler in order to prove the Fundamental Theorem of Hopf Modules. The coinvariants functor $(-)^{c o H}: \mathbb{M}_{H}^{H} \rightarrow \mathbb{M}_{k}$ has been observed by R. Wisbauer as the Hom-functor $\operatorname{Hom}_{H}^{H}(H,-)$ without needing any antipode.

Over a quasi-Hopf algebra $H$, the Fundamental Structure Theorem for quasi-Hopf $H$-bimodule has been formulated by introducing two versions of coinvariants as the inverse equivaleces for the comparison functor $-\otimes_{k} H:{ }_{H} \mathbb{M} \rightarrow{ }_{H} \mathbb{M}_{H}^{H}$.

In this paper, for a qusi-Hopf algebra $H$, we will introduce a version of Hom-functor as right adjoint to the comparison functor $-\otimes_{k} H$ : ${ }_{H} \mathbb{M} \rightarrow{ }_{H} \mathbb{M}{ }_{H}^{H}$. For this, we do not need any quasi-antipode. In case $H$ is a quasi-Hopf algebra, we show that this Hom-functor is inverse equivalence to the comparison functor and it is isomorphic to both generalized versions of coinvariants.


Mathematics Subject Classification: Primary 16W30; Secondary 18A40, 18D10.

Keywords: Quasi-Hopf algebra, Coinvariants, Monoidal category.

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# On the Ratio of Rice Random Variables 

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#### Abstract

The ratio of independent random variables arises in many applied problems. In this article, the distribution of the ratio $X / Y$ is studied, when X and Y are independent Rice random variables. Ratios of such random variable have extensive applications in the analysis of noises of communication systems. The exact forms of probability density function (PDF), cumulative distribution function (CDF) have been derived in terms of several special functions.


Mathematics Subject Classification: 33C90, 62E99.
Keywords: Rice Distribution, Ratio Random Variable, Special Functions.

[^46]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Krein Condition For The Existence Of Strongly Regular Graphs 

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Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Cartan equivalence problem for Riemannian metrics 

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#### Abstract

In present paper, we determine the Cartan local equivalences problem for the flat Friedman metric.


Mathematics Subject Classification: Primary 53A55, Secondary 53B21, 53B99.

Keywords: Cartan equivalence problem, Coframe, Gaussian curvature, The flat Friedman metric.

[^47]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Rough lattices 

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#### Abstract

In this papers, we apply rough sets on lattices and introduce the notions of rough sublattice and rough ideal. Also we prove some related properties of approximations in sublattices and ideals.

Mathematics Subject Classification: Primary 03XG10; Secondary


 18A32.Keywords: rough set; lower approximation; upper approximation; rough sublattice; rough ideal

[^48]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Solving Linear Fredholm Fuzzy Integral Equations Of The Second Kind By Artificial Neural Networks 

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Ferdowsi university of Mashhad, Mashhad, Iran.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# ON INTEGRABILITY OF ALMOST PRODUCT RIEMANNIAN STRUCTURES 

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#### Abstract

Let $M$ be a $C^{\infty}$ - manifold of finite dimension $n$. We denote by $\mathcal{T}_{s}^{r}(M)$ the module over $F(M)$ of all $C^{\infty}$-tensor fields of type (r,s) on $M$, where $F(M)$ is the algebra of $C^{\infty}$-functions on $M$. Let $M$ be an almost product manifold with almost product structure $\varphi$. It is well known that the integrability of $\varphi$ is equivalent to the vanishing of the Nijenhuis tensor $N_{\varphi}$. In this paper we consider another possible condition of the integrability of almost product structures on Riemannian manifolds.


Keywords: Product Structure, Manifold, Tensor field.

[^49]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> MULTI-VALUED $(\varphi-k)-B$ contraction 

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#### Abstract

In this paper, we shall generalize the definition of $(\varphi-k)-B$ contraction to multi-valued mappings. Then we shall prove two fixed point theorems for multi-valued $(\varphi-k)-B$ contraction mappings in probabilistic metric space.


Keywords: Probabilistic metric space, $(\varphi-k)-B$ contraction, fixed point.

[^50]
# Numerical solution of the nonlinear Klein-Gordon equation using cubic B-spline scaling functions and generalized Thin plate splines 

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#### Abstract

In this paper,we propose two numerical schemes for solving the nonlinear Klein-Gordon equation, using cubic B-spline scaling function and generalized thin plat splines.


Mathematics Subject Classification: 65D07, 65M06, 65Zxx.
Keywords: Klein-Gordon equation, Cubic B-spline scaling functions, Radial basis functions, Thin plate splines.

[^51]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A weighted algorithm based on variational iteration method for identifying heat transfer coefficient 

Kh. Paryab

A.R. Yazdanian ${ }^{1}$


#### Abstract

In this paper, we consider an inverse problem of heat equation with Robin boundary condition for identifying heat transfer coefficient. The numerical solution is developed by using a weighted algorithm based on variational iteration method. This method uses initial and boundary conditions simultaneously and effectively for constructing the solution. Using this method a rapid convergent sequence can be obtained which tends to the exact solution of the problem.


Mathematics Subject Classification: Primary 20F28, Secondary 20 E22.
Keywords: Heat transfer coefficient, Inverse problems, Variational iteration method

[^52]
# The Properties of Generalized Soluble Groups 

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#### Abstract

In the present article we introduce a new concept of generalized soluble groups, which will be called autosoluble groups. Using the autocommutators, a new series will be constructed, which is some how a generalization of the derived series of a given group. We determine the structure of such groups, when the generalized series are terminated.


Mathematics Subject Classification: 20D45, 20E36, 20K10, 20 K 15.
Keywords: Soluble group, autocommutator subgroup, absolute centre, autosoluble group.

[^53]
# Point Estimation for the Burr Type XII Distribution Based On Type II Censored Data 

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S. Asadi

Associate professor, Engineering College, Payame Noor University, Iran.


#### Abstract

This article deals with the point estimation of unknown parameters of the type II censored Burr Type XII distribution. We consider the maximum likelihood procedure of the unknown parameters. We also obtain Approximate Bayes estimators of the unknown parameters under the assumptions of gamma priors on both of them.


Mathematics Subject Classification: Primary 62N01, Secondary 62N02.

Keywords: Burr Type XII distribution, Bayes estimator, Maximum likelihood estimator, Type-II censoring.

[^54]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Minimal CL-Subgroups and Central automorphisms group of finite gourops 

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#### Abstract

Let $G$ be a finite group and $S_{G}$ be symmetric group of $G$. An automorphisms $\sigma$ of $G$ is said to be central if $\sigma$ commutes with every inner automorphisms of $G$. The central automorphisms group $A u t_{c}(G)$, is of great importance in studying $\operatorname{Aut}(G)$. We say that a subgroup $Q$ of $G$ is a centrally large subgroup, or CL-subgroup of $G$ if $|Q \| Z(Q)| \geq$ $\left|Q^{*}\right|\left|Z\left(Q^{*}\right)\right|$ for every subgroup $Q^{*}$ of $G$. In this note, we use minimal centrally large subgroups to obtain some further properties of $A u t_{c}(G)$. In particular, we obtain some sufficient conditions to show that $\operatorname{Aut}_{c}(G)=\operatorname{Aut}(G) / \operatorname{Inn}(G)$.


Mathematics Subject Classification: Primary 20F28, Secondary 20 E22.
Keywords: Centrally large subgroup, Central automorphisms, Full automorphisms group.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# comparing the interval efficiency ofradial non-radial and Hybrid models with together in DEA 

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#### Abstract

In this paper we introduce an interval Hybrid (IHybrid) model in data envelopment analysis (DEA) to find it's interval efficiency, then we extract the interval efficiency of radial and non-radial models from the proposed model. Finally in a theorem we will compare the interval efficiency of these models with together.


Keywords: IHybrid, $I$ Hybrid', ICCR, IBCC, ISBM, $I S B M^{\prime}$ interval efficiency.

[^55]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Bayes action for different balanced-type loss functions 

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#### Abstract

In this approach we propose constrained Bayes estimator in a normal population, when it is suspected that priori a pre-specified value may settle as the main parameter. The constrained Bayes estimator is derived under the balanced loss function for difference weight functions and the relative risk functions are also computed.


Mathematics Subject Classification: Primary 62F15; Secondary 62F30.
Keywords: Balanced loss function, Conjugate prior distribution, Constrained Bayes.

[^56]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran 

# F-Permutations Matrices 

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#### Abstract

In this paper, the concept of F-permutation is introduced. Then by applying this notion, we give a presentation of an F-permutation by F-permutation matrices. We show that, there is a one-to-one corresponding between all F -permutations on $n$-letters and all F-permutation matrices.


Mathematics Subject Classification: 20N25, 08A72.
Keywords: fuzzy permutation matrices.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# n-fold positive implicative hyper K-ideals 

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#### Abstract

In this paper we are supposed to introduce the definitions of $n$-fold positive implicative hyper K-ideals. These definitions are the generalizations of the definitions of positive implicative hyper K-ideals, which have been defined in [12]. Then we obtain some related results.


Keywords: Inequality.

[^57]
# THE USE OF MAPLE PLATFORM FOR THE STUDY OF GEODESICS IN THE SCHWARZSCHILD DE 

## SITTER SPACE-TIME

A. TALESHIAN ${ }^{1}$

M. EBRAHIMI

[^58]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Analytical and Numerical Solution of Hyperbolic Heat Conduction in Cylindrical Coordinates 

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H. Eskandar
S. Saedodin
P. Salehi


#### Abstract

In this paper, the hyperbolic effect in a cylinder subjected to a heat flux boundary condition is carried out. Equations are solved by deriving the analytical and the numerical solution of the hyperbolic heat conduction equation. The main aim of this paper is to obtain some possibly explicit analytical solution of the (1+2)-dimensional hyperbolic heat conduction equation for given initial and boundary condition with method of separation of variables.


Keywords: Analytical Solution, Numerical Solutin, Hyperbolic Equation, Separation of Variables

[^59]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference
12-15 September 2010, University of Urmia, Urmia-Iran

## Some types of hyper $M V$-ideals in hyper

 $M V$-algebrasL. Torkzadeh<br>Department of Mathematics, Islamic Azad University, Kerman Branch, Kerman,<br>Iran.


#### Abstract

In this paper we define hyper $M V$-ideals of types $1,2,3$ and 4 in hyper $M V$-algebras. Then we prove that hyper $M V$-ideals of type 1 and type 4 are equivalent and by some examples we show that the hyper $M V$ ideals of types 1,2 and 3 are not equivalent. Finally we determine the relationships between hyper $M V$-ideals of types 1,2, and 3 .


Mathematics Subject Classification: 06D35, 06F35, 03G25.
Keywords: Hyper $M V$-algebra, Hyper $M V$-ideal.

# Some Results on Associated Prime Submodules 

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#### Abstract

Let $R$ be commutative ring with identity and $M$ be a unitary $R$ module. the notions of associated and supported prime submodules are considered. Our aim is to extend the results concerning associated and supported prime ideals of a module and find new properties when the modules are multiplication, have finite length, are finitely generated or weakly finitely generated.


Keywords: Associated and supported prime submodules, Multiplication module, Prime submodules, Radical of a submodule.

[^60]
# A Fixed Point Theorem on Ordered Metric 

## Space

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#### Abstract

Fixed point results are presented for single-valued generalized weak contractions in a complete metric space endowed with a partial order.


Mathematics Subject Classification: 47H10.
Keywords: fixed point, generalized weak contraction, partially ordered set, lower semi-continuous.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Osculatory interpolation in non-overlapping domain decomposition method 

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#### Abstract

We present a non-overlapping domain decomposition method (DDM) for the method of fundamental solution (MFS) to improve the conditioning of the problem [?]. This method often deal with the Poisson-type equations by approximating a particular solution via radial basis functions (RBF). When imposing the Numann boundary condition, the use of osculatory RBF (ORBF) has a considerable effect on the accuracy. In the case of employing a non-overlapping DDM with an interface boundary, the physical matching conditions including a Nummann type are essentially applied. Therefore, the use of ORBF can improve the quality of the solution.


Mathematics Subject Classification: 65C20, 35A08, 65 M 55.
Keywords: Method of fundamental solution; Non-overlapping domain decomposition.

[^61]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Maximum Zagreb, Minimum Hyper-Wiener and Graph Connectivity 

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#### Abstract

Among all $n$-vertex graphs with edge or vertex connectivity $k$, i.e graphs with $\kappa=k$ or $\kappa^{\prime}=k$ for $1 \leq k \leq n-1$, the graph $G=$ $K_{k} \vee\left(K_{1}+K_{n-k-1}\right)$ is the unique graph with maximum sum of square of vertex degrees (i.e with maximum Zagreb index). This is also the unique $n$-vertex graphs with edge or vertex connectivity $k$ whose hyperWiener index is minimum.


Mathematics Subject Classification: 92E10, 05C05 .
Keywords: Graph invariants, Vertex-connectivity, Edge-connectivity, Zagreb index, Hyper-Wiener index, extremal graphs.

[^62]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Numerical Range of Some Weighted Composition Operators 

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#### Abstract

The theory of numerical range has played a crucial role in the study of some algebraic structures. The aim of this paper is to determine the numerical range of some weighted composition operators on the weighted Hardy space.


Mathematics Subject Classification: Primary 47B33, Secondary 47B37.
Keywords: weighted Hardy space, weighted composition operator, numerical range.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A class of Banach algebras induced by conditional expectations 

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#### Abstract

In this note by using some properties of conditional expectation operators a class of Banach algebras introduced and then some properties of this class will be investigated.


Mathematics Subject Classification: Primary 47B20, Secondary 47B38.
Keywords: Conditional expectation, multipliers, multiplication operators.

[^63]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran 

# fuzzy subgroups and fuzzy cosets 

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#### Abstract

In this paper, we introduce the concept of fuzzy sets and fuzzy subgroups and then we present some of its basic properties like left (right) cosets of fuzzy subgroups. First we introduce some new concepts of fuzzy group theory and then by using the definitions we obtain the same theorems and results on fuzzy cosets of a fuzzy subgroup and cosets of a subgroup of a group.


Keywords: fuzzy sets, fuzzy algebra, fuzzy subgroups, fuzzy cosets.

[^64]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Lattice NystrÖm methods for Hammerstein integral equations (HIE) 

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#### Abstract

We return to earlier work in Dick et al. J. Complexity 23 (2007), concerning to Fredholm linear integral equation of the second kind. In the present work, we emphasize the need for using Lattice-Nyström on nonlinear integral equation. Our study is motivated by problems in statistics and mathematical finance, where integral equations can arise as a result of financial applications. This method causes that the computational cost is to reduce. We obtain the solution of nonlinear integral equation by the Nyström method using N rank-1 lattice points.


Keywords: Nonlinear integral equation, lattice rules, financial mathematics.

[^65]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference
12-15 September 2010, University of Urmia, Urmia-Iran

# THE ASYMPTOTIC FORM OF EIGENVALES AND EIGENFUNCTION OF THE STURM-LIOUVILLE PROBLEM WITH DISCONTINUOUS CONDITIONS 

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A. JODAYREE AKBARFAM

[^66]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Ricci Flow and Bi-invariant Metrics on 

$$
\mathfrak{s l}(3, \mathbb{R})
$$

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#### Abstract

n compact Lie groups with bi-invariant metrics, all metrics are Einstein and therefore fix points of Ricci flow. In the paper, we will discuss non-compact Lie groups and we will prove that in this case bi-invariant metrics, if exist, are semi-metrics and Ricci flow is not necessarily an ODE.


Keywords: Lie Groups, Ricci Flow, Bi-invariant metrics

[^67]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> DUAL GENERALIZED QUATERNIONS IN SPATIAL KINEMATICS 

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#### Abstract

In this paper, the dual generalized quaternions are studied and some of their basic properties are investighated.Also, two Hamilton operators are defined and algebra of dual generalized quaternions is developed using these operators. Properties of Hamilton operators are then used to find some mathematical expressions for screw motion of a line and a point.


Mathematics Subject Classification: 15A33, 15A66, 53A17.
Keywords: Dual Generalized Quaternion, Hamilton Operator, Screw Motion.

[^68]
# Solving fractional Riccati differential equations using homotopy perturbation 

## Padé technique

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#### Abstract

In this paper, the homotopy perturbation method (HPM) is reintroduced with the enhancement of Padé approximants to lengthen the interval of convergence of HPM when used alone in solving nonlinear problems.


Mathematics Subject Classification: 34A08, 35C10, 26 A33.
Keywords: Riccati equation, Fractional derivative, Homotopy perturbation method, Padé approximants.

[^69]
# Stochastic Approximation Boosting Algorithm for Spatial Censored Data 

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#### Abstract

Sometimes we deal with situations where the data collection mechanism is such that the values of spatial phenomenon of interest is not completely observed. In such cases, we adopt a spatial model with censored data. Due to the likelihood function involves analytically intractable integrals and hence, direct maximization of the likelihood is numerically difficult, this work utilizes stochastic approximation boosting algorithm to obtain maximum likelihood estimates of the model parameters. In fact, this algorithm employs boosting with a variant of stochastic approximation to handle censored data problems.


Mathematics Subject Classification: Primary 91B72; Secondary 91D25, 62L20.

Keywords: Boosting; Spatial model; Censored data; Stochastic approximation.

[^70]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Maximum and Minimum Of The Sum Of Element Orders Of Finite Groups Of The Same Orders 

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# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> $\mathbf{C}^{1}$-PERSISTENTLY SENSITIVE HOMOCLINIC CLASSES 

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## S. Ashoori

H. Gharib

## S. Jalalipoo ${ }^{1}$


#### Abstract

Let $f$ be a diffeomorphism of a closed $n$-dimensional $C^{\infty}$ manifold, and $p$ be a hyperbolic saddle periodic point of $f$. In this paper, we introduce the notion of $C^{1}$-persistently sensitive for a closed $f$-invariant set. We prove that for the homoclinic class $H_{f}(p)$ of $f$, if $f_{\mid H_{f}(p)}$ is $C^{1}$-persistently sensitive then $H_{f}(p)$ admits a dominated splitting. Especially, on a 3-dimensional manifold, the splitting on $H_{f}(p)$ is partially hyperbolic, and if in addition, $f$ is far from homoclinic tangency, then $H_{f}(p)$ is strongly partially hyperbolic.


Mathematics Subject Classification: 37B20, 37C29, 37C50.
Keywords: Persistently sensitive, Homoclinic class, Dominated splitting, Partially hyperbolic, Strongly partially hyperbolic.

[^71]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# New approach for obtain bound for inverse of the tridiagonal matrix in general 

R. Jalilian


#### Abstract

The bound for inverse of the tridiagonal matrix $P_{n}\left(x_{i}, z_{i}, y_{i}\right)=\left[\delta_{i, j}\right]$ so that $\delta_{i, i}=z_{i}, \delta_{i, i-1}=-x_{i}$, and $\delta_{i, i+1}=-y_{i}$ are obtained if $x_{i} \geq$ $0, z_{i}>0, y_{i} \geq 0$, and $x_{i}+y_{i} \leq z_{i}$. Employing these expressions, we compute $\left\|P_{n}^{-1}\left(x_{i}, z_{i}, y_{i}\right)\right\|_{\infty}$ which is required in proving the convergence analysis of the numerical methods.


Mathematics Subject Classification: 34C12, 15A09, 65F05.
Keywords: Band matrix, Monotone matrix, Difference equation.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Adaptive Galerkin Frame Methods for Solving Operator Equations 

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#### Abstract

In this paper we use frames to construct corresponding trial spaces for an adaptive Galerkin scheme and design an adaptive algorithm in order to give an adaptive approximation solution to operator equations. We describe construction, prove error estimates for the resulting scheme and then investigate computational complexity.


Mathematics Subject Classification: 65J10, 65L99, 65F99.

Keywords: Frames. Adaptive solution. Galerkin method. N-term approximation. Quasi-Banach spaces $\ell_{\tau}^{\omega}(\Lambda)$.

[^72]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Solving boundary value problems of fractional order by Galerkin methods with fractional polynomials 

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#### Abstract

n this paper, we use the fractional polynomials on interval $[0,1]$ to solve the nonlinear boundary value problems of fractional order by Galerkin methods.


Mathematics Subject Classification: Primary 65L60, Secondary 34A08.
Keywords: Galerkin method, Fractional integral, Caputo fractional derivative, fractional polynomials.

[^73]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Crossed products of E-unitary inverse semigroups 

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#### Abstract

The main result of this paper is a partial crossed product decomposition for the $C^{*}$-algebras of a strongly $0-E$-unitary inverse semigroup. We first construct a partial action $\alpha$ of $G$ on the $C^{*}$-algebra of the semilattice of idempotents of a strongly $0-E$-unitary inverse semigroup $S$ and show that $C_{0}^{*}(S)$ is isomorphic to a crossed product of $C_{0}^{*}(E)$ by partial action $\alpha$ of group $G$.


Mathematics Subject Classification: Primary 16W22, Secondary 46L55, 16S35.

Keywords: crossed products, inverse semigroups, partial actions.

[^74]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A More General Case on the Norm of Extension of a Hilbert's Type Linear Operator in the continuous form 

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#### Abstract

The main purpose of this paper is to study a more general case on the norm of extension of a Hilbert's type linear operator in the continuous form. In addition to expressing the norm of a Hilbert's type linear operator $T: L^{2}(0, \infty) \rightarrow L^{2}(0, \infty)$, more general case such that $0<\lambda \leq$ 1 has been studied in this article. By putting $\lambda=1$ a norm of extension of Hilbert's integral linear operator is obtained.


Mathematics Subject Classification: 26D15, 47A07.
Keywords: Beta Function, Inner Product, Holder's Inequality, Norm, Hilbert's Inequality, Extension of Hilbert's Inequality.

[^75]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Infinitesimal Generator of A Unitary Operator on Hilbert $C^{*}$-modules 

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#### Abstract

In this talk, we investigate the infinitesimal generator of a $C_{0}$-group unitary operators in the framework of Hilbert $C^{*}$-modules.


Mathematics Subject Classification: Primary 46C50, Secondary 47L08.
Keywords: infinitesimal generator, $C_{0}$-semigroup, $C_{0}$-group, Hilbert $\mathcal{A}$ module, unitary operators, adjointable operators.

[^76]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Finite Volume Method for solution of Diffusion Equation 

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M. Hajisadeghi ${ }^{1}$


#### Abstract

This paper presents a finite volume method for diffusion equation on cartesian product nonuniform meshes in two dimensions. The error estimate in a discrete $H_{0}^{1}$ - and $L_{2}$-norm for the approximate solution is proved.


Mathematics Subject Classification: 74S10, 65N15.
Keywords: Finite volume methods, Error bound; Diffusion Equation, sobolev spaces.

[^77]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Special metric in product space 

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#### Abstract

In this paper we use tensor product to construct the curvature tensor of convolution manifolds and investigate fundamental property of this kind of manifolds. In particular we study the relationship between natural product manifold and convolution manifold.


Mathematics Subject Classification: 53B20, 53C50, 53C42.
Keywords: twisted product, warped product, convolution metric, flat convolution Riemannian manifold.

[^78]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# ON THE NORM OF CERTAIN COMPOSITION OPERATORS ON THE GENERALIZED HARDY SPACES 

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#### Abstract

In this paper, we obtain the norm inequality and the norm of certain composition operators on $H_{F, p}$.


Mathematics Subject Classification: Primary 47B33, Secondary 47B38.
Keywords: eneralized Hardy spaces, norm, norm inequality, Banach space.

[^79]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran 

## Bipartite IP-graph

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#### Abstract

The IP-graph of a naturally valenced association scheme arising from the transitive action of a group on a set and some of its properties has been studied recently. In this paper we introduce the bipartite version of this graph, namely bipartite IP-graph which we denote it by BIP. We also investigate some of its properties.


Mathematics Subject Classification: 05E30.
Keywords: Bipartite divisor graph, Association scheme.

[^80]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Locally regular Finsler $s$-manifolds 

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#### Abstract

In this paper we study locally regular Finsler $s$-manifolds. We introduce these spaces and show that any such space is homogeneous. Also we show that these spaces and the covering space of them are locally isomorphic.


Mathematics Subject Classification: 53C60, 53C35.
Keywords: s-structure, Generalized symmetric space, Locally regular Finsler $s$-manifold.

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran 

# Symplectic classification of 2-forms in dimension 4 

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#### Abstract

Classification of exterior 2-forms on 4-dimensional symplectic vector space ( $V, \Omega$ ) with structure 2 -forms $\Omega$ is considered. This classification will process by finding orbits of action $G L(V)$ on the space of 2-forms on 4 -dimensional symplectic vector space $V$ which is called Jacobi planes in the sequel.


Keywords: Symplectic Geometry, differential forms, Pfaffian.

[^81]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

## Best proximity pairs

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#### Abstract

. The object of our study is best proximity pairs and proximity points in normed space $X$. Also we give efficient algorithm for finding distance between two sets is presented


Mathematics Subject Classification: 41A65, 41A52, 46N10.
Keywords: Best proximity pairs, pair minimizing sequence, best proximity points.

[^82]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On properties of hyper $B C K$-ideals in the hyper $B C K$-algebras with condition r-m 

Habib Harizavi


#### Abstract

In this paper, we investigate the generated (weak)hyper $B C K$-ideal of the hyper $B C K$-algebra satisfying condition $\mathrm{r}-\mathrm{m}$ and show that the notions of weak hyper $B C K$-ideal and hyper $B C K$-ideal are coincide. Also we characterize the elements of generated hyper $B C K$-ideal.


Mathematics Subject Classification: 06F35, 03G25
Keywords: Inequality.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Poisson Generalized-Gamma Models 

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#### Abstract

This paper considers Poisson models and addresses the problem of overdispersion. We extend the common probability models for count data using mixture of Poisson and generalized gamma distributions to handle the problem. It is shown that the proposed model includes several distributions, previously adopted to the literature, as special cases. Furthermore, due to the computational complexity of integrals involved in the marginal likelihood, an alternative approach is suggested.


Mathematics Subject Classification: Primary 62JXX, Secondary 62J12
Keywords: Count Data, Mixed Models, Overdispersion, Random Effects.

[^83]
# Galerkin Method for Solving the Hyperbolic Telegraph Equation 

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#### Abstract

Recently, it is found that telegraph equation is more suitable than ordinary diffusion equation in modelling reaction diffusion for such branches of sciences. In this article, a numerical scheme for solving the onedimensional hyperbolic telegraph equation is presented. The method is based upon Legendre polynomials approximation. The properties of Legendre polynomials are presented. These properties together with Galerkin method utilized to reduce the telegraph equation to the solution of algebraic equations. The results of numerical experiments are presented, and are compared with analytical solutions to confirm the good accuracy of the presented scheme.


Mathematics Subject Classification: Primary 58J45, Secondary 37L65

Keywords: Inequality.

[^84]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

## An Adjoint Between Pointed Sets And Power Set Algebras

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Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Legendre wavelet method for solving multi-order fractional differential Equations 

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#### Abstract

In this paper Legendre wavelet and its operational matrix of integration are implemented to give approximate solutions for multi-order fractional differential equations. The main characteristic behind this technique is that it reduces such problems to those of solving a system of algebraic equations thus greatly simplifying the problem. Numerical results show that this approaches is easy to implement and accurate when applied to multi-order fractional differential equations


Keywords: Inequality.

[^85]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Numerical solution of integral equation by using combination of chebychev collocation method and lagrange interpolation 

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# Solving shortest path problem using IWO and IWO/PSO in graphs with negative weight cycle 

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#### Abstract

This paper presents two approaches based on invasive weed optimization (IWO) algorithm and hybrid of IWO and particle swarm optimization (IWO/PSO) to the shortest path (SP) routing problem in graphs with negative weight cycle. Route optimality ratios, which is obtained by applying these approaches on some case studies, show the efficiency of the given schemes.


Mathematics Subject Classification: 90C35, 90C59.
Keywords: Shortest path problem, Evolutionary optimization, Path encoding.

[^86]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A Mathematical Model for Steady blood flow in uniform straight and rigid circular tube 

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#### Abstract

In this paper an effort has been made to investigation the steady blood flow with periodic body acceleration in the presence of uniform transverse magnetic field by considering blood as a couple stress fluid in an uniform straight and rigid circular tube. The main idea of this work is the mathematical study of this phenomenon in order to obtain analytical expressions for axial velocity.


Mathematics Subject Classification: 76BXX; 76DXX.
Keywords: blood flow,Viscosity magnetic filed, body acceleration.

[^87]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On the Minimum of a Multivariate Pareto Distribution 

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#### Abstract

Assume that $\left(X_{1}, X_{2}, \ldots, X_{n}\right)$ is a multivariate Pareto random vector. This note calculates an analytic formula for density of minimum of a multivariate Pareto random vector and examines the effects of the distribution parameters on the first two moments of the minimum of $\left(X_{1}, X_{2}, \ldots, X_{n}\right)$.


Mathematics Subject Classification: 62G32
Keywords: heavy tail, minimum, moments, multivariate Pareto distribution, survival function.

[^88]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A class of integral table algebras of rank four 

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#### Abstract

In this note, we first classify integra table algebra of rank four such that one of its non identity basis element has degree 1 and two other basis elements are the same degree $\lambda \geq 4$. Then we prove that the Krein parameters of one of this classes are nonnegative real numbers


Mathematics Subject Classification: 20C99.
Keywords: Table algebra, Krein parameters.

[^89]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> ON RADICAL OF PRIMARY SUBMODULE OF MODULES OVER COMMUTATIVE RINGS 

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#### Abstract

In general the radical of a primary submodule is not prime as is valid in the ideal case. We give some sufficient conditions to this property holds in the module setting. Specially it is shown that, if $M$ is a onedimensional faithful multiplication module over a domain $R$ and $Q$ is a primary submodule of $M$. Then either $a n n M$ is a radical ideal or $\operatorname{rad} Q$ is $(r a d Q: M)$-prime.


Mathematics Subject Classification: Primary 13A15, Secondary 13C13.

Keywords: lMultiplication module, Cancellation module, Primary module.

[^90]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# THE $C^{*}$-ALGEBRA NUMERICAL RANGE OF A NILPOTENT ELEMENT 

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#### Abstract

Let A be a $C^{*}$-algebra with unit 1 . For each $\mathrm{a} \in \mathrm{A}$, let $\mathrm{V}(\mathrm{a})$, $\mathrm{v}(\mathrm{a})$ and $v_{0}(a)$ denote its numerical range, numerical radius and the distance from the origin to the boundary of its numerical range, respectively. If a is a nilpotent element of A with the power of nilpotency n , i.e., $a^{n}=0$, and $v(a)=(n .1) v_{0}(a)$, then we prove that $\partial V(a)$ does not contain any arc of circle.


Mathematics Subject Classification: Primary 47A12; Secondary 46K10.
Keywords: $C^{*}$-algebra Numerical range Numerical radius $C^{*}$ - algebra Nilpotent element

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A Fibering Map Approach to Quasilinear Elliptic Boundary Value Problem 

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# Interpolation Wavelets Based on Collocation Method for Solve Two-dimensional Fredholm Integral Equation 

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#### Abstract

In this paper, we study the numerical solution of two-dimensional Fredholm integral equation by collocation method. Also, supposing that solutions of these equations belong to $[-1,1]$, we use the interpolation wavelets, based on Chebyshev polynomials, for constructing the approximation subspaces. Numerical results are preformed in order to show the accuracy of the present work.


Keywords: Interpolation Wavelets, Collocation Method, Chebyshev polynomials.

[^91]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On eigenvalues and boundary curvature of the numerical rang of self-inverse operators 

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#### Abstract

For a bounded linear operator $A$ on a Hilbert space $\mathcal{H}$, let $M(A)$ be the smallest possible constant in the inequality $D_{p}(A) \leq M(A) R_{p}(A)$. Here $p$ is a point on the smooth portion of the boundary $\partial W(A)$ of the numerical range of $A . R_{p}(A)$ is the radius of curvature of $\partial W(A)$ at this point and $D_{p}(A)$ is the distance from $p$ to the spectrum of $A$. In this paper we compute the $M(A)$ for $A$ is self-inverse.


Mathematics Subject Classification: 47A12; 15A42; 14H50
Keywords: Numerical range,Eigenvalues, Curvature

[^92]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Numerical Solution of Abel'S Integral Equations Presented by A Fractional Differential Equation 

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#### Abstract

We present a method for solving Able's integral equations which is presented by a fractional differential equation. Some examples are given to show the accuracy of the method.


Keywords: Abel's integral, Fractional differential equation.

[^93]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran<br>\title{ A Numeration Method for Solving FDH-Hyperbolic Efficiency Models in DEA }<br>Khalil Paryab<br>Department of Mathematics, Iran University of Science<br>and Technology, Tehran, Iran<br>Paryab@iust.ac.ir<br>Rashed Khanjani shiraz ${ }^{1}$<br>Department of Mathematics, Iran University of Science and Technology, Tehran, Iran<br>Rashed-khanjani@yahoo.com


#### Abstract

This paper, introduces FDH-Hyperbolic efficiency(FDH-HE) and presents an algorithm for the computation of FDH-HE with various kinds of return to scale(RTS). The proposed algorithm obtains an optimal solution of FDH-HE without solving nonlinear integer programming problems.


## Mathematics Subject Classification:

Keywords: Data Envelopment Analysis (DEA); Free Disposal Hull (FDH); FDH-Hyperbolic Efficiency; Dominated unit .

[^94]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On $\mathcal{S G C}$-projective and $\mathcal{S G C}$-injective Modules 

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#### Abstract

Motivated by Bennis and Mahdu [?], we define the concept of a $\mathcal{S G C}$-projective, (resp., $\mathcal{S G C}$-injective) module $M$, and characterize these classes of modules, in terms of vanishing of the functors $\left\{E x t_{p_{C}}(M,-)\right\}_{i \geq 0}$ (resp., $\left\{E x t_{I_{C}}(-, M)\right\}_{i \geq 0}$ ). It is proved that a $\mathcal{S G C}$-projective (resp., $\mathcal{S G C}$-injective) module of finite $\mathcal{P}_{C}$-projective (resp., $\mathcal{I}_{C}$-injective) dimension is a $C$-projective (resp., $C$-injective) module.


Mathematics Subject Classification: 13D02, 13D05, 13D07, 18G15, 18G20, 18G25, 18G10.

[^95]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A Generalization of the SOR Method 

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#### Abstract

In this paper, a generalization of the successive overrelaxation (SOR) method is presented and its convergence properties are discussed. Some numerical experiments are given to show the efficiency of the proposed method.


Mathematics Subject Classification: Primary 65F10
Keywords: SOR, Generalized SOR, M-matrix, Convergence.

[^96]
# Solving systems of Fuzzy Linear Equations by Generalized Jacobi and Gauss-Seidel methods 

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#### Abstract

In many applications a solution to system of linear equations has to be found. In this paper we introduce the generalized Jacobi and Gauss-Seidel iterative methods for fuzzy linear system $A X=Y$ when coefficients matrix $A$ contains crisp entries and $Y$ is an arbitrary fuzzy vector. It will also be illustrated by some examples.


Keywords: Fuzzy linear system, Jacobi and Gauss-seidel methods.

[^97]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> An oscillation criterion for second order delay differential equations 

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#### Abstract

In this paper, we propose an oscillation criterion for second order delay differential equation.


Mathematics Subject Classification: Primary 34C10, 34K11; Secondary 34 K 06 .

Keywords: Oscillation, delay differential equation.

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference 

12-15 September 2010, University of Urmia, Urmia-Iran

# Elliptic Curves and their application in $C_{A}$ - Curves 

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#### Abstract

Now days, elliptic curves cryptosystems (ECC) receive attention and much efforts are being dedicated to make it more and more practical. However on the other hand elliptic curves are too special objects in the mathematical background to used for cryptosystems.

In the presented paper we study a new class of curves, i.e. $C_{A^{-}}$ curves. we use elliptic curves properties to make $C_{A}$-Curves, then see the application of these curves in cryptography.


Keywords: Elliptic Curve, $C_{A^{-}}$Curve, Weierstrass Equation, Cryptography.

[^98]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Characterizations of generalized derivations and generalized Jordan derivations on Banach algebras 

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#### Abstract

Let $\mathcal{A}$ be an algebra and $\mathcal{M}$ be an $\mathcal{A}$-bimodule. Let $X$ be in $\mathcal{A}$ and $\delta: \mathcal{A} \rightarrow \mathcal{M}$ and $\tau: \mathcal{A} \rightarrow \mathcal{M}$ be linear maps which satisfies $\delta(A B)=$ $\delta(A) B+A \tau(B)$ and $\tau(A B)=\tau(A) B+A \tau(B)$ for all $A, B \in \mathcal{A}$ with $A B=X$. It is shown that $\delta$ is a generalized Jordan derivation if $\delta$ is continuous and X is left (or right) invertible. Also, it is shown that $\delta$ is a generalized derivation if X is idempotent such that for $M \in \mathcal{M}$ the condition $X \mathcal{A}(I-X) M=0$ implies $(I-X) M=0$ and the condition $M X \mathcal{A}(I-X)=0$ implies $M X=0$.


Keywords: Generalized derivations, Generalized Jordan derivation, Banach algebras.

[^99]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Global nonexistence for a nonlinear mean curvature equation 

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#### Abstract

In this work we consider a nonlinear mean curvature equation, with dirichlet boundary value conditions. we show that the solution blows up in finite time even for negative initial energy.


Keywords: mean curvature, nonglobal solution, weight space.

[^100]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On universal covering for Lie tori 

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#### Abstract

In this paper we will provide a model for the universal coverings of Lie tori and we prove that the universal covering of a Lie $\Lambda$-torus of type $\Delta$ is again a Lie $\Lambda$-torus of type $\Delta$.

Mathematics Subject Classification:


[^101]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A new family of elliptic curves with positive rank 

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#### Abstract

In this paper, we are going to introduce a new family of elliptic curves with positive rank. These elliptic curves have been constructed with certain rational numbers, namely $\mathrm{a}, \mathrm{b}$, and c . It turns out that the torsion group of these curves are of the form $\frac{\mathbb{Z}}{2 \mathbb{Z}} \times \frac{\mathbb{Z}}{2 \mathbb{Z}}$.


Mathematics Subject Classification: Primary 14G05; Secondary 14H52, 11G05.

Keywords: Elliptic curves,Rank,Torsion.

# A numerical solution of the Rayleigh equation by parameter-expansion method 

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#### Abstract

In this paper, an approximate solution of the nonlinear oscillator known as the Rayleigh equation is presented. This is application of parameter-expansion method to obtain an approximate solution and frequency of equation. Parameter-expansion method (PEM) suggested by Ji-Huan He have been proved to be a very effective and useful method for handling nonlinear problems.


Mathematics Subject Classification: Primary 34C15; Secondary 39A11, 81Q15, 34E10.

Keywords: Parameter-expansion method; Rayleigh equation.

[^102]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Synchronization of the new chaotic system via linear feedback control 

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#### Abstract

This paper presents the linear feedback control laws to synchronize of the new chaotic system described in [Physica A 373 (2009) 36373642]. The sufficient conditions for achieving the synchronization of two identical systems are derived based on Lyapunov stability theorem. The proposed controller ensures that the states of the controlled chaotic response system asymptotically synchronizes to the states of the drive system. Finally, numerical simulations are presented to demonstrate the effectiveness of the proposed chaos synchronization scheme.


Mathematics Subject Classification: Primary 74H65; Secondary 37N35, 37N30.

Keywords: Chaotic system; Synchronization; Linear feedback control; Lyapunov stability theorem.

[^103]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A new characterization of inner product spaces 

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#### Abstract

In this talk we present a new characterization of inner product spaces related to the $p$-angular distance.


Mathematics Subject Classification: 46C15; 46B20; 46C05.
Keywords: inner product space, characterization of inner product spaces, $p$-angular distance, Dunkl-Williams inequality.

[^104]
# New generalization of some famous integral inequalities for pseudo-integrals 

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#### Abstract

In this paper, we study Jensen and Chebyshev type inequality for pseudo-integrals and prove a Stolarsky type inequality for pseudo-integrals where $g:[0,1] \rightarrow[0,1]$ is an increasing function and continuous generator of the pseudo-addition $\oplus$ and the pseudo-multiplication $\odot$. More precisely, we show that: $$
\int_{[0,1]}^{\oplus} f\left(x^{\frac{1}{a+b}}\right) d x \geq\left(\int_{[0,1]}^{\oplus} f\left(x^{\frac{1}{a}}\right) d x\right) \odot\left(\int_{[0,1]}^{\oplus} f\left(x^{\frac{1}{b}}\right) d x\right)
$$ where $a, b>0, f:[0,1] \rightarrow[0,1]$ is a continuous and strictly decreasing and $\mu$ is the Lebesgue measure on $\mathbf{R}$.


Mathematics Subject Classification: 03E72; 26E50; 28E10.

Keywords: Stolarsky inequality, Jensen inequality, Chebyshev inequality, pseudo-integral.

[^105]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Numerical solutions to fractional-order heat equations 

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#### Abstract

In this study we investigate the numerical solutions of fractionalorder heat equations. According to the Grunwald-Letnikov discretization method, fractional-order derivative is discretized to a difference equation system. Then the result difference scheme is used to achieve some numerical solutions to fractional-order heat equation. The numerical results will be compared to some classical results related to heat equations for efficiency of our method.


Mathematics Subject Classification: 26A33; 35K05; 65M06.
Keywords: fractional differentiation,Fractional-order heat equation

[^106]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran 

# On Products of Characters 

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#### Abstract

Let $G$ be a finite $p$-group, for some prime $p$, and, $\psi, \theta \in \operatorname{Irr}(G)$ be irreducible complex characters of $G$. It has been proved that if, in addition, $\psi$ and $\theta$ are faithful characters, then the product $\psi \theta$ is a multiple of an irreducible or it is the nontrivial linear combination of at least $(p+1) / 2$ distinct irreducible characters of $G$. We show that if we do not require the characters to be faithful, then given any integer $k>0$, we can always find a $p$-group $P$ and irreducible characters $\Psi$ and $\Theta$ of $P$ such that the product $\Psi \Theta$ is the nontrivial combination of exactly $k$ distinct irreducible characters.


Keywords: p-group, characters.

[^107]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

## An Explicit Construction of Einstein Randers Metrics With Non-constant Flag Curvature

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# PERTURBED ITERATIVE ALGORITHM FOR IMPLICIT VARIATIONAL-LIKE INCLUSIONS 

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[^108]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Stability of linear time varying delay dynamical systems on time scales and applications to delay control systems 

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#### Abstract

In this article we have considered the stability of delayed linear time varying systems on time scales. Using the Lyapunov function, sufficient delay dependent conditions for the exponential stability are given. The existence of the solution of Riccati equations $(R E)$ and linear matrix inequalities ( $L M I$ ) guarantee the exponential stability of linear time varying delay systems on time scales. The results are extended to linear time varying delay control systems.


Keywords: Exponential stability, Time scale, Time varying, Matrix inequalities, Lyapunov function, Riccati equation, Delay control system.

[^109]
# Application of Regularization Method for Solving an Inverse Parabolic Problem 

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#### Abstract

his paper deals with estimation of unknown surface heat flux in one dimensional inverse heat conduction problem . The fundamental solution of heat equation, together with prescribed initial and boundary data defined on the domain of problem are used to construct a system of integral equations on the boundary of domain. The discrete approximation of the problem is based on the finite differences method for system of integral equations. The standard Tikhonov regularization technique with the generalized cross-validation (GCV) criterion for choosing regularization parameter.


Mathematics Subject Classification:35R30; 35A08; 35K05; 74S20.
Keywords: Inverse Problem, Regularization Method, Regularization Parameter, Inverse Problem.

[^110]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran 

# $B(H, K)$ as a Hilbert $C^{*}$-module 

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#### Abstract

For Hilbert spaces $H$ and $K, B(H, K)$ is a Banach space but it is not a Hilbert space. In the present paper we consider $B(H, K)$ as a Hilbert $B(K)$-module and study some properties about operators on this especial space.


Mathematics Subject Classification: 46L08; 46B28; 46C50.
Keywords: Hilbert $C^{*}$-module, Adjointable operator, Positive operator.

[^111]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Inverse spectral analysis for the SturmLiouville equation with spectral parameter in the boundary conditions 

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#### Abstract

In this paper, we study Sturm-Liouville problems with spectral parameter linearly contained in one of the boundary conditions. We give uniqueness theorem for the solution of the inverse problem according to the spectral data. Then, we recover the potential function and coefficients of boundary conditions from the spectral data.


Mathematics Subject Classification: 34B24; 34A55; 34L05.
Keywords: Sturm-Liouville, Inverse problems, Spectral parameter, Eigenvalue.

[^112]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Using Buchberger's Criteria For Computing Computing comprehensive Grobner Bases 

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# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Numerical solution of differential equations by neural network 

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#### Abstract

In this paper, a novel hybrid method based on optimization techniques and neural networks method for the approximate solution of differential equations(DEs), is presented.


## Mathematics Subject Classification:

Keywords: bernoulli differential equations; neural network;
Feedforward artifical neural network.

[^113]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A priori error estimate for SD-Methods of a Strongly Damped Wave Equation 

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#### Abstract

We return to earlier work in Thomee and Wahlbin, BIT Numer. Math. 44 (2004), concerning to finite element method for a strongly damped wave equation and finding maximum norm estimates. In the present work, we use streamline diffusion methods (SD) as spatial discretization. Therefore, the regularity requirements on the a priori error estimation is computed.


Mathematics Subject Classification: 65M15; 65N12, 65N30.
Keywords: Streamline diffusion methods, strongly damped wave equations, a priori error estimate, finite element.

[^114]
# On approximate additive-quartic and quadratic-cubic functional equations in two variables in non-Archimedean spaces 

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#### Abstract

We establish the generalized Hyers-Ulam stability of the additivequartic and quadratic-cubic mappings with two variables in non-Archimedean spaces.


Mathematics Subject Classification: 39B82, 39B52.
Keywords: Hyers-Ulam-Rassias stability, quadratic functional equation, cubic functional equation, quartic functional equation, quintic functional equation, Non-Archimedean space.

[^115]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On the non-riemanian aspects of projective finsler geometry 

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[^116]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference
12-15 September 2010, University of Urmia, Urmia-Iran

# The Properties of autocentral series of abelian groups 

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#### Abstract

In the present paper we introduce the lower autocentral series of autocommutator subgroups of a given group. Using our previous work in 2010, it is shown that every finite abelian group is isomorphic with $n^{\text {th }}$-term of the lower autcentral series of some finite abelian group.


Mathematics Subject Classification: 20D45, 20D25; 20E34, 20E36, 20K10.

Keywords: Autocentral series, autocommutator subgroup, Sylow subgroups, abelian group.

[^117]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A New Algorithm for Computing Sagbi-Grobner Bases 

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Department of Mathematics, Damghan University, Damghan, Iran.

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Cyclic $S$-posets satisfying Condition $\left(E^{\prime}\right)$ <br> Parisa Rezaei <br> mohammadreza rahmati ${ }^{1}$ <br> Department of Mathematics, University of Sistan and <br> Baluchestan, Zahedan, Iran. 


#### Abstract

Condition ( $E^{\prime}$ ) of right posets was defined by Rezaei in 2009(see[4]). In this paper, we discuss Condition $\left(E^{\prime}\right)$ of one element and cyclic Sposets.


Mathematics Subject Classification: Primary 00X00, Secondary 00X00, 00X00.

Keywords: Cyclic $S$-poset, Condition ( $E^{\prime}$ ), Left po-collapsible.

[^118]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Linear maps preserving the set of Fredholm operators and essential spectral radius 

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#### Abstract

Let $H$ be an infinite-dimensional separable complex Hilbert space and $\mathcal{B}(H)$ the algebra of all bounded linear operators on $H$. In this paper we characterize surjective linear maps $F: \mathcal{B}(H) \rightarrow \mathcal{B}(H)$ preserving the set of Fredholm operators in both directions. As an application we prove that $\phi$ preserves the essential spectrum if and only if the ideal of all compact operators is invariant under $\phi$ and the induced linear map $\varphi$ on the Calkin algebra is either an automorphism, or an antiautomorphism. Moreover, linear maps from $\mathcal{B}(H)$ onto itself preserve the essential spectral radius.


Mathematics Subject Classification: Primary 41A58, 42C15.
Keywords: linear preservers, Fredholm operators,Calkin algebra

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On Fréchet Frames 

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#### Abstract

In this paper, the concept of frame for Fréchet spaces will be introduced and some of its properties will be investigated. Also invariance of this kind of frames under perturbation will be shown.


Mathematics Subject Classification: 42C15, 42C20, 46A13, 46A45.
Keywords: Banach frame, Fréchet frame, pre-Fréchet frame.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Using Block pulse functions for solving integral equations with time delay 

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#### Abstract

This article proposes a simple efficient method for solving integral equations with time delay. By using block pulse functions and their operational matrix of integration, integral equation can be reduced to a linear lower triangular system which can be directly solved by forward substitution. Numerical examples show that the approximate solutions have a good degree of accuracy.


Mathematics Subject Classification: 45D05, 45B05, 45D99.
Keywords: Block pulse functions, Operational matrix, Integral equations with time delay, Delay operational matrix.

[^119]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference 

12-15 September 2010, University of Urmia, Urmia-Iran

# The Chinese remainder, Going up and lying over theorems in Basic logic algebras 

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#### Abstract

In this paper, by considering the notion of residuated lattice and BL algebra, we concern a relationship between the important theorems in commutative algebra and BL-algebra theory.


Mathematics Subject Classification: Primary 03G25,13B24,13B30,06D35.
Keywords: residuated lattice, BL-algebra, MV-algebra, Going up theorem.

[^120]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> reconstruction of a jacobi matrix from mixed eigendata 

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#### Abstract

In this paper we consider the construction of a $n \times n$ jacobi matrix J of the form $$
J=\left(\begin{array}{cc} J_{1} & b_{k} e_{k} e_{1}^{T} \\ b_{k} e_{k}^{T} e_{1} & J_{2} \end{array}\right)
$$ from mixed eigendata $\lambda_{1}, \mu_{1}, \mu_{2} \in \Re, X=\left(x_{1}, x_{2}, \ldots, x_{n}\right) \in \Re^{n}, Y_{1}=$ $\left(y_{1}, y_{2}, \ldots, y_{k}\right) \in \Re^{k}, Y_{2}=\left(y_{k+1}, y_{k+2}, \ldots, y_{n}\right) \in \Re^{n-k}$ such that $X=$ $\lambda C X, J_{i}=\mu_{i} C_{i} Y_{i}, i=1,2$, where $C$ is a given jacobi matrix. Here $0<k<n$ and $J_{1}, J_{2}$ are $k \times k$ and $(n-k) \times(n-k)$ square matrices, respectively. Indeed We consider a generalized inverse eigenvalue problem of the form $J u=\lambda C u$.


Mathematics Subject Classification: 65F15, 65H15.
Keywords: Jacobi matrix;Eigenvectors;Inverse eigenvalue problem.

[^121]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On a Class of Analytic Functions Defined by Gaussian Hypergeometric Function 

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#### Abstract

In this paper by making us of Gaussian hypergeometric function a new class of analytic univalent functions in the unit disc $U=\{z ;|z|<$ $1\}$ is defined. some results about this class are obtained.


Mathematics Subject Classification: Primary 30C45; Secondary 30C45, 30C45.

Keywords: Univalent function, starlike function, convex function, Gaussian hypergeometric function.

[^122]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# finite element method and surface elliptic equations 

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#### Abstract

In this study we consider a new finite element method for discretization of elliptic equations on surfaces. The idea of this approach is to use finite element spaces that are induced by triangulations of an outer domain to discretize the partial differential equations (PDE) on surface. It has been shown that the method has optimal order of convergence both in the $H^{1}$ - and $L^{2}-n o r m$.


Mathematics Subject Classification: 65N30, 65N12, 65N15.
Keywords: Finite element, Convergence, Error bounds.

[^123]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# THE NEIMARK-SACKER BIFURCATION AND ITS DYNAMICAL ECONOMIC MODEL 

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#### Abstract

The paper describes the Hick Samuelson Keynes dy- namical economic model with discrete time and consumer senti- ment. We seek to demonstrate that consumer sentiment may cre- ate uctuations in the economical activities. The model possesses a Neimark-Sacker bifurcation.


Variational problems, Euler-lagrange equation

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On frame Wavelet Sets for 

$L^{2}(\hat{G}) \oplus L^{2}(\hat{G})$

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#### Abstract

For a locally compact abelian ordered group $G$, we introduce frame wavelet sets on the Pontryagin dual $\hat{G}$ of $G$. This is done systematically by a set of group isomorphisms that induces some equivalence relations on $\hat{G}$, which determine required Haar measurable subsets of $\hat{G}$.


Mathematics Subject Classification: 46N99, 46B28, 11K70.
Keywords: frame,wavelet, wavelet set.

[^124]
# Colon of Varieties in the semimodule $\zeta(M)$ 

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#### Abstract

Throughout, unless otherwise stated, all rings are commutative rings and all modules are unitary. In this work, the colon $(V(K): V(N))$ in the $\zeta(R)$-space $\zeta(M)$ is considered, when $K$ and $N$ are submodules of an $R$-module $M$. In particular for a submodule $N$ of $M$, It is shown that, if $(N: M)$ is a prime (resp. primary) ideal of $R$, then $(V(N): V(M))$ is a prime (resp. primary) ideal of $\zeta(R)$. The reverse containment holds, when $M$ is finitely generated or a multiplication module.


Mathematics Subject Classification: Primary 13C05,13C13; Secondary 54B99.

Keywords: Multiplication module, radical submodule, Prime submodule.

[^125]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Killing form of lie algebras 

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#### Abstract

In this paper, we study ad(adjoint) and kiling forms. we consider properties of kiling form and use some results of it and present example for kiling form. At end, we prove theorems of kiling form and adjoint


Keywords: kilking form, lie algebra, bilinear form.

[^126]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Generalizations of symmetrics spaces 

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[^127]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Computation of exact inertia of large sparse symmetric matrix 

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#### Abstract

If A is a symmetric matrix then the Sylvester law of inertia provides us with diagonal pivoting factorization for compute the inertia of $A$. in the case that $A$ is a large and sparse matrix; this factorization is not useful (see $[1-2]$ ). In this paper we develop an algorithm based on Krylov subspace method for computing the exact inertia of a real symmetric matrix without computing the eigenvalues. The implementation of the final algorithm has been tested by numerical examples, the results show that the algorithm converges fast and works accurately.


Mathematics Subject Classification: Primary 65L15; Secondary 65F15, 65F50.

Keywords: Inertia-Krylov-exact-symmetric.

[^128]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# beta exponentiated Weibull Distribution and its application 

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#### Abstract

In this paper, we introduce the beta exponentiated Weibull distribution for which the exponentiated Weibull is a special case. Various properties of the new distribution are discussed. The density function can be expressed as a mixture of the exponentiated Weibull densities. Some mathematical properties of the new distribution is obtained in terms of the corresponding properties of the exponentiated Weibull distribution. We obtain expressions for the density, mgf and moments. Estimation of the parameters is derived using the method of maximum likelihood. Simulation study is given.


Keywords: exponentiated Weibull; hazard function; maximum likelihood.

[^129]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Constructing Strictly Inductive limits in Locally convex cones 

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#### Abstract

We introduce a way of constructing strictly inductive limits in locally convex cones. By this definition, we prove that the strict inductive limit of a sequence of locally convex cones with the strict separation property has the same strict separation property. Also we establish that the strict inductive limit of a sequences of separated cones is separated too. Finally we verify barreledness for this strict inductive limit.


Mathematics Subject Classification: Primary 46A03; Secondary 46A08, 46A13.

Keywords: locally convex cone, convex quasiuniform structure, inductive limit.

# APPLICATION OF DIFFERENTIAL TRANSFORM METHOD TO ABEL'S INTEGRAL EQUATIONS 

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#### Abstract

A method for solving Abel's integral Equations is given by using the differential transform method. The approximate solution is calculated in the form of a series with easily computable terms and also the exact solutions can be achieved by the known forms of the series solutions. Several examples are given to demonstrate the reliability and the performance of the presented method.


Keywords: Abel's integral, Volterra integral equation, differential transform.

[^130]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Explicit solution of the polynomial least squares approximation problem on modified Chebyshev exterma nodes 

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#### Abstract

In this paper, obtaining explicit solution of polynomial least squares approximation on modified Chebyshev exterma[2]nodes is done. We also show that the inverse of normal matrix on this set of nodes can be represented as the sum of two symmetric matrices: a full rank matrices which admits a Cholesky factorization and a 2 -rank matrix. Some Numerical examples will be presented to illustrate efficiency of the proposed method.


Mathematics Subject Classification: Primary 41A10; Secondary 11Y05, 05A19.

Keywords: Polynomial Approximation; Cholesky Factorization; Combinatorial Identities.

[^131]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On the existence of homoclinic orbits for generalized Liénard systems 

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## V. ROOMI ${ }^{1}$


#### Abstract

In this work we study the existence of homoclinic orbits of the planer system of Liénard type $\dot{x}=h(y-F(x))$ and doty $=-g(x)$ where $h$ is strictly increasing and $h( \pm \infty)= \pm \infty$. We present sufficient and necessary conditions for this system to have homoclinic orbits. The conditions obtained are very sharp.


Mathematics Subject Classification: 37C29, 34A12.
Keywords: Homoclinic orbit, Liénard system.

[^132]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A numerical study of extraction well equation 

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#### Abstract

In this study, the groundwater flow will be considered. A nonlinear diffusion equation is investigated numerically in a single injectionextraction well.


Mathematics Subject Classification: 35K20, 35K61, 76S99.
Keywords: extraction well, nonlinear diffusion equation, numerical solution, Adomian-decomposition method.

[^133]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> ELMRES for Solving Ill-posed Linear System of Equations 

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#### Abstract

tiny The solution of large linear discrete ill-posed problem $A x=b$ where $A$ and $b$ are contaminated by noise, by iterative methods has recently received considerable attention. Due to the severe ill-conditioning of $A$ and $b$, the meaningful solution of this equation is not yield, obviously. Regularization is the best way to avoid this problem. Tikhonov regularization minimizes a least-square problem instead of solving the original system that is less sensitive to perturbations. Here we apply Tikhonov regularization to solve ill-posed problems by ELMRES method. Future discussions and numerical example will certified the efficiency of Tikhonov for solving this kind of problems.


Mathematics Subject Classification: Primary 65-XX, Secondary 65Fxx , 65F10.

Keywords: Tikhonov regularization, ELMRES, GMRES, Least square problem.

[^134]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Variation of induced linear operators 

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#### Abstract

Let $V$ be an $n$-dimensional inner product space and $G$ be a subgroup of the symmetric group $S_{m}$. Let $\lambda$ be an irreducible character of $G$, and let $V_{\lambda}(G)$ be the symmetry class of tensors associated with $\lambda$. Let $A$ be a linear operator on $V$ and let $K_{\lambda}(A)$ be the operator it induces on $V_{\lambda}(G)$. We obtain an upper bound and a lower bound for the norm of the derivative of the map $A \rightarrow K_{\lambda}(A)$. This leads to a bound for the distance between the induced operators of two operators. Also we obtain the norm of this map exactly, when $\lambda$ is the principal character of $G$. This problem have been studied for case $G=S_{m}$ in [2, 3].


Mathematics Subject Classification: Primary 15A69, Secondary 20C15, 47A60.

Keywords: Symmetry class of tensors, Induced linear operator, Derivative, Norm.

[^135]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference
12-15 September 2010, University of Urmia, Urmia-Iran

# NUMERICAL SOLUTIOS OF THE SECOND-ORDER PARTIAL DIFFERENTIAL EQUATIONS OF ELLIPTIC TYPE BE USING HPM QND GREENS FUNCTION 

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[^136]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# The continuous Galerkin method for the wave equation with optimal a priori error estimates and minimal regularity assumption 

Fardin Saedpanah


#### Abstract

The classical wave equation on a bounded convex domain is considered. Then a continuous Galerkin method, based on piecewise linear polynomials both in space and time, is applied, and stability estimates for a slightly more general problem are obtained. These are then used to prove optimal order a priori error estimates with minimal regularity assumptions on the solution.


Mathematics Subject Classification: 65M60, 65M15.
Keywords: finite element, continuous Galerkin, wave equation, stability, a priori error estimate.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

## A 2-LOCAL CHARACTERIZATION OF

$M(24)^{\prime}$

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#### Abstract

The group $M(24)^{\prime}$ has been characterized by the structure of a non 2 -central involution in [?] with a further assumption. In [?], they have assumed that the composition factors of the centralizer of a 2-central involution in $G$ are from among the known finite simple groups. In this paper we do not have this assumption and we have used of [?] to determine the structure of the centralizer of a 2 -central involution in the group $G$. Further for identifying the group $M_{24}$, they have used of [?] and here we have identified the group $M_{24}$.


Mathematics Subject Classification: 20D08.
Keywords: Finite Simple groups, Finite Groups.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# The index complex of maximal subalgebras in finite dimensional Lie algebras 

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#### Abstract

Let $M$ be a maximal subalgebra of a finite dimensional Lie algebra $L$. A subalgebra $C$ of $L$ is said to be a completion of $M$ in $L$ if $C$ is not contained in $M$ but every proper subalgebra of $C$ which is an ideal of $L$, is contained in $M$. The set $I(M)$ of all completions of $M$ is called the index complex of $M$ in $L$. This is analogous to the concept of the index complex of a maximal subgroup of a finite group, which has been studied by a number of authors. We use this concept to study the influence of the maximal subalgebras on the structure of a finite dimensional Lie algebra. In particular, we give some characterizations of solvable and supersolvable Lie algebras.


Mathematics Subject Classification: 17B05, 17B20, 17B30, 17B50.
Keywords: Lie algebras, index complex, solvable, supersovable.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A Note on the Symmetric Hit Problem 

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#### Abstract

The symmetric hit problem was introduced for the first time by the author in his thesis. The aim of this talk is to solve an important open problem posed in the thesis, in an special case, which is one of the fundamental results in the studies of the symmetric hit problem.


Mathematics Subject Classification: 55S10.
Keywords: Steenrod algebra, hit problem, symmetric hit problem.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Numerical solution to Nonlinear Diffusion Problem 

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#### Abstract

In this paper, the author considers a nonlinear diffusion problem of Gases in a Reservoir, i.e., a nonlinear diffusion equation with initial and boundary condition. A scheme for the discretization in time of that problem is proposed. The stability and the convergence of the scheme are proved.


Mathematics Subject Classification: Primary 65M06, 65M12.
Keywords: Numerical Solution - Nonlinear Diffusion Problem - Gas Reservoir - New finite difference method.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On the high rank of $\theta$-congruent number elliptic curves 

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#### Abstract

In this talk, we use the Mestre's conditional upper bound for the Mordell-Weil rank of elliptic curves to improve the authors' results on high rank $\theta$-congruent number elliptic curve over rational field for $\theta=$ $\pi / 2, \pi / 3$, and $2 \pi / 3$.


Mathematics Subject Classification: Primary 11G05; Secondary 14H52.
Keywords: $\theta$-congruent number, elliptic curve, Mordell-Weil rank.

[^137]
# Stock Option Pricing and Inverse Finance Problem 

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#### Abstract

In this paper, the inverse problem of determining the stock option pricing is discussed. For this important, we describe the general formalism and derive the exact distribution of prices and stock option. Also we discuss and solve the inverse problem in financial mathematics. Finally we will present a relatively fast algorithm for solving the inverse problem in finance which determine the volatility function and give some numerical examples.


Keywords: Financial Mathematics, Inverse finance Problem, PDE.

[^138]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference
12-15 September 2010, University of Urmia, Urmia-Iran

## A Note On Total Restrained Domaination In Graphs

M. Ali Soleimani Delarstaghi

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A New Way to Estimate the Unknown Coefficient in Parabolic PDEs of Special Structure 

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#### Abstract

Finding the capacity of heat transferring in a non-homogenous bar is a big challenge in applied sciences. Here, we study the determination of an unknown spacewise-dependent coefficient in a parabolic partial differential equation by considering the inverse problem and adding an additional initial condition.


Mathematics Subject Classification: Primary 35C05; Secondary 35Q80.
Keywords: Parabolic PDE, Fixed Point Method, Inverse Problem.

[^139]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# ON THE STABILITY OF THE QUATIC FUNCTIONAL EQUATION 

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#### Abstract

In this paper, we establish the Hyers-Ulam-rassias stability of the functional equation $f(k x+y)+f(k x-y)=k^{2}[f(x+y)+f(x-y)]+$ $2 k^{2}\left(k^{2}-1\right) f(x)-2\left(k^{2}-1\right) f(y)$, which $k \in \mathbb{N}$ is fixed. The generalized Hyers-Ulam stability originated from the Th.M.Rassias stability theorem that appeared in his paper [Th.M.Rassias, On the stability of the linear mapping in Banach spaces Proc. Amer. Soc.72(1978)297-300].


Mathematics Subject Classification: 39X82, 39X52, 39X52.
Keywords:Hyers-Ulam-rassias stability.

[^140]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference
12-15 September 2010, University of Urmia, Urmia-Iran

# NUMERICAL SOLUTION OF TWO-DIMENSIONAL INTERGRAL EQUATIONS USING HAAR WAVELETS 

S. SOHRABI, H. DERILI AND B. BARANJI ${ }^{1}$

URMIA UNIVERSITY

[^141]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Risk analysis of nonnested models under incomplete data 

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#### Abstract

We are interested in quantifying a difference of risks between two models on a particular set of information. We propose a normalization of a difference of estimators for estimating the difference of expected Kullback-Leibler risks between maximum likelihood estimators of the distribution in two different models when the data are incomplete. We wish to assess the risk incurred on a particular set of information. We constructed an interval which contains the true difference of expected Kullback-Leibler risks with a prespecified probability in situation under which the data is incomplete.


Keywords: AIC, Kullback-Leibler risk, Model selection.

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Modified multiple criteria approach to data envelopment analysis 

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#### Abstract

This paper, presents a multiple criteria data envelopment analysis (MCDEA) model which can be used to compute input and output weights with out a priori information about the weights. Here a new model proposed for computing weights with out zero value. In order to do this "Assurance region method" is used.


Keywords: Assurance Region Method (AR), Data Envelopment Analysis (DEA), Multiple Criteria (MC), Zero Weights

[^142]
# Concerning the Smith Form of Matrix Polynomials for Solution of Nonlinear Systems of Integral Equations 

N. Shayanfar ${ }^{1}$

M. Hadizadeh


#### Abstract

In this paper, a reliable method for the nonlinear mixed type system of integral equations is constructed based on the properties of matrix polynomials. Choosing the variable of the matrix polynomial, an equivalence relation between system of integral equations and matrix polynomial equation is given. Using the Smith decomposition form, leads to the final solution of the mixed system.


Mathematics Subject Classification: 15A21; 47G10; 45F05.
Keywords: Matrix polynomial, Matrix multivariable polynomial, Smith form, System of nonlinear integral equations .

[^143]
# APPROXIMATE CONNES-AMENABILTY OF DUAL BANACH ALGEBRAS 

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#### Abstract

We introduce the notions of approximate Connes - amenability and approximate strong Connes-amenability for dual Banach algebras. Then we characterize these two types of dual Banach algebras in terms of approximate normal virtual diagonals and approximate $\sigma W C$-virtual diagonals.

We show by means of an example that the class of approximately Connes ameanble Banach algebras properly contains the class of Connesameanble Banach algebras. Moreover cases where approximate Connesamenability of $\mathcal{A}^{* *}$ implies approximate Connes-amenability or approximate amenability of $\mathcal{A}$ are also discussed.


Mathematics Subject Classification: Primary 46H25, 46H20, Secondary 46 H 35 .

Keywords: Approximately inner derivation, Approximately Connes amenable, Approximately strongly Connes amenable, Approximate normal virtual diagonal, Approximate $\sigma W C$-virtual diagonal.

[^144]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

## F-Permutations Matrices

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#### Abstract

In this paper, the concept of F-permutation is introduced. Then by applying this notion, we give a presentation of an F-permutation by F-permutation matrices. We show that, there is a one-to-one corresponding between all F -permutations on $n$-letters and all F-permutation matrices.


Mathematics Subject Classification: 20N25, 08A72.
Keywords: fuzzy permutation matrices

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran 

# Golden Geometry 

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#### Abstract

A research on the properties of the Golden structure (i.e. a polynomial structure with the structure polynomial $\left.Q(X)=X^{2}-X-1\right)$ is carried out in this seminar. The geometry of the Golden structure on a manifold is investigated by using a corresponding almost product structure.


Keywords: Golden ratio, Differential manifold, Tensor field, Polynomial structure.

[^145]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Artin Exponent of Some Rational Groups 

H. Sharifi

Department of Mathematics, University of Shahed

Tehran, Iran.

# A note on the symplectic embedding of skinny ellipsoids into balls 

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#### Abstract

In this talk we investigate conditions under which we can generalize the results on symplectic embeddings of ellipsoids into balls in dimension 4 , to an arbitrary dimension.


Mathematics Subject Classification: 53C15,58Axx.
Keywords: Symplectic embedding, symplectic capacity, embedding obstruction.

[^146]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference
12-15 September 2010, University of Urmia, Urmia-Iran

# Solving fractional integro-differential equations by the haar wavelet method 

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#### Abstract

In this paper, we propose the Haar wavelet method for the numerical solution of fractional integro-differential equations of volterra type(FIDE). For this purpose, we also use collocation method and obtain a system of linear equations.


Mathematics Subject Classification: 34K37, 65T60.
Keywords: Haar wavelet, Fractional integro-differential equation, Scaling function, Collocation method

[^147]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Double centralizer on Banach spaces 

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#### Abstract

Mathematics Subject Classification: 05B35. Keywords: REal Banach space, Double centralizer, Stability, Cocircuit, Support of a vector.


[^148]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> RIF $F_{P}$ - NS preconditioner for nonsymmetric positive definite matrices 

Raheleh Shokrpour ${ }^{1}$<br>Payam Noor University, Tabriz<br>Leila Moghadam<br>Payam Noor University, Khoy Branch


#### Abstract

In this paper a new ILU factorization preconditioner for solving large linear systems by iterative methods is presented. The factorization which is based on $A$ - birothogonalization process is well defined for a general positive definite matrix. Numerical experiments illustrating the performance of the preconditioner are presented. A comparison with the well known preconditioner $R I F_{p}$ of Benzi and Tuma is also included.


Mathematics Subject Classification: 65F10.
Keywords: Implicit Preconditioner, Sparse matrices, RIF, RIF $p_{p}$

[^149]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> A second order differential equation in Banach spaces 

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#### Abstract

In this paper, our purpose is study of existence, uniqueness and maximal regularity of strict solutions of a specific second order differential equation in Banach spaces.


Mathematics Subject Classification: 34A25.
Keywords: Banach Spaces, Second order differential equations.

[^150]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A Generalization of the SOR Method 

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#### Abstract

In this paper, a generalization of the successive overrelaxation (SOR) method is presented and its convergence properties are discussed. Some numerical experiments are given to show the efficiency of the proposed method.


Mathematics Subject Classification: Primary 65F10.

Keywords: SOR, Generalized SOR, M-matrix, Convergence.

[^151]
# The infinite product representation of solutions of indefinite Sturm-Liouville problems with three turning points 

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#### Abstract

We study the infinite product representation of solutions of second order differential equation of Sturm-Liouville type on a finite interval having three turning points under the assumption that the turning points are types IV, II, III , respectively. Such representations are useful in the associated studies of inverse spectral problems for such equations.


Mathematics Subject Classification: Primary 34E20, Secondary 34E05, 34B24, 34B09.

Keywords: Turning point, Sturm-Liouville, Nondefinite problem, Infinite products, Hadamard Factorization Theorem, Spectral theory

[^152]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> ON MOUFANG HYPERIDENTITIES 

Kh. Shahbazpour<br>Department of Mathematics, Urmia University


#### Abstract

In this paper we will investigate Moufang loops and identities that define this loops. Then we will consider one of these identities and discuss hyperidentities that satisfy in variety of Moufang loops.


Mathematics Subject Classification: Primary 20N05, Secondary 05C25.
Keywords: Moufang Loops, Hyperidentities, Second Order Logic.

\author{
Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> \title{
Numerical solution of the Sturm-Liouville problem by using Chebyshev cardinal functions


#### Abstract

<br> In this paper, we want to compute the eigenvalues of Sturm-Liouville problem with the boundary conditions by using cardinal Chebyshev functions.


 <br> Mathematics Subject Classification: 34B24, 41A50. <br> Keywords: Sturm-Liouville problem, Chebyshev cardinal.}

[^153]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On submodule-based zero-divisor graph of a module over a commutative ring 

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#### Abstract

The zero-divisor graph $\Gamma(R)$ of a commutative ring with identity $R$ has been generalized from some viewpoints. One of these is the idealbased zero divisor graph $\Gamma_{I}(R)$ by replacing an arbitrary ideal $I$ of $R$ instead of the zero ideal. Also the another of them are the zero divisor graphs $\left.\Gamma_{*}(M)\right), \Gamma(M)$ and $\Gamma^{*}(M)$ of an $R$-module $M$ instead of $R$. We define the submodule-based zero-divisor graph by mixing both of them. For a submodule $N$ of an $R$-module $M$ we show that $\operatorname{diam} \Gamma_{* N}(M) \leq 3$ and $\operatorname{gr}\left(\Gamma_{* N}(M)\right) \leq 4$, if it contains a cycle.


Mathematics Subject Classification: Primary 13A99, Secondary 05C25, 13C99.

Keywords: Submodule based zero-divisor graph, diameter, girth, cutpoint

[^154]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Solving a Class of Nonlinear Optimal Control Problems via A Modified Variational Iteration Method 

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## Sohrab Effati


#### Abstract

This paper presents an analytical approximate solution for nonlinear quadratic Optimal Control Problems (OCP's). The proposed method consists of a modified Variational Iteration Method (VIM), for solving the extreme conditions obtained from the OCP. An illustrative example is given to demonstrate the simplicity and efficiency of the proposed method.


Mathematics Subject Classification: 49M05
Keywords: Optimal control problem, Variational iteration method, Shooting method

[^155]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# The Homotopy Analysis Method for Solving Variational problems 

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#### Abstract

In this paper, homotopy analysis method ( $H A M$ ) will be employed for solving some problems in calculus of variations. Numerical results reveal that HAM is very effective and simple for obtaining approximate solutions to variational problems.


Keywords: Homotopy analysis method, Calculus of variation, Variational problems, Euler-lagrange equation

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On Structure of H-Spaces 

## H.R.Sahebi

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#### Abstract

A pair $(X, A)$ of a topological space $X$ and a topological $\operatorname{ring} A$ is called an H-space, if for each closed subset $F$ of $X$ and $x \notin F$, there exists $f \in C_{A}(X)$ such that $f(x) \neq o_{A}$ and $F \subseteq Z(f)$ and a topological space $X$ is called a $V$-space, [4], if for points $a, b, c$, and $d$ of $X$, where $a \neq b$, there exists a continuous functions $f$ of $X$ into itself such that $f(a)=c$ and $f(b)=d$. In this paper we investigate some properties of H -spaces. In addition to, we show that every H -space is not a V-space.


Mathematics Subject Classification: 54C10.
Keywords: H-space, V-space, Hausdroff space.

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Results of generalized local cohomology modules of $\mathfrak{a}$-minimax modules 

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#### Abstract

Let $R$ be a commutative Noetherian ring, $M$ a finitely generated $R$-module, and $N$ a minimax $R$-module. It is shown that if $\mathfrak{a}$ is an ideal of $R$ such that the cohomological dimension $\operatorname{cd}(\mathfrak{a})=1$, then $H_{\mathfrak{a}}^{j}(M, N)$ and $\operatorname{Ext}_{R}^{i}\left(M, H_{\mathfrak{a}}^{j}(N)\right)$ are $\mathfrak{a}$-cominimax for all $i, j$. Furthermore, if $t$ is a non-negative integer such that $H_{\mathfrak{a}}^{j}(M, N)$ is $\mathfrak{a}$-minimax for all $j<t$, then for any $\mathfrak{a}$-minimax $R$-submodule $L$ of $H_{\mathfrak{a}}^{t}(M, N)$, the $R$-module $\operatorname{Hom}_{R}\left(R / \mathfrak{a}, H_{\mathfrak{a}}^{t}(M, N) / L\right)$ is $\mathfrak{a}$-minimax. As a consequence, it follows that the Goldie dimension of $H_{\mathfrak{a}}^{t}(M, N) / L$ is finite, and so the associated primes of $H_{\mathfrak{a}}^{t}(M, N) / L$ is finite


Mathematics Subject Classification: 13D45, 13E99.
Keywords: Generalized local cohomology module, minimax module.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A representation of selfadjoint module maps 

K. Sharifi ${ }^{1}$


#### Abstract

We will find a representation of selfadjoint $\mathrm{C}^{*}$-linear module maps into positive, negative and zero parts via the operators which are appear in the polar decomposition of them. This enables us to study those orthogonal submodules which are reduced by selfadjoint C*-linear module maps.


Mathematics Subject Classification: 46L08, 47A05, 47L60, 46C05
Keywords: Hilbert C*-modules, unbounded operators, polar decomposition, $\mathrm{C}^{*}$-algebras of compact operators.

[^156]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# About Edge-Tenacity of a Graph 

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#### Abstract

In this paper we introduce a new invariant edge-tenacity, for graphs. it is another vulnerability measure. we present several properties and bounds on the edge-tenacity. we also compute the edge-tenacity of some classes of graphs.


Mathematics Subject Classification: 05C45, 90B10, 68R10.
Keywords: cut set ,tenacity, network vulnerability.

[^157]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Quadrature formulae of Gauss type based on Euler identities compare with Legendre 

Sara Saboori<br>Islamic Azad University, Lahijan Branch, Lahijan, Iran.


#### Abstract

The aim of this paper is to derive quadrature formulae of Gauss type based on Euler identities and compare between the Gauss 2-point formula obtained by Euler identities and Legendre 2-point formulae.


Mathematics Subject Classification: 41A55, 41X00.
Keywords: Quadrature formulae, Euler identities, Gauss type.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Numerical solution of Schrödinger equation by using modified variational iteration and homotopy analysis methods 

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#### Abstract

In this paper, a Schrödinger equation is solved by using the variational iteration method (VIM), modified variational iteration method (MVIM) and homotopy analysis method (HAM). The approximate solution of this equation is calculated in the form of series which its components are computed by applying a recursive relation. The existence and uniqueness of the solution and the convergence of the proposed methods are proved. A numerical example is studied to demonstrate the accuracy of the presented methods.


Mathematics Subject Classification: Primary 00X00, Secondary 00X00, 00X00.

Keywords: Schrödinger equation, Variational iteration method, Modified variational iteration method, Homotopy analysis method.

[^158]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Groups with marginal automorphisms as elementary abelian groups 

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#### Abstract

Let $W$ be a non-empty subset of a free group. The automorphism $\alpha$ of a group $G$ is said to be a marginal automorphism, if for all $x \in G$, $x^{-1} \alpha(x) \in W^{*}(G)$, where $W^{*}(G)$ is the marginal subgroup of $G$.

In this paper, we give necessary and sufficient condition for a purely non-abelian $p$-group $G$, such that the set of all marginal automorphisms of $G$, form an elementary abelian $p$-group.


Mathematics Subject Classification: 20D45, 20F28, 20E05, 20 E36.
Keywords: Elementary abelian $p$-group, marginal automorphism, marginal subgroup, purely non-abelian group, verbal subgroup.

[^159]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Approximate solution for the KGS equation By RBF in a finite-Difference mode 

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A. Safdari-Vaighani ${ }^{1}$


#### Abstract

In this paper, we present an numerical method for approximate solution of the coupled Klein-Gordon-Schrodinger equations using radial basis functions. For this aim, we apply an alternative RBF based formulation which generate a local interpolant using scattered data RBF interpolant method. In this method, function derivatives are approximated as a linear combination of the function values.


Mathematics Subject Classification: 41A21, 41A30, 41A63.
Keywords: Klein-Gordon-Schrödinger equation, Radial basis functions, Finite difference method.

[^160]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# ON LEFT DERIVATIONS OF TRIANGULAR MATRIX RINGS 

## M. NADER GHOSSEIRI

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#### Abstract

Let $R, S$ be rings with identity and $M$ be an $(R, S)$ - bimodule. In this paper we determine the structure of left derivations and Jordan left derivations of the triangular matrix ring $T=\left(\begin{array}{cc}\mathrm{R} & \mathrm{M} \\ 0 & \mathrm{~S}\end{array}\right)$.

Mathematics Subject Classification: 16W25, 16N60, 16 U 80. Keywords: Left derivation, Jordan left derivation, triangular matrix ring.


[^161]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A relation between preorderability and orderability of topological spaces and some it's results 

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#### Abstract

In this paper we studies the quotient maps that their domains are the preorder topologic spaces and we obtain some results in this concepts.


Mathematics Subject Classification: 54F05, 06 A05.
Keywords: Totally preordered sets, Topological spaces, Order and preorder topology, Quotient spaces.

[^162]
# PRESERVING POWER GEOMETRIC MEAN TO PRESERVING RANK ONE OPERATORS ON B(H) + 

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#### Abstract

Let $\varphi$ is a unital bijective mapping on $B(H)_{+}$that preserve the power geometric mean for some $\alpha$, $(0<\alpha<1)$, then we conclude that $\varphi$ preserves rank-one projections bidirectionally.


Keywords: Power geometric mean, rank one operator.

[^163]
# On the positive and negative solutions of $p$-Laplacian BVP with Neumann boundary conditions 

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## J.Mohammadpour

## M.Zameni ${ }^{1}$


#### Abstract

In this paper, we consider the following Neumann boundary value problem $$
\left\{\begin{array}{l} -\left(\varphi_{p}\left(u^{\prime}(x)\right)\right)^{\prime}=u(x)|u(x)|^{p}-\lambda|u(x)|^{q}, \quad x \in(0,1), \\ u^{\prime}(0)=0=u^{\prime}(1), \end{array}\right.
$$ where $\lambda \in \mathbb{R}, p$ and $q$ are parameters such that $p \in(1, \infty), q \in(0, \infty)$ and $p>q$. We study the positive and negative solutions of this problem, by using a quadrature method, we obtain our results.


Mathematics Subject Classification: 34B15, 34B18.
Keywords: Positive and negative solutions, Interior critical points.

[^164]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Some Results on the N-Ary Algebraic Hyperstructures <br> M. Taheri, A. Shahsavan 

Yasooj University, Yasooj, Iran.
Mathematics Subject Classification:08A05, 20N15, 20N20.
Keywords: Hyper structures, hyper group, multi algebra, Fundamental algebra

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Enveloping actions of partial actions on $C^{*}$-algebras 

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#### Abstract

Let $G$ be a countable discrete group and $\alpha$ be a partial action of $G$ on a locally compact space. We describe the enveloping action and the enveloping space of $\alpha$. Also, if $\alpha$ is an action of $G$ on a $C^{*}$-algebra, we will introduce its enveloping action and its enveloping $C^{*}$-algebra, if exist.


Mathematics Subject Classification: 46L05.
Keywords: Action of groups, $C^{*}$-algebras, homeomorphisms.

[^165]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> chain conditions on a class of submodules 

Yahya Talebi<br>Behnam Talaee ${ }^{1}$<br>Department of Mathematics, Faculty of Basic Sciences, University of Mazandaran, Babolsar, Iran


#### Abstract

Let $R$ be a ring and $M$ a right $R$-module. Here we show that $M$ satisfies acc on F-small submodules iff $\operatorname{Rad}(M)$ is noetherian. It is also shown that if $M$ satisfies acc on F -small submodules, then $M$ has property $P^{*}$ iff $M$ is F-lifting.


Mathematics Subject Classification: Primary 16D70, Secondary 16D80, 16D90.

Keywords: F-small submodule, F-supplement submodule, F-lifting module.

[^166]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Using radial basic functions for solving integral equations by meshless-type method 

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#### Abstract

In this paper, we develop a new method using radial basic function (RBF)is presented for solving integral equation of Fredholm and Volterra types. The idea is to first produce a uniform mesh in a three dimensional domain and then equi-distribute the mesh in the three coordinate direction. The generated mesh points are suitable for meshlesstype methods which only need some scattered points rather than a mesh with smoothness properties.


Mathematics Subject Classification: 65R20, 11Y05, 05A19.
Keywords: Radial basic function, Integral equation, Adaptive mesh, Equidistribution, collocation meshless method.

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Approximation of the Inverse Continuous Frame Operator 

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#### Abstract

A discrete frame in a separable Hilbert space $\mathcal{H}$ allows every element in $\mathcal{H}$ can be written as a infinite linear combination of the frame elements, with coefficients called frame coefficients. Peter G. Casazza and Ole Christensen introduced some methods to approximate frame coefficients. In this article, we investigate some of these results for a continuous frame. As a consequence, approximation of the solution to a moment problem is also discussed.


Mathematics Subject Classification: 42C15, 41A35.
Keywords: Frames, continuous frame, operator frame.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Fuzzy Coprimary Submodules 

## J. A'zami ${ }^{1}$

## N. Zamani


#### Abstract

Let $R$ be a commutative ring with non-zero identity and $M$ a nonzero unitary $R$-module. This paper deals with the concept of fuzzy coprimary submodules. We define this notion and study some of its basic results. The behavior of this concept with fuzzy localization will be studied.


Mathematics Subject Classification: 08A72.
Keywords: fuzzy coprimary submodules, fuzzy attached primes, fuzzy prime and primary ideals and submodules.

[^167]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> $\mathrm{C}^{1}$-PERSISTENTLY SENSITIVE HOMOCLINIC CLASSES 

A. FAkhari<br>School of Mathematics and Computer Science, Damghan<br>University, Damghan, Iran.

## S. Ashoori

H. Gharib

## S. Jalalipoo ${ }^{1}$


#### Abstract

Let $f$ be a diffeomorphism of a closed $n$-dimensional $C^{\infty}$ manifold, and $p$ be a hyperbolic saddle periodic point of $f$. In this paper, we introduce the notion of $C^{1}$-persistently sensitive for a closed $f$-invariant set. We prove that for the homoclinic class $H_{f}(p)$ of $f$, if $f_{\mid H_{f}(p)}$ is $C^{1}$-persistently sensitive then $H_{f}(p)$ admits a dominated splitting. Especially, on a 3-dimensional manifold, the splitting on $H_{f}(p)$ is partially hyperbolic, and if in addition, $f$ is far from homoclinic tangency, then $H_{f}(p)$ is strongly partially hyperbolic.


Mathematics Subject Classification: 37B20, 37C29, 37C50.
Keywords: Persistently sensitive, Homoclinic class, Dominated splitting, Partially hyperbolic, Strongly partially hyperbolic.

[^168]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> On Saturation of submodules of Multiplication Modules 

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#### Abstract

Let $R$ be a commutative ring and $M$ be a unitary $R$-module. For a prime ideal $p$ of $R$ and submodule $N$ of $M$, the submodule $\{m \in$ $M: r m \in N$ for some $r \in R-p\}$ of $M$, denoted $S_{p}(N)$, is called the saturation of submodule $N$. In this work we study the saturation of certain submodules $I N$ (specially $p M$ ) related to an ideal $I$ (specially prime ideal $p$ ) of $R$ and submodule $N$ of $M$. It is shown that for an ideal $I$ of $R$ and finitely generated multiplication $R$-module $M, S_{p}(I M)=$ $S_{p}(I) M$. Using this we obtain the reduced and module-reduced primary decomposition of $I M$ of a reduced primary decomposition of $I$.


Mathematics Subject Classification: 13A99; 05C25; 13C99
Keywords: Saturation, Radical of a submodule, Prime submodule, Prime specteum

[^169]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On the Completeness, and basis property of the function system cosin in the space sobolev $\left(W_{p}^{1}(0, \pi)\right)$ 

N.Abbasi ${ }^{1}$<br>Department of Mathematics, Lorestan University, P. O. Box 465, Korammabad, Iran.

## M.Ghasemi


#### Abstract

In the present paper, we proved that the completeness,and basis property of the function system cosine in the space sobolev.


Mathematics Subject Classification: 35j70
Keywords: Inequality.Frankl problem,Bessel equation,Fubini theorem,Lebesgue integral,spase sobolev.

[^170]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran 

## Regularity of elements for

$$
T_{E^{*}}(X)
$$

M. Abbasi<br>Department of Mathematics, Azad University, Zahedan, Iran.


#### Abstract

Let $T_{X}$ be the full transformation semigroup on a set $X$. For a non trivial equivalence $E$ on $X$, let $T_{E}(X)=\left\{f \in T_{X}: \forall a, b \in X,(a, b) \in\right.$ $E \Rightarrow(f(a), f(b)) \in E\}$, and $T_{E^{*}}(X)=\left\{f \in T_{X}: \forall a, b \in X,(a, b) \in\right.$ $E \Leftrightarrow(f(a), f(b)) \in E\}$. In this paper, we discuss regularity of elements for these semigroups.


Mathematics Subject Classification: 20M20.
Keywords: Semigroup, Transformation, Equivalence, Regular element.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Operator valued $p$-frames 

Mohammad Reza Abdollahpour<br>Department of Mathematics, Faculty of Sciences, University of Mohaghegh Ardabili, Ardabil, Iran.


#### Abstract

In this paper we introduce the concept of operator valued $p$-frames and we give a characterization of operator valued $p$-frames. Also we show that if a Banach space $X$ can be equipped with an operator valued $p$-frame then each member of $X^{*}$ will be represented by an unconditionally convergent series.


Mathematics Subject Classification: Primary 41A58, Secondary 42C15.
Keywords: p-frame, operator valued p-Bessel sequence, operator valued p-frame.

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> A Note on the Schur multiplier of Lie algebras 

B. Edalatzadeh<br>Department of Mathematics, Faculty of science, Razi<br>University, Kermanshah


#### Abstract

In this article, we remind the concepts of homology, cohomolgy and the Schur multiplier of a Lie algebra. Using homological methods, a relation between homology and cohomology of a Lie algebra is given. Also, we obtain some inequalities and certain bounds for the dimension of $\mathcal{M}(L)$.


Mathematics Subject Classification: 17B30, 17B60, 17B99.
Keywords: Lie algebra, homology and cohomology, Schur multiplier.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Using Adomain's Decoposition Method For Solving Newell-Whithead Equation 

R. Ezati and K. Shakibi<br>Department of Mathematics,<br>Islamic Azad University, Karaj Branch,<br>Karaj, Iran.

# answering some old questions about nontrivial minimal blocking set by covering groups. 

Mohammad Javad Ataei<br>Department of Mathematics, second University, P. O. Box 22222, City, Country.


#### Abstract

In this paper we introduce application of covering groups by subgroups for answering some old questions about nontrivial minimal blocking set and we give nontrivial minimal blocking sets in $P G(3,3)$ of sizes 7 and 8 ; and in $P G(4,3)$ of size 9 . Non-existence of a minimal blocking set of size 27 is still open.


Mathematics Subject Classification: 51E21, 20D60.
Keywords: Blocking sets; projective spaces, maximal irredundant cover for groups, covering groups by subgroups

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On The Shannon Wavelets Approximation For The Volterra Integro Differential 

K. Malknejad and M. Attary<br>Department of Mathematics,<br>Islamic Azad University, Karaj Branch,<br>Karaj, Iran.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Pseudometric on $B C K$-algebras 

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#### Abstract

In this note we defined a pseudometric on $B C K$-algebras. We use this meter for defining neighborhoods, open and closed sets and hausdorff sets in $B C K$-algebras and prove theorems and we define the ralation between them.


Mathematics Subject Classification: 06F35, 03G25, 08A05.
Keywords: BCK-algebras, BCK-class, NBCK-class, Pseudometric.

[^171]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference
12-15 September 2010, University of Urmia, Urmia-Iran

# APPROXIMATE GENERALIZED JORDAN DERIVATIONS ON BANACH MODULES 

SAED OSTADBASHI

ROGAYEH ALAVI ${ }^{1}$

[^172]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran 

# Hyperspace and Powerdomain 

M. Ali-Akbari ${ }^{1}$<br>Department of Mathematics, Semnan University, P. O. Box 35195-363, Semnan, Iran.<br>M. Pourmahdian<br>School of Mathematics and Computer Science


#### Abstract

We consider a powerdomain of the space of formal balls $\mathbf{B} X$ for a quasi-metric space ( $X, d$ ), denoted by $\mathbf{C B} X$, as the chain completion of the set of all finite subsets of $\mathbf{B} X$ with respect to the Egli-Milner relation and prove that there is an embedding map between $\mathcal{K}_{0}(X)$ with Vietoris topology and CB $X$ with Scott topology.


Mathematics Subject Classification: 54B20.
Keywords: Formall ball, Hyperspaces, Powerdomain, Vietoris topology.

[^173]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Triangular functions method for the solution of population balance differential equation 

Amjad Alipanah<br>University Of Kurdistan, Sanandaj, P. O. Box: 416, Iran.


#### Abstract

In this paper, triangular orthogonal functions (TF) method is applied as a basis in collocation method, to solve the population balance equation, which arise in the description of particle-size distribution of a continuous, mixed-suspension, mixed product removal crystallizer with taking account of the effect of particle breakage. To demonstrate the validity of this method obtained results have been compared with other methods.


Mathematics Subject Classification: Primary 65Z05, Secondary 65M70, 41A30.

Keywords: Triangular orthogonal functions, Population balance equation, Collocation method.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Inverse Minimax Location Optimization with augmentation of Arc Lengths 

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#### Abstract

In this investigation, we consider the inverse absolute and vertex minimax location problems with arc length augmentation on a tree network $T$ with $n+1$ vertices. The aim is to increase the arc lengths in the cheapest possible way such that a prespecified vertex of $T$ becomes an absolute (or a vertex) minimax location under the modified lengths. We develop an $\mathcal{O}(n \log n)$-time optimal algorithm for this problem. Moreover, an $\mathcal{O}(n \log n)$-time algorithm is proposed for the cardinality constrained variant of the inverse minimax location problem with equal cost coefficients.


Mathematics Subject Classification: 90C27, 90B80, 90 B 85.
Keywords: Mminimax location optimization, Inverse optimization, Knapsack models.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Symbols of Fourier Integral Operators 

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# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> COMPACT ENDOMORPHISMS OF $\operatorname{Lip}_{A}(\overline{\mathbb{D}}, K, \alpha)$ 

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#### Abstract

Let $\Omega$ be a domain in complex plane such that $\Omega \subseteq \mathbb{D}$ and let $K=\bar{\Omega}$, where $\mathbb{D}$ is the open unit disk $\{z \in \mathbb{C}:|z|<1\}$. We take $A(\overline{\mathbb{D}}, K)=\left\{f \in C(\overline{\mathbb{D}}):\left.f\right|_{K} \in A(K)\right\}$, where $A(K)$ is the algebra of continuous complex-valued functions on $K$ which are analytic on $\operatorname{int}(K)$. It is known that $A(\overline{\mathbb{D}}, K)$ is a natural uniform algebra on $\overline{\mathbb{D}}$. In this note we study endomorphisms of certain natural uniform subalgebras of $A(\overline{\mathbb{D}}, K)$ and investigate necessary and sufficient conditions for which these endomorphisms to be compact.


Mathematics Subject Classification: Primary 46J10, Secondary 46J15.
Keywords: Analytic functions, Banach function algebras, Compact endomorphisms.

[^174]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> The Annihilating-Product-One Side-Ideal graph 

F. Ali Niaei Fard ${ }^{1}$<br>epartment of Mathematics, Isfahan university of technology, P. O. Box 84156-83111, Isfahan, Iran.


#### Abstract

For a commutative ring R with identity, the annihilating-ideal graph of $R$, denoted $A G(R)$, is the graph whose vertices are the nonzero annihilating ideal of R with two distinct vertices joined by an edge when the product of the vertices is zero. This article extend the definition of the annihilating ideal graph to non-commutative rings.


Mathematics Subject Classification: primary 16U99, Secondary 05C50, 16S50

Keywords: The Annihilating-ideal graph, The Annihilating-Product-One side-Ideal graph.

[^175]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Computing Minimal Polynomial of Matrices by Grobner Bases 

Amir Hashemi, Benyamin M. Alizadeh

Isfahan University of Technology,
Isfahan, Iran.

# Radial basis Functions for solving of nonlinear integral equation illustrating thermal radiation in a kerr blackbody 

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M. Eatesami
G. B. Loghmani


#### Abstract

Solution of nonlinear integral equation are often cost and difficult. There are many methods for solving these equations. We introduce radial basis functions(RBFs) as a tool of approximation that can be used for constructing solution of integral equation [?]. Here, RBFs are applied for solving of nonlinear integral equation illustrating thermal radiation in a kerr blackbody.


Mathematics Subject Classification: 45Gxx, 33F05, 97N40.
Keywords: Integral equation, Radial Basis Functions, Modeling.

[^176]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Nonlinear Regression via Radial Basis Functions on Dentistry Data 

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## Zakieh Avazzadeh

M.T. Shakeri

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#### Abstract

Nonlinear regression models often have complex structure [?]. There are many methods for constructing these models. We introduce radial basis functions(RBFs) as a tool of approximation that can be used for finding curve through a series of data. In fact, unknown parameters adjust the amount of overlapping basis functions and adopts the information of the input and response variables. We use real dentistry data that can not be fitted on linear regression.


Mathematics Subject Classification: 62J02, 33F05, 65Fxx, 93 E 24.
Keywords: Nonlinear Regression, Radial Basis Functions, optimization, least square method.

[^177]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On Sezabo operator in Lorentzian manifolds 

S. Aimpour ${ }^{1}$

## A. Haji Badali

## M. Toomanian


#### Abstract

In this paper, we classify Sezabo operator related to Ricci operator of three-dimensional Lorentzian manifold. Also we construct the necessary and sufficient condition for function $f(t, x, y)$ of the Walker metric of three-dimensional manifolds, to have, zero Sezabo operator.


Mathematics Subject Classification: Primary 53C30, Secondary 53C50, 53C80.

Keywords: Lorentzian manifolds, Walker manifolds, Curvature tensor, Sezabo operator.

[^178]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference
12-15 September 2010, University of Urmia, Urmia-Iran

# On Iterative Formulae for Computing The Inverse of A Square Matrix 

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#### Abstract

In this paper, a new family of iterative formulae of order $k$ for $k \geq 2$ is presented that computes the inverse of a nonsingular matrix $A$.


Mathematics Subject Classification: 15A09, 65F10, 11D04.
Keywords: Matrix inversion, Iterative methods, Linear equations.

[^179]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Analytic solution of nonlinear partial differential equations by tanh-coth method 

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A. Ghafury ${ }^{1}$

Department of Mathematics, Yazd University, P. O. Box: 89195-741, Yazd, Iran.


#### Abstract

Nonlinear partial differential equations in mathematical physics play a majer role in various fields. In this work we derive travelling wave solutions for the Burger's equation. The tanh-coth method is used to determine these sets of travelling wave solutions. We also answer to this question that "Does this method derives all sets of soluations?".


Mathematics Subject Classification: Primary 65M99, Secondary 65N99.

Keywords: The tanh-coth method,Wave variable, Nonlinear partial differential equations .

[^180]
# Iterated Importance Sampling Algorithm for Estimating the Order of Autoregressive Process in the Poisson Stochastic Volatility Models 

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#### Abstract

Importance sampling methods can be iterated like MCMC algorithms, while being more robust against dependence and starting values as shown in Cappé et al. (2005). In this work we use this algorithm to estimate the order of autoregressive process which is dynamic part of the models called Poisson Stochastic Volatility models.


Mathematics Subject Classification: Primary 62F40; Secondary 63F15.
Keywords: Adaptive algorithms, Population Monte Carlo, Dynamic Generalized Linear Models; Poisson Regression; Poisson Stochastic Volatility;

[^181]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference
12-15 September 2010, University of Urmia, Urmia-Iran

# Discrete Gabor transform on finite non-abelian groups 

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#### Abstract

Let $G$ be finite non-abelian group and $\ell(G)$ be the set of all complex valued functions on $G$. We define Gabor transform of $f \in \ell(G)$ with respect to a window function $g \in \ell(G)$ and we study basic properties of this transform. Also, we find a matrix interpretation for this transform.


Mathematics Subject Classification: 43A30, 43A32.
Keywords: Discrete Gabor transform, Fourier transform, Plancherel formula, unitary representation, irreducible representation.

[^182]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Multistep Collocation methods for nonlinear two dimensional Volterra integral equation 

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## S. Shahmorad


#### Abstract

In this paper, we construct multistep collocation methods for nonlinear two dimensional Volterra integral equation. These methods depend on the numerical solution in a fixed number of previous time and spatial steps. We analyze the order of resulting methods and show the efficiency of the method by some numerical examples.


Mathematics Subject Classification: 65R20.
Keywords: Multistep collocation methods, Two dimensional Volterra integral equation.

[^183]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Laplace transform-Adomian decomposition for Volterra's Population model ${ }^{1}$ 

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J. Fadaei ${ }^{1}$<br>Mathematics Department, Shahd Bahonar University of Kerman, kerman, IRAN.


#### Abstract

In this paper, a combined form of the Laplace transform method with the Adomian decomposition method is developed for analytic treatment of the Volterra's model for population growth of a species within a closed system. This model is a nonlinear integro-differential equation where the integral term represents the effect of toxin.


Mathematics Subject Classification: 45A05, 45B05, 45D05, 45J05, 47G20.

Keywords: Laplace transform-Adomian decomposition method, Volterras population model, Padé approximants.

[^184]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On 3-Rewritable Groups 

## A. Faramarzi Salles and C. Sica

Department of Mathematics, Damghan University, Damghan, Iran.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference

12-15 September 2010, University of Urmia, Urmia-Iran

## ON THE QUASIMONOTONE AND MONOTONE MAPS

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Numerical algorithm for solving linear systems using iterative refinement Monte Carlo method 

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M. Aalaei


#### Abstract

In this paper, a numerical algorithm involving the combined use of iterative refinement method and Monte Carlo method is proposed for solving linear systems. A numerical test is performed in order to show the efficiency and accuracy of the present work.


Mathematics Subject Classification: 65C05, 65 N 22.
Keywords: Iterative refinement method, Monte Carlo method, Linear systems.

[^185]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Best Uniform Polynomial Approximation For a Class Of Rational Function 

M. A. Fariborz Argahi and F. Froozanfar<br>Department of Mathematics, Islamic Azad university, Kermanshah Branch, Kermanshah, Iran.

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Certain Subclasses of convex Functions with Positive and Missing Coeffecient by using a Fixed Point 

## A. Ebadian

Z. Farhad Tuski ${ }^{1}$
H. Soleimani

Urmia University, Urmia, Iran
Islamic azad University, Malayer

Keywords: P-valent function, Coefficient estimate, Distortion dound, Fixed point.

[^186]
# The use of homotopy analysis method to approximate the solution of Schrödinger equation 

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Sh. Sadigh Behzadi

Young Researchers Club, Islamic Azad University, Central
Tehran Branch, Tehran, Iran.


#### Abstract

The Schrödinger equation is a typical partial differential equation that plays an important role in different areas of chemistry and mathematical physics. In this work, we apply the homotopy analysis method (HAM) to approximate the solution of the Schrödinger equation and compare the results with the modified variational iteration method (MVIM).


Mathematics Subject Classification: Primary 65M99, Secondary 35QX55.
Keywords: Schrödinger equation, Homotopy analysis method, Modified variational iteration method,

[^187]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# New strategy for approximating the p.d.f. of stable distributions 

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## S. M. Hashemiparast


#### Abstract

In this short note, first basic concepts of stable distributions are introduced. Also, the fractional calculus as a means of stable distributions are expressed. Two specific fractional partial differential equations, which their fundamental solutions are probability density function of stable distributions are introduced. Finally, the methods to solve these fractional partial differential equations are applied.


Mathematics Subject Classification: 60Exx, 60Gxx, 62JXX. Keywords: Stable Distributions, Fractional Calculus.

[^188]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A Numerical Method For Solution The Burger's-Fisher Equation 

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#### Abstract

In this paper, we propose a numerical scheme to solve the Burger'sFisher equation. Our scheme uses the collocation points and approximates the solution using Thin Plate Splines (TPS) radial basis functions (RBF). The implementation of the method is simple as well as finite difference methods. The results of numerical experiments are presented, and are compared with analytical solutions to confirm the good accuracy of the prossed scheme.


Mathematics Subject Classification: 65M99, 65N99.
Keywords:Radial basis functions, Burger's-Fisher equation, Collocation method.

[^189]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# The incidence chromatic number of some graphs of maximum degree 4 

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#### Abstract

In this paper we investigate the incidence coloring conjecture (ICC) for graphs of maximum degree 4 and prove that ICC holds for some classes of such graphs.


Mathematics Subject Classification: 05C15.
Keywords: Incidence coloring, Incidence chromatic number.

[^190]
# Estimation of the shape parameter of the generalized Pareto distribution under loss functions Convergent Iterative Scheme 

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S. Nezamdoust


#### Abstract

In this paper Bayes estimators of the shape parameter of the generalized Pareto distribution is obtained by taking a given prior distributions using the squared error loss, squared log error loss, precautionary and entropy loss functions. Monte Carlo simulations are presented to compare the Bayesian estimation and the maximum likelihood estimation of the unknown parameter.


Keywords: Generalized Pareto distribution, Bayesian estimation, Loss function, Maximum likelihood estimate.

[^191]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Cubic symmetric graphs of order $8 p^{3}$ 

Mohsen Ghasemi<br>Department of Mathematics, Urmia University


#### Abstract

An automorphism group of a graph is said to be $s$-regular if it acts regularly on the set of $s$-arcs in the graph. A graph is $s$-regular if its full automorphism group is $s$-regular. In this paper all $s$-regular cubic graphs of order $8 p^{3}$ are classified for each $s \geq 1$ and each prime $p$.


Mathematics Subject Classification: 05C10, 05C25, 20 B 25.
Keywords: symmetric graphs, s-regular graphs, regular coverings.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Solving systems of linear equations whose coefficient matrices are low rank perturbations of cymmetric matrices 

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Barani

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#### Abstract

MINRES-CN is an iterative method for solving systems of linear equations with conjugate-normal coefficient matrices whose conspectra are located on algebraic curves of a low degree. This method was proposed in a previous publication of author and KH. D. Ikramov. In this paper, the range of applicability of MINRES-CN is extended in new direction. These are conjugate-normal matrices that are low rank perturbations of Symmetric matrices.


Mathematics Subject Classification: 65F10.
Keywords: conjugate-normal matrices, MINRES-CN method, conspectrum.

[^192]
# A common Fixed Point Theorems in Menger Spaces with using property (E.A) 

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## S. Ghayekhloo ${ }^{1}$

> M.Sc. Student of Mathematics and member of young Researchers club, Islamic Azad University- Ghaemshahr Branch.


#### Abstract

The main purpose of this paper is to define Menger probabilistic metric space and the nation of weakly compatible and define a new propert and prove a common fixed point theorem for four self maps in menger space with using the notion of property (E.A).


Keywords: Triangle function (t-norm), Menger space, Fixed point theorem, Weak compatibility, property (E.A).

[^193]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Almost double derivations on $J B^{*}$-triples 

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#### Abstract

In this paper, we obtain the general solution for a following new functional equation $$
\begin{equation*} \sum_{i=1}^{m} f\left(m x_{i}+\sum_{j=1, j \neq i}^{m} x_{j}\right)+f\left(\sum_{i=1}^{m} x_{i}\right)=2 m \sum_{i=1}^{m} f\left(x_{i}\right) \tag{0.1} \end{equation*}
$$ for a fixed positive integer $m$ with $m \geq 2$. Moreover, we introduce the concept of double derivations and Jordan double derivations on $J B^{*}$ - triples and investigate the generalized Hyers - Ulam - Rassias stability of double derivations on $J B^{*}$ - triples associated with functional equation (0.1).


Mathematics Subject Classification: 39B52, 39B82.
Keywords: Hyers - Ulam - Rassias stability, $J B^{*}$ - triples, double derivation, Jordan double derivation.

[^194]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Explicit solution of certain classes of differential equations by means of fractional calculus 

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#### Abstract

By means of fractional calculus techniques, we find explicit solutions of a number of linear ordinary and partial differential equations of the second and higher orders. We use the N -fractional calculus operator method to derive the solutions of these equations.


Mathematics Subject Classification: 26A33, 34A08, 34K37.
Keywords: Fractional calculus, Differintegral equations, Homogeneous and nonhomogeneous equations, Analytic functions.

[^195]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Modal Operators on Pseudo Hoops 

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#### Abstract

In this paper, we introduce the notion of modal operators (special cases of closure operators) on a pseudo hoop and obtain some related results. In particular, we show that each modal operator $\gamma$ on a pseudo hoop induce a normal filter and there exists an isomorphism between the quotient algebra induced by this normal filter and the set of all fix points of $\gamma$.


Mathematics Subject Classification: 06F99, 08A30, 94D05. Keywords: Pseudo hoop, Modal operator, Normal filter, Congruence.

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> INTERPOLATION OF QUASI-BANACH SPACES 

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#### Abstract

let $\left(A_{0}, A_{1}\right)$ be a compatible couple of quasi-Banach spaces in the interpolation theory sense. Some theorems about real interpolation of quasi-Banach space readjusted. We give a maximal description in the sense of Aronszajn-Gagliardo for the real methods in the case of quasiBanach quaternion.


Mathematics Subject Classification: 46B70, 46M35.
Keywords: interpolation space.

[^196]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Special Representations of the Parabolic subgroubs of simple triality groups $3 D_{4}\left(2^{n}\right)$. 

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#### Abstract

A square matrix over the complex field with non-negative integral trace is called a quasi-permutation matrix. Thus every permutation matrix over $C$ is a quasi-permutation matrix. The minimal degree of a faithful representation of $G$ by quasi-permutation matrices over the complex numbers is denoted by $c(G)$ and $r(G)$ denotes the minimal degree of a faithful rational valued complex character of $G$. The purpose of this paper is to calculate above quantities for the maximal parabolic subgroups of simple triality groups ${ }^{3} D_{4}\left(2^{n}\right)$.


Mathematics Subject Classification: 20C15.
Keywords: Chevalley group ,Character table,Shur index, Quasi-permutation representation.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On normal matrices that commute with their complex conjugate 

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#### Abstract

We consider the class of normal complex matrices that commute with their complex conjugate. We show that such matrices are real orthogonally similar to a canonical direct sum of 1-by-1 and certain 2-by-2 matrices. A canonical form for quasi-real normal matrices is obtained as a special case. We also exhibit a special form of the spectral theorem for normal matrices that commute with their conjugate.


Mathematics Subject Classification: 15A21; 15A57.
Keywords: Canonical form, Real normal matrix, Quasi-real normal matrix, Real orthogonal similarity, Unitary similarity.

[^197]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# reconstruction of a jacobi matrix from mixed eigendata 

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#### Abstract

In this paper we consider the construction of a $n \times n$ jacobi matrix J of the form $$
J=\left(\begin{array}{cc} J_{1} & b_{k} e_{k} e_{1}^{T} \\ b_{k} e_{k}^{T} e_{1} & J_{2} \end{array}\right)
$$ from mixed eigendata $\lambda_{1}, \mu_{1}, \mu_{2} \in \Re, X=\left(x_{1}, x_{2}, \ldots, x_{n}\right) \in \Re^{n}, Y_{1}=$ $\left(y_{1}, y_{2}, \ldots, y_{k}\right) \in \Re^{k}, Y_{2}=\left(y_{k+1}, y_{k+2}, \ldots, y_{n}\right) \in \Re^{n-k}$ such that $X=$ $\lambda C X, J_{i}=\mu_{i} C_{i} Y_{i}, i=1,2$, where $C$ is a given jacobi matrix. Here $0<k<n$ and $J_{1}, J_{2}$ are $k \times k$ and $(n-k) \times(n-k)$ square matrices, respectively. Indeed We consider a generalized inverse eigenvalue problem of the form $J u=\lambda C u$.

Mathematics Subject Classification: 65F15, 65H15. Keywords: Jacobi matrix, Eigenvectors, Inverse eigenvalue problem


[^198]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On the circuits and cocircuits of splitting matroids 

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#### Abstract

In this paper, we characterize the circuits and cocircuits of splitting matroids $M_{X}, M_{X}^{\prime}$ in terms of the circuits and cocircuits of the original matroid $M$.


Mathematics Subject Classification: 05B35.
Keywords: Binary matroid, Splitting matroid, Circuit, Cocircuit, Support of a vector.

[^199]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference 12-15 September 2010, University of Urmia, Urmia-Iran <br> ( $\alpha, \beta$ )-Jordan Derivations of Triangular Algebras 

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#### Abstract

Let $A$ and $B$ be unital algebras over a commutative ring $R$, and $M$ be a unital $(A, B)$-bimodule and $\alpha, \beta$ be algebra homomorphisms of $A$. This paper determines all homomorphisms and hence all automorphisms of the triangular algebra $\operatorname{Tri}(A, M, B)=\left(\begin{array}{cc}A & M \\ 0 & B\end{array}\right)$ and using the characterizations, it is shown that under some conditions, every $(\alpha, \beta)$ Jordan derivation from the triangular algebra $\operatorname{Tri}(A, M, B)$ into itself is an ( $\alpha, \beta$ )-derivation. As a consequence several known results is extended.


## Mathematics Subject Classification:

Keywords: triangular matrix algebra, homomorphism, automorphism, $(\alpha, \beta)$ - derivation, $(\alpha, \beta)$-Jordan derivation.

[^200]
# The Nehari manifold for semilinear equation with Dirichlet BOUNDARY condition 

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#### Abstract

The Nehari manifold for the equation $-\Delta u(x)=b(x) u^{p}$ for $x \in \Omega$ together with Dirichlet boundary condition is investigated.


Keywords: variational method, Nehari manifold,Fibering maps.

[^201]
# Solution of nonlinear inverse problem by Tikhonov regularization method 

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#### Abstract

In this paper, a numerical algorithm based on finite-difference method and the least-squares scheme for solving a nonlinear inverse diffusion problem is proposed. At the beginning of the numerical algorithm, Taylors series expansion is employed to linearize nonlinear terms, removed the time-dependent terms by Laplace transform, and then finitedifference method is used to discretize the problem domain. The present approach is to rearrange the matrix forms of the differential governing equations and estimate unknown diffusion coefficient. The least-squares method is adopted to find the solution. To regularize the resultant illconditioned linear system of equations, we apply the Tikhonov regularization method to obtain the stable numerical approximation to the solution. All the computations are performed on the PC.


Mathematics Subject Classification: Primary 65M32, Secondary 35K05.
Keywords: Diffusion coefficient, Nonlinear inverse diffusion problem, Finite difference method, Least-squares method, Regularization method.

[^202]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On $\phi$-symmetric Kenmotsu manifolds 

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#### Abstract

In the present paper we study the $\phi$-recurrent Kenmotsu manifolds and we show that they are $\phi$-symmetric. Moreover we show these manifolds are Einstein manifolds.


Mathematics Subject Classification: 53C25, 53D15.
Keywords: $\phi$-recurrent manifold, Kenmotsu manifold.

[^203]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Weakly maximal submodules and local cohomology 

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#### Abstract

In this paper, by using the notion of weakly maximal submodule, we give some results about local cohomology modules.


Mathematics Subject Classification: 13D45, 13E05, 13 E 10.
Keywords: Weakly maximal submodules, Local cohomology.

[^204]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Numerical solution of stochastic partial differential equation 

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S.M. Hosseini


#### Abstract

In this paper for the approximate solution of stochastic partial differential equations (SPDEs), a class of finite difference method (with regards to the coefficients in the equations) is analyzed and then we discuss a new method based on spectral collocation method. We prove the consistency and stability of finite difference methods and investigate the influence of the multiplier (particularly multiplier of the random noise) in mean square stability. Numerical experiments are included to show the efficiency of these methods.


Mathematics Subject Classification: 60H15, 60H35.
Keywords: Stochastic partial differential system, finite difference method, spectral collocation method.

[^205]
# TOPOLOGICAL GAMES, EQUICONTINUITY AND SIGMA-FRAGMENTABILITY IN FUNCTION SPACE 

## ALIREZA KAMEL MIRMOSTAFAEE

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#### Abstract

We will introduce a topological game on $X \times X$, then we will show that if the second player does not have a winning strategy in this play, $C(X)$ with the pointwise topology is framented by the norm. In particular, if X is Valdivia compact, then $C_{p}(X)$ is sigma-fragmentable by the supremum norm.


Mathematics Subject Classification: Primary 54C30, 54C35, 54C05, Secondary 46E15.

Keywords: Topological game, equicontinuity, pointwise topology.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Characterizations of Shift Invariant Spaces 

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#### Abstract

Mathematics Subject Classification: 47A15, 42B99, 22B99. Keywords: locally compact abelian group, shift invariant space, frame, range function


[^206]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# The Finite Differences Method for Solution of An Inverse Problem with <br> Nonlinear Source Term 

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#### Abstract

In this paper, a nonlinear problems of inhomogeneous heat equation with linear boundary conditions will be considered. The surface temperature history of a heat conducting body will be identified. The approach of proposed method is approximated unknown function by polygons linear pieces which are determined consecutively from the solution of minimization problem based on the overspecified data. Some numerical examples also will be presented.


Mathematics Subject Classification: Primary 65M15, Secondary 35R30.

Keywords: Direct and Inverse Heat Conduction Problem, Residual Minimization, Chebyshev Polynomial, Least-Square Method, Implicit Finite Differences Approximation.

[^207]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference
12-15 September 2010, University of Urmia, Urmia-Iran

# KDV-Burrgers Solution with Convergence Analysis 

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Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# To Introduce a New Multigraph for Groups 

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#### Abstract

In this paper we define $S_{m}$ multigraph on arbitrary group G which is a multigraph with $\mathrm{m}+1$ vertexs and parallel edges. Finally we show some cyclic groups are $S_{m}$ multigraph.

Mathematics Subject Classification: 94C15, 20B05, 00AXX, 05C25. Keywords: Cyclic Groups, Stabilizers, $S_{m}$ multigraph


Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Approximate Solution of a Singular Integral Equation with a Cauchy Kernel Kernel on the Real Half-Line 

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#### Abstract

In this paper, exact solution of the integral equation with Cauchy kernel on the real half-line is presented. Then, Chebyshev polynomials are used to derive approximate solution of this equation.


Keywords: Inequality.

[^208]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran 

# Computing the Complete CS Decomposition 

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#### Abstract

An algorithm is developed to compute the complete CS decomposition (CSD) of a partitioned unitary matrix. The algorithm computes the complete 2 -by- 2 CSD, which requires the simultaneous diagonalization of all four blocks of a unitary matrix partitioned into a 2 -by- 2 block structure. The computation occurs in two phases. In the first phase, the unitary matrix is reduced to bidiagonal block form, as described by Sutton and Edelman. In the second phase, the blocks are simultaneously diagonalized using techniques from bidiagonal SVD algorithms of Golub, Kahan, and Demmel.


Mathematics Subject Classification: 65F30.
Keywords: singular value decomposition, bidiagonalization.

[^209]
# Numerical investigation of a Stefan problem arises from the release of drug from drug-delivery devices 

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#### Abstract

In this paper a general model is presented for the release of drug from porous nonswelling, transdermal drug-delivery devices. This model is investigated for a spacial case and analytical and numerical solutions based on wave similarity solutions and finite differences method are derived.


Mathematics Subject Classification: 65M06, 92B05, 35K15.
Keywords: drug-delivery devices, diffusion, moving boundary problem, numerical method

[^210]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Survey of cumulative residual entropy 

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#### Abstract

Recently, Rao et al[3], Asadi and Zohrevand[2] and Navarro et al[1] defined the cumulative residual entropy, dynamic cumulative residual entropy and dynamic cumulative past entropy, respectively, as some new measures of uncertainty. They studied some properties and applications of these measures. In this paper we obtain some results connecting these measures on the weighted distribution.


Keywords: Reliability function, Cumulative residual entropy, Dynamic cumulative past entropy, weighted distribution .

[^211]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Mathematical Study of Magnetic Resonance Imaging Process in Blood Vessels 

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Mathematics Subject Classification: 65M06, 92B05, 35K20.
Keywords: Bloch NMR equations, Differential equations, Boubaker polynomials;finite difference method.

[^212]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> New approach of variational iteration method for nonlinear partial differential equations with exponential nonlinearity 

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## S. Keighobadi ${ }^{1}$

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#### Abstract

In this work, new approach of the variational iteration method by using $r$ terms of Taylor's series is applied for solving nonlinear partial differential equations with exponential nonlinearities. Numerical results are revealing its effectiveness and simplicity.


Mathematics Subject Classification: 35A35, 65M99, 65N99.
Keywords: Nonlinear partial differential equation, Exponential nonlinearity, Variational iteration method, Taylor's series.

[^213]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran 

# The power graph of groups 

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#### Abstract

The power graph of a group $G$ is the graph whose vertex set is $G$ and two elements being adjacent if one is a power of the other. We obtain some properties of graph theory such as independence number and clique number for group $Z_{p^{\alpha}} \times Z_{2}$ and group $D_{2 p^{\alpha}}$, where $p$ is a prime number and $\alpha \geq 1$ is a positive integer.


Keywords: group, power graph, independence graph, clique number.

[^214]
# Inner Totally Positive Matrices with Two Spectrum in Common 

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## F. Gilasi


#### Abstract

Let $\sigma(A)$ be the set of eigenvalues of $A$ and $\sigma_{i}(A)$ be the set of eigenvalues of $A_{i}$, where $A_{i}$ is submatrix of $A$ after deleting the $i^{\text {th }}$ rows $i^{\text {th }}$ column of $A$. Suppose $\rho=\left\{\rho_{1}, \rho_{2}, \ldots, \rho_{n}\right\}$ and $\gamma=\left\{\gamma_{1}, \gamma_{2}, \ldots, \gamma_{n}\right\}$ be staircase sequences. A matrix $A \in M_{n}$ is called a staircase matrix with row and column, $\rho, \gamma$; if $a_{i j}=0$ when $i>\gamma(j)$ or $j>\rho(i)$. A minor $A(\alpha ; \beta)$ with $\alpha=\left\{\alpha_{1}, \ldots, \alpha_{k}\right\}, \beta=\left\{\beta_{1}, \ldots, \beta_{k}\right\}$ is said to be an inner minor of A if $\alpha_{i} \leq \gamma\left(\beta_{i}\right), \beta_{i} \leq \rho\left(\alpha_{i}\right)$ for $i=1,2, \ldots, k$. A is said to be inner tatally positive(ITP) if every inner minor of A is positive. We show that an ITP matrix may be reduced by similarity transformations to an ITP band matrix, and may alternatively be filled-in by similarity transformations to become a $T P$ matrix. This operations keep two spectrum of the given matrix, i.e. $\sigma(A)$ and $\sigma_{i}(A)$.


Mathematics Subject Classification: 15A48, 15A23
Keywords: Oscillatory matrices, totally positive matrices, inner totally positive matrices

[^215]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# the skew half-normal distribution 

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M. Rafiei


#### Abstract

In this paper we introduce the skew half-normal distribution, which is skewed by the parameter $\lambda$ and is denoted as $\operatorname{SHN}(\lambda)$. This distribution belongs to a family of distribution which includes the half-normal distribution along with an extra parameter to regulate skewness. We derive the density function and various properties of this new distribution. The properties derived include the cumulative distribution function, the $r$ th moment, the $r$ th central moment, moment generating and characteristic functions, mean deviation about the mean, Renyi and Shannon entropy, estimation of parameter by the method of maximum likelihood and simulation issues. Finally, the flexibility of the new distribution is illustrated in an application to a real data set.


Mathematics Subject Classification: Primary 62E99, Secondary 60E99.
Keywords: half-normal distribution, hypergeometric function, skweness, moment generating function.

[^216]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Induced topological pressure for countable state markov shifts 

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Department of Mathematics, The University of Guilan, P.O. Box 1841, Rasht, Iran.


#### Abstract

In this paper we introduce the notion of induced topological pressure for countable state Markov shift. This helps to clarify the connection between the various different notions of pressure for such Markov shift. One first natural application of our formalism is given by an exhausting principle. Also special flows of countable state Markov systems will be discussed in some detail.


Mathematics Subject Classification: Primary 37A45, Secondary 37D35.
Keywords: Thermodynamical formalism, pressure, special flows, group extensions, countable state Markov shift.

[^217]
# SOME RESULTS ON LOCAL COHOMOLOGY MODULES defined by a pair of ideals 

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#### Abstract

Let $R$ be a commutative Noetherian ring, $I$ and $J$ two ideals of $R$ and $M$ a finitely generated $R$-module. It is shown that (1) if $t$ is an integer such that $H_{I, J}^{i}(M)$ is finitely generated for all $i<t$ and $N$ a finitely generated submodule of $H_{I, J}^{t}(M)$, then $H_{I, J}^{t}(M) /\left(N+J H_{I, J}^{t}(M)\right)$ has finite associated primes; (2) if $M$ is of dimension $n$, then $H_{I, J}^{n}(M) / J H_{I, J}^{n}(M)$ and $H_{I, J}^{n}(M) / I H_{I, J}^{n}(M)$ are Artinian.


Mathematics Subject Classification: 13D45, 13E10.
Keywords: Artinian modules, Associated primes, Local cohomology modules.

[^218]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On the geometry of bi-invariant Randers metrics on Lie groups 

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#### Abstract

In this paper we study the geometry of Lie groups with bi-invariant Randers metric. We prove that bi-invariant Randers metrics are of Berwald type. We give an explicit formula for the flag curvature of bi-invariant Randers metrics.


Mathematics Subject Classification: Primary 53C60, Secondary 53C30.
Keywords: Inequality.

[^219]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A new modified homotopy analysis method for solving nonlinear differential-algebraic equations 

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#### Abstract

In this paper, modified homotopy analysis method is used for numerical solution of nonlinear systems of differential-algebraic equations. This method is very simple and convenient to give approximate solution. The scheme is tested for two nonlinear systems of differential-algebraic equations and the results demonstrate simplicity and efficiency of this method.


Mathematics Subject Classification: 65L80, 34A09.
Keywords: Differential-algebraic equations, Homotopy analysis method, Modified homotopy analysis method.

[^220]
# Solving boundary value problems of fractional order by Galerkin methods with fractional polynomials 

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#### Abstract

In this presentation, numerical solutions are obtained for the ZakharoveKuznetsov equation by Variational Homotopy Pertebration method(VHPM) and Variational iteration method (VIM) are discussed. Comparisons are made among the Variational Iteration Method (VIM) and the proposed method (VHPM). The results reveal that the proposed method VHPM is very effective and can be used for other nonlinear problems in mathematical.


Mathematics Subject Classification: Primary 65L60, Secondary 34A08.
Keywords: Galerkin method, Fractional integral, Caputo fractional derivative, fractional polynomials.

[^221]
# Collocation method for solving Fredholm integral equation of the first kind using Shannon wavelet system 

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#### Abstract

Wavelet-collocation approach for numerical solution of linear Fredholm integral equation of the first kind with specific kernels arising in electromagnetics problems is presented. We implement the method in two ways; using Shannon scaling functions alone, and using Shannon scaling functions together with Shannon wavelet functions. Its computational efficiency is compared with that of collocation method using Haar scaling functions.


Mathematics Subject Classification: Primary 65R20, Secondary 41A30.
Keywords: First kind Fredholm integral equation, Collocation method, Numerical solution, Shannon wavelet system.

[^222]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Fractional Fourier Transform and its applications 

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#### Abstract

In this paper, we introduce the fractional Fourier transform (FRFT) and then present some new results, such as the interpretation of this transform as a rotation in the time-frequency plane, which can be thought of as the fourier transform (FT) to the n-th power where n need not be an integer. Then, an application of the FRFT is given, and finally we will investigate two advantages of the FRFT in comparison with FT.


Mathematics Subject Classification: 42A38, 26A33, 34k37.
Keywords: Fractional Fourier Transform, Fourier Transform, signal processing and analysis.

[^223]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Periodic Quasi-Wavelets for Nonlinear Integral Equations 

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epartment of Mathematics, Faculty of Science, Urmia University, P.O. Box 165, Urmia, Iran.


#### Abstract

A survey on the use of the periodic quasi-wavelets method for solving nonlinear integral equations is presented. This problem is solved with the aid of collocation technique to reduce the solution of nonlinear integral equations to a nonlinear system of equations which can be solved by the Newton's method.


Mathematics Subject Classification: Primary 45G15, Secondary 65T60.
Keywords:Nonlinear integral equation, Periodic quasi-wavelets, Collocation method.

[^224]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On the numerical solution of Zakharove-Kuznetsov equation 

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#### Abstract

In this presentation, numerical solutions are obtained for the ZakharoveKuznetsov equation by Variational Homotopy Pertebration method(VHPM) and Variational iteration method (VIM) are discussed. Comparisons are made among the Variational Iteration Method (VIM) and the proposed method (VHPM). The results reveal that the proposed method VHPM is very effective and can be used for other nonlinear problems in mathematical.


Mathematics Subject Classification: 47J30, 49S05.
Keywords: Variational Homotopy Pertebration Method, Variational Iteration Method, Zakharove-Kuznetsov equation.

[^225]
# Refinement by Iteration for Approximated Eigenvalues of Bounded Operators on a Banach Space 

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#### Abstract

In this paper, we introduce some defect correction methods, refining the approximations of eigenpair of a bounded operator defined on a Banach space. These methods consist the elementary iteration, double iteration, Rayleigh-Schrödinger iteration, and acceleration refinement methods.


Mathematics Subject Classification: 45C05.
Keywords: elementary iteration, double iteration, Rayleigh-Schrödinger iteration, acceleration refinement.

[^226]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Criteria for Maximal Abstract Monotonicity with Applications in Optimization 

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#### Abstract

In this paper, we develop a theory of monotone operators in the framework of abstract convexity. Indeed, by using an additivity constraint qualification, we prove a generalization of Fenchel's duality theorem in the framework of abstract convexity, and give criteria for maximal abstract monotonicity. Finally, we present necessary and sufficient conditions for maximality of abstract monotone operators.


Mathematics Subject Classification: Primary 47H05, 47H04, 52A01, 26A51, Secondary 26B25.

Keywords: Constraint qualification, Generalized Fenchel's duality, Monotone operator, Abstract monotonicity, Abstract convex function, Abstract convexity.

[^227]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# SMALL CONJUGACY CLASSES IN THE AUTOMORPHISM GROUPS OF RELATIVELY FREE GROUPS $F / R$ 

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#### Abstract

In a series of papers [4,6,7] Dyer and Formanek justified several conjectures by Baumslay on the automorphism towers of finitely generated relatively free groups. In particular, they proved that the automorphism group $\operatorname{Aut}\left(F_{n} / \hat{R}\right)$ of the group $F_{n} / \hat{R}$ is complete where R is a characteristic subgroup of $F_{n}$ which is contained in the commutator subgroup $\dot{F}_{n}$ of $F_{n}$ such that the quotient group $F_{n} / R$ is residually torsion-free nilpotent. The aim of the present paper is to extend the latter result to infinitely generated relatively free groups.


[^228]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A REMARK ON THE ABELIAN p-GROUPS 

## A. MOHAMADPOUR, M. PARVIZI, P. NIROOMAND

Damghan University, Damghan, Iran.


#### Abstract

In this paper we try to classify all finite abelian p- groups with multipliers of the same order.


Mathematics Subject Classification: 20D15; Secondary 20E34; 20F18. Keywords: Finite abelian p-group, Schur multiplier.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Numerical solution of fractional integro-differential equations by using Legendre wavelets 

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#### Abstract

In this study, the Legendre wavelet and its operational matrix of integration are first presented. Legendre wavelet approximating method is then employed to reduce the fractional integro-differential equation to the algebraic equations. Illustrative examples are included to demonstrate the validity and applicability of the technique.


Keywords: Inequality

[^229]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Hybrid Steepest-Descent Methods for a New Class of Nonlinear Operators 

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#### Abstract

In this talk, we prove the following: Let $T: H \rightarrow H$ be a nonexpansive mapping with $C=F i x(T) \neq \emptyset$ and $B: H \rightarrow H$ be $(r, T)$-strongly monotone and $\mu$-Lipschitzian. Applying hybrid steepest-descent method, we generate a sequence $\left\{x_{n}\right\}$ converging strongly to the unique solution of the variational inequality $V I(B, C)$.


Mathematics Subject Classification: Primary 47H09, 47H10, Secondary 47J20.

Keywords: Hybrid steepest-descent methods, convergence, nonexpansive mappings, Hilbert space.

[^230]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# An overlapping domain decomposition method applied to the method of fundamental solution 

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#### Abstract

We propose an overlapping domain decomposition method (DDM) to improve the method of fundamental solution (MFS). The MFS often tackles the Poisson-type equations by approximating the particular solution using radial basis functions (RBF). The RBF interpolation often leads to ill-conditioned problems. This work suggests a domain decomposition technique which is a standard way to localize the globally supported RBF.


Mathematics Subject Classification: Primary 65C20, Secondary 35A08, 65M55.

Keywords: Method of fundamental solution, Overlapping domain decomposition.

[^231]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> $C_{0}$-semigroups and center manifold theory 

H. M. Mohammadinezhad ${ }^{1}$<br>Department of Mathematics, Birjand University, P. O. 97175/615, Birjand, Iran .


#### Abstract

In this paper we extend center manifold theory to a class of infinite dimensional problems. For simplicity we only consider equations of the form $\dot{w}=C w+N(w), \quad w(0) \in Z$ where $Z$ is a Banach space, $C$ is the generator of a strongly continuous linear semigroup $S(t)$ on $Z$ and $N$ : $Z \longrightarrow Z$ has a continuous second derivative with $N(0)=0, N^{\prime}(0)=0$.


Mathematics Subject Classification: 34C05, 34A34.
Keywords: $C_{0}$-semigroup, center manifold, generator, invariant.

[^232]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Regression Outliers with Singular Spectrum Analysis 

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Mathematics Subject Classification: 62J05, 93E10, 93E11. Keywords: Least Square, Outlier, Singular Spectrum Analyze.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Values represented by a Pfister form 

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#### Abstract

A result due to A. Pfister gives a lower bound for the number of square classes of the multiplicative group of a field $K$ in terms its level. The aim of this talk is to present a generalization of this result by obtaining a lower bound for the index of the group of nonzero values represented by a Pfister form. This talk is based on an ongoing collaboration with G. Berhuy (Institut Joseph Fourier) and N. Grenier-Boley (Université de Rouen).


Mathematics Subject Classification: Primary 11E04, 11E25, 11E39, 11E81

Keywords: Level of a field, quadratic form, Pfister form, sums of squares, number of square classes.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Orthogonal Collocation Method for Fractional Integro-Differential Equations 

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#### Abstract

In this paper, the orthogonal collocation, an easy-to-use variant of the spectral methods for the numerical solution of fractional integrodifferential equations(FIDE's), is considered. In order to obtain matrix-vector-product approach for spectral approximations to FIDEs, the kernel function in integral term is approximated by using two variable interpolation polynomials. Numerical results are presented, which clarify the high accuracy of the method.


Mathematics Subject Classification: Primary 65R20, Secondary 34A05.

Keywords:Fractional integro-differential equations, Caputo derivative, orthogonal collocation method.

[^233]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# An Equitable Fixed Cost Allocation Method 

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#### Abstract

Li et. al. (Eur.J.Oper.Res.(2009)) argued that the method of treating the allocated cost as an extra input of each DMU is questionable. Generally speaking, if each DMU has other cost measures then the allocated cost should be combined with these costs to form a single input measure during performance measurement. They developed a DEAbased approach to allocate the fixed cost among various DMUs. Their method was hardly computational and the first principle: the minimum gaps on the allocated cost among all DMUs, was questionable. In this paper we improve their method and develops a DEA approach to allocate the fixed cost among various DMUs in an equitable way.


Mathematics Subject Classification: 90Cxx; 90C05

Keywords: Data Envelopment Analysis; equitable allocation.

[^234]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Characterization of a class of Hamiltonian connected graphs 

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#### Abstract

. In this paper, we define the concept of critical Hamiltonian connected graphs. We present some necessary conditions for a graph to be critical Hamiltonian connected. Moreover, we characterize all critical Hamiltonian connected graphs which contains a vertex adjacent to all the other vertices.


Mathematics Subject Classification: 05C45, 05C15.
Keywords: Inequality.

[^235]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# The stone-weierstrass theorem in extended lipschitz algebras 

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#### Abstract

Let ( $X, d$ ) be a compact metric space and $K \subseteq X$ be a non-empty compact subset. Let $\operatorname{Lip}(X, K, \alpha)(\operatorname{lip}(X, K, \alpha))$ be the set of functions in $C(X)$ whose restriction on $K$ belongs to $\operatorname{Lip}(K, \alpha)(\operatorname{lip}(K, \alpha))$. In this paper, we prove an extension of Hedberg's theorem in extended lipschitz algebras.


Mathematics Subject Classification: 46J10, 46J15.
Keywords: Banach function algebra, Lipschitz algebra.

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Inequalities for $(\alpha, \beta)$-Normal Operators in Hilbert Spaces 

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#### Abstract

In this paper we study some new inequalities for norm on Banach algebra $B(\mathcal{H})$ of all bounded linear operators $T: \mathcal{H} \rightarrow \mathcal{H}$, where $\mathcal{H}$ is Hilbert space and $T,(\alpha, \beta)$-normal operator.


Mathematics Subject Classification: Primary 47A12, Secondary 47A30, 47B20.

Keywords: Normal Operator, Majorization Lemma, Numerical Radius, Norm Inequality in Normed Linear and Inner Product Spaces.

[^236]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On The approximate solution of Integral Equations on Polygons in $\mathbb{R}^{2}$ 

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#### Abstract

This article introduces a numerical scheme for solving integral equations on polygons, based on a Gauss-like cubature formula, which does not need any preprocessing like triangulation of the domain. The applied cubature formula is exact for polynomials of degree at most $2 n-1$, using $N \sim m n^{2}$ nodes, which $m$ is the number of sides that are not orthogonal to a given line and not lying on it. The convergence analysis of the method is also provided and some numerical experiments are presented which confirm the accuracy of the mentioned approach.


Mathematics Subject Classification: 65R20, 45L10, 65D32.
Keywords: Integral equation, Gauss-like cubature, Polygon, Numerical treatment.

[^237]
# Numerical Solution of Functional Integral Equations by Using B-Splines 

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## A. Shahmohammadi

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Sh. Mashhoodi ${ }^{1}$

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#### Abstract

This paper describes an approximating solution, based on Lagrange interpolation and spline functions, to treat functional integral equations of Fredholm type and Volterra type. This method can be extended to functional differential and integro-differential equations. For showing efficiency of the method we have investigated some numerical examples.


Mathematics Subject Classification: 65R20, 65D07, 65D05.
Keywords: Lagrange interpolation, B-spline functions, Functional integral equation.

[^238]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# The Optimal Replacement of Machines in Continuous time Using Integral Equations Approach 

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#### Abstract

The optimal replacement of "machines" or "vintage capital" under Technological Change (TC) plays an important role in simulation of economic growth, operations research and management sciences. The optimal replacement process in continuous time can be described by the delay nonlinear Volterra integral equation, in which the unknown function appears both in upper limits of integration and in the integrand and its solution is essential for finding the optimal policy of equipment replacement under technological advances. Here, the numerical analysis and simulation of this model will be discussed.


Mathematics Subject Classification: Primary 45G10, Secondary 49K22.
Keywords: Nonlinear Optimization, Integral Equation, optimal Equipment lifetime.

[^239]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> The Combination of Collocation and Multigrid Methods in Solution of the 1-D Telegraph Equation 

M. Moini<br>Department of Mathematics, Islamic Azad University, Roodehen, Iran.


#### Abstract

In this article, we introduce a high-order accurate method for solving one-space dimensional Telegraph equation. We apply a compact finite difference approximation of two and four orders for discretizing spatial derivative of linear telegraph equation and collocation method for the time component. This method is unconditionally stable and solves the telegraph equation with high accuracy. In this technique the solution is approximated by a polynomial at each grid point that its coefficients are determined by solving a linear system of equations. We employ the multigrid method for solving the resulted linear system. Multigrid method is an iterative method which has grid independently convergence and solves the linear system of equations in small amount of computer time.


Mathematics Subject Classification: 65M70, 65M55, 65L12.
Keywords: Collocation technique; Compact finite difference schemes; Multigrid method; Telegraph equation.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On subdirectly irreducible $S$-acts over left zero semigroups 

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#### Abstract

The aim of this paper is to characterize subdirectly irreducible $S$ acts over left zero semigroups. Also we compute the number of such acts and specify cogenerators acts over left zero semigroups.


Mathematics Subject Classification: 08A60, 08B30, 08C05.
Keywords: $S$-act, separated, subdirectly irreducible, left zero semigroup.

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> ON THE CARDINALITY OF COMPLETELY SIMPLE SUBSEMIGROUPS 

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## M. Moghimian ${ }^{1}$

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#### Abstract

In this paper, the cardinality of a completely simple subsemigroup are considered. In general, the cardinal number of a completely simple subsemigroup of a finite completely simple semigroup $S$ dose not divide the cardinal number of $S$, as is valid in the group case. We study sufficient conditions for which these properties hold in the completely simple subsemigroup setting.


Mathematics Subject Classification: Primary 20M10, Secondary 20M05.

Keywords: Completely Simple Subsemigroup, Rees Isomorphism.

[^240]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Unitary Cayley Graph over Finite Commutative Ring 

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#### Abstract

We study the unitary Cayley graph in association with an arbitrary finite commutative ring with an identity element, we compute eigenvalues and classify all hyperenergetic graphs within this class and also we calculate the energy of the complement of this graph. In addition, we prove that if $U \Gamma(R) \simeq U \Gamma(S)$ then $\frac{R}{J_{R}} \simeq \frac{S}{J_{S}}$ where $J_{R}$ and $J_{S}$ are radical jacobson of $R$ and $S$ respectively.


Mathematics Subject Classification: Primary 05C50, Secondary 16U60.
Keywords: Unitary Cayley graph, Local ring; Category product; Eigenvalue of graph; Energy of graph.

[^241]
# Modification Of Cross Efficiency Obtained By Common Weights 

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#### Abstract

This paper analyzes the potential flawes which happens when the ultimate average cross efficiency scores are used and we consider the $D M U_{s}$ as the players in a cooperative game, where the characteristic function values of coalitions are defined to compute the Shapley value of each DMU, and the common weights associate with the imputation of the Shapley values are used to determine the ultimate cross efficiency scores. In this paper, we modified said model for avoiding occurence zero weight in determination of cross efficiency value.


Mathematics Subject Classification: 91A12.
Keywords: Cooperative game, Common weights, Cross efficiency, Data Envelopment Analysis (DEA), Shapley value

[^242]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Structures of CTI-Groups 

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#### Abstract

A finite group $G$ is called a CTI-group if any cyclic subgroup of $G$ has a trivial intersection with its distinct conjugates. In this paper we will describe structures of finite CTI-groups.


Mathematics Subject Classification: 20D10, 20E34.
Keywords: CN-Group, TI-Group, ATI-Group, QTI-Group, CTI-Group.

[^243]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Uniform Continuity Of Exponential Spectrum On Commutative Banach Algebras 

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#### Abstract

We know that the spectrum function, $x \rightarrow S p x$, is uniformly continuous on commutative Banach algebra A. In this paper we see that the exponential spectrum of A , $x \rightarrow \varepsilon(x)$, is uniformly continuous too.


Mathematics Subject Classification: 47A11, 47A10, 47B48.
Keywords: spectrum, exponential spectrum.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# g-frame generator sets 

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#### Abstract

We use a unitary system and a set of linear operators to construct a $g$-frame on $H$ and we obtain some important properties of this class of g -frame generator sets.


Mathematics Subject Classification: 94A12, 42C15, 68M10, 46C05.
Keywords: Frames, Generalized frames, Operator valued frames, G-frame generator sets, Unitary systems.

[^244]
# Weakly compact right multipliers on $L^{1}(\mathcal{G})^{\prime \prime}$ 

$$
L^{1}(\mathcal{G})^{\prime \prime}
$$

M. J. Mehdipour ${ }^{1}$

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#### Abstract

In this paper, we investigate some result about weakly compact right multipliers on the Banach algebra $L^{1}(\mathcal{G})^{\prime \prime}$. We show that if $\mathcal{G}$ is not amenable, then there is no non-zero weakly compact right multiplier on certain ideals of $L^{1}(\mathcal{G})^{\prime \prime}$.


Mathematics Subject Classification: 43A15, 43A20, 47B07, 47B48.
Keywords: Locally compact group, right multiplier, weakly compact operator, right weakly completely continuous element.

[^245]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On Group Classifications and Invariant Solutions of the Cylindrical Helmholtz Equation 

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#### Abstract

In this expository paper, we investigate symmetry properties of cylindrical homogeneous Helmholtz equation for a three dimensional space. Then considering the symmetry group of the equation, we give a complete set of its functionally independent invariants, a form of general solutions, the structure of point symmetry group, an optimal system of one-dimensional subalgebras. In addition, we classify the invariant solutions of the equation by introducing a complete set of fundamental invariants corresponding to each operator of the optimal system.


Mathematics Subject Classification: 34C14, 35J05, 70G65.
Keywords: Helmholtz equation, Lie point symmetries, optimal system, Invariant solutions.

[^246]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference
12-15 September 2010, University of Urmia, Urmia-Iran

# Local Automorphisms of $C^{*}$-Algebras with non-zero Commutative Ideal 

A. Taghavi, F. Mehryar

University of Mazandran, Babolsar, Iran.
Keywords: Local automorphisms, Ideal, Purely infinite.

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Radical functors related to radical and coradical classes in the category of modules 

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#### Abstract

The properties of two classes of radicals in the category of modules; E-radicals and T-radicals are studied by Timoshenko and Krylov. In this paper we study the preradicals and radicals in the category of modules, in their most general form, as radical functors.


Mathematics Subject Classification: 16S90, 16D90.
Keywords: Category, module, radical functor, (co)radical class.

# SUBCLASSES OF MEROMORPHICally UNIVALENT FUNCTIONS ASSOCIATED WITH SALAGEAN OPERATOR 

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#### Abstract

Making use of salagean operator, new classes of univalent functions was defined. We investigated the coefficient bounds, radii of starlikeness and convexity and some interesting properties for this classes.


Mathematics Subject Classification: Primary 30c45, Secondary 30c45, 30c45.

Keywords: Analytic functions, Starlike and convex functions, Meromorphic functions.

[^247]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# EXISTENCE RESULTS FOR NONHOMOGENEOUS SYSTEMS OF ELLIPTIC EQUATION WITH LACK OF COMPACTNESS 

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#### Abstract

We establish the existence of a nontrivial solution for inhomogeneous quasilinear elliptic systems, governed by two Pseudo-Laplacian operators. Our result depending on the local minimization.


Mathematics Subject Classification: 35J60; 35J30; 35B40.
Keywords: Elliptic systems; Nehari manifold; Local minimization.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A Numerical Study of Nonlinear Partial Differential Equation 

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## A. Heydari

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#### Abstract

In this paper, we use a kind of univariate Multiquadric (MQ) radial basis function(RBF) quasi-interpolation to solve nonlinear partial differential equation (PDE). we propose a numerical scheme, by using the derivative of the quasi-interpolation to approximate the spatial derivative of the dependent variable and finite difference method(FDM). Our numerical examples are solving Korteweg-de Vries (KdV) equations.


Mathematics Subject Classification: 37N30.

Keywords: KdV equation, MQ quasi-interpolation, RBF.

[^248]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A new system of variational inclusions with B-monotone operator in Banach spaces 

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#### Abstract

In this paper, we introduce a new class of operator-B-monotone operators in Banach space. We define a proximal mapping associated with the B-monotone operator and show its Lipschitz continuity. We also consider a new system of variational inclusions with B-monotone operators in Banach spaces and constructed a new iterative algorithm for solving the system of variational inclusions in Banach spaces. Under some suitable conditions, we prove the convergence of the iterative sequence generated by the algorithm.


Mathematics Subject Classification: 49J40, 47H05.
Keywords: B-monotone operator, Proximal mapping, Iterative Algorithm, System of variational inclusions.

[^249]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Strong Numerical Methods For Stochastic Differential Equations 

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#### Abstract

In this paper we discuss three-stage stochastic Runge-Kutta (SRK) methods for computing strong solutions of Stratonovich stochastic differential equations (SDEs). Two new SRK methods are constructed in this paper. They are explicit and semi-implicit SRK methods of strong global order 1 with minimum principal error coefficients. The stability properties and numerical results show the effectiveness of these methods by prsenting some numerical results.


Mathematics Subject Classification: 60H10, 65L06, 65L20.
Keywords: Stochastic differential equations, Runge-Kutta methods, Numerical stability.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Comparison numerical simulation of stochastic differential equation with white and colored noise in ship heave motion 

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#### Abstract

Modeling of ship heave motion in still waters by ordinary differential equations ignores stochastic effects. By adding random elements into the differential equations, a system of stochastic differential equations (SDEs) arises which can describe the ship motion in irregular waves. This paper compares the numerical solution of stochastic differential equation for ship heave motion with white and colored noise. For this purpose the deterministic model is replaced by stochastic models by adding a noise term in force, and then these models will be solved analytically and numerically. Finally by giving an example the comparison between white and colored noise will be presented.


Mathematics Subject Classification: 60H10, 60 H 35 .
Keywords: Stochastic differential equation, White noise, Color noise, ship heave motion.

[^250]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# On Fuglede-Putnam type theorems 

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#### Abstract

Let $A, B, X \in \mathbf{B}(\mathcal{H})$ for some complex Hilbert space $\mathcal{H}$ and $\tilde{A}$ denote the Aluthge transformation of $A$. Then $A X=X B$ implies $\tilde{A} X=X \tilde{B}$, whenever it implies that $A^{*} X=X B^{*}$. We show that if $A, B^{*}$ are loghyponormal and $\tilde{A} X=X \tilde{B}$ then $A X=X B$. If $A=U|A|$ be the polar decomposition of $A, U|A|^{\frac{1}{2}} \geq a \geq 0$ and $X$ is an operator such that $U^{*} X=X U$, then we prove that $\left\|\tilde{A}^{*} X-X \tilde{A}\right\|_{p} \geq 2 a\left\||A|^{\frac{1}{2}} X-X|A|^{\frac{1}{2}}\right\|_{p}$.


Mathematics Subject Classification: Primary 47B20, Secondary 47B15, 47A30.

Keywords: Fuglede-Putnam theorem, Aluthge transformation, norm inequality, hyponormal, log-hyponormal, p-hyponormal, polar decomposition, Schatten $p$-norm.

[^251]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

## Properties of $G$-frames

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#### Abstract

We give some properties of $g$-frames in Hilbert spaces.


Mathematics Subject Classification: 42C15, 46C05, 47B10.
Keywords: frame, $g$-frame, dual $g$-frame, Parseval $g$-frame, $g$-frame approximation.

[^252]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Numerical solution of Volterra-Fredholm integral equations by using CAS wavelets 

Reza Ezzati<br>Department of Mathematics, Karaj Branch, Islamic Azad University, Karaj, Iran.<br>Saeid Najafalizadeh ${ }^{1}$<br>Department of Mathematics, Karaj Branch, Islamic Azad University, Karaj, Iran.


#### Abstract

In this paper, first we introduce CAS wavelets and approximate functions by using them, then we use CAS wavelets as a collocation bases to change the Volterra-Fredholm integral equations to a system of algebraic equations. Finally, some numerical examples illustrate the efficiency of this method.


Mathematics Subject Classification: 65RXX, 33F05, 65LXX.
Keywords: integral equation, CAS wavelets, Operational matrix.

[^253]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> stability and Hopf bifurcation for a delayed logistic population model 

M. Najafi ${ }^{1}$<br>K. Ghanbari<br>Department of Mathematics, Sahand University of Technology, Tabriz, Iran.


#### Abstract

In this paper the dynamics of a logistic equation with discrete delay are investigated, together with the local and global stability of the equilibria. In particular, the conditions under which a sequence of Hopf bifurcations occur at the positive equilibrium are obtained. Explicit algorithm for determining the stability of the bifurcating periodic solutions and the direction of the Hopf are derived. Global existence of periodic solutions is also established by using a global Hopf bifurcation result.


Mathematics Subject Classification: 37F45, 37G15.
Keywords: Logistic, Bifurcation, delayed, Population

[^254]
# Numerical Solution of Nonlinear Volterra Integral Equations Using a Quadratically Convergent Iterative Scheme 

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#### Abstract

The iterations of the quasilinear technique when is employed to the nonlinear volterra integral equations, are expressed as linear integral equations. The solutions of these linear equations are approximated using one-step collocation method that is carried out on the Chebyshev nodes. Combining these numerical solutions and iterations of the quasilinear technique yields an approximation solution to the nonlinear integral equation. The convergence is considered and some numerical examples confirm the accuracy of the solution.


Mathematics Subject Classification: 45D05, 65L60.
Keywords: Integral equations, Quasilinear technique, one-step collocation method.

[^255]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# STABILIZERS AND ANNIHILATORS IN BCK-ALGEBRAS 

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#### Abstract

in this paper, we introduce the notion of stabilizers and annihilators on a BCK-algebra and compareable its properties.


Keywords: BCK-algebra, Stabilizer,Annihilator.

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> SPECIAL WEYL PROJECTIVE CURVATURE ON FINSLER MANIFOLDS 

SAMANEH. AMOZEGAR, BEHZAD. NAJAFI

Shahed University, Tehran, Iran.


#### Abstract

Finsler metrics are a natural generalization of Rie- mannian metrics. Some theorems from Riemannian world have been extended to Finslerian one. But, celebrated Beltrami the- orem asserting that a Rimannian manifold is projectively at if and only if it is of constant curvature, is no longer true for generic Finsler manifolds. Here, we state and prove a Beltrami type theo- rem for Finsler manifolds, using the notion C-projectively at.


Mathematics Subject Classification: Primary 58E20.
Keywords: Inequality.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Some results on non-existence of 

$$
t-(v, t+1) \text { latin trades }
$$

M. S. Najafian ${ }^{1}$<br>Department of Mathematics, Zanjan University, P. O. Box 313, Zanjan, Iran.


#### Abstract

Latin bitrades have been introduced in connection to Latin squares. In recent years this concept has been generalized and Latintradestvk are defined. In this talk we study the spectrum (that is, the set of allowable volumes) of $t-(v, t+1)$ Latin trades, $S(t, t+1)$, and present some new results on non-existence of Latintradestvt +1 .


Mathematics Subject Classification: 05B15.
Keywords: Latin bitrade, $t$-Latin trade, Spectrum.

[^256]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> on pointwise multipliers of modulation spaces 

Ghassem Narimani ${ }^{1}$


#### Abstract

It is proved that any function in the Wiener amalgam space $W\left(H_{p}^{s}\left(\mathbf{R}^{\mathbf{d}}\right), \ell_{\infty}\right)$ is a pointwise multiplier for modulation spaces $M_{p, q}^{r}\left(\mathbf{R}^{\mathbf{d}}\right)$ whenever $1 \leq$ $p, q \leq \infty$ and $s>|r|+d$.


Mathematics Subject Classification: 26D10, 46E25, 42B25.
Keywords: modulation space, pointwise multiplier, Bessel potential spaces, Wiener amalgam spaces

[^257]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Solution of Integral Equation System by Using Wavelet Galerkin Method 

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#### Abstract

In this paper, we propose the cubic semiorthogonal compactly supported B-spline wavelets as basis functions for the efficient solution of the system of Fredholm integral equations. The method is computationally attractive, and applications are demonstrated through illustrative example.


Mathematics Subject Classification: 65C30, 65D07, 65L60.
Keywords: system of integral equations, Galerkin method, B-spline wavelets.

[^258]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# PRIMARY TORSION MODULES OVER ONE DIMENSIONAL DOMAINS 

F. Shahsavar

M. Nazari ${ }^{1}$
H. Fazaeli


#### Abstract

Throughout this paper, we consider only commutative rings with identity and modules which are unitary. In this paper it is shown that if $M$ is a primary torsion module over one dimensional domain $R$, then $\theta(M)=R$ or $\theta(M)=\operatorname{ann}(M)=\operatorname{ann}(r m)$ in which $\theta(M)=$ $\sum_{m \in M}(R m: M)$. Moreover if $M$ is also projective, then $\bigcap_{I M \neq 0}=R$ or $\bigcap_{I M \neq 0}=0$.


Mathematics Subject Classification: Primary 13C05, Secondary 13C13.
Keywords: Multiplication module, Primary Module,Torsion module.

[^259]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A modified preconditioned AOR iterative method for L-matrices 

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#### Abstract

In recent years, a number preconditioners have been applied to solving of $L$-matrices with AOR method (see [1]). In this paper we use $\left(I+S_{\alpha}^{\prime}\right)$ instead of $\left(I+S_{\alpha}\right)$ comprised with H.Wang's precondition [1] and obtain better convergence rate. A numerical example is also show that our preconditioner has the best convergence rate.


Mathematics Subject Classification: 34A30, 65F10
Keywords: Preconditioning, Week regular splitting, $L$-matrix, AOR method.

[^260]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference
12-15 September 2010, University of Urmia, Urmia-Iran

# Characterizations of Continuous G-Frame in Hilbert $C^{*}$-Modules 

Akbar Nazari, Mehdi Rashedi<br>Shahid Bahonar University, Kerman, Iran.

Mathematics Subject Classification: Primery 41A58, Secondary 42C15, 46L99, 47A05.

Keywords: Continuous g-frame, Frame, Hilbert $C^{*}$-module.

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Helix submanifolds in a Lorentzian space 

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#### Abstract

Recently A.J. Di scala and G. Ruiz-Hernandez studied helix submanifolds of Euclidean space $R^{n}$. An interesting motivation for the study of helix hypersurfaces comes from the physics of interfaces of liquid cristals. In this paper we generalize the concept of helix submanifolds to Lorentzian space $L^{n}$ ( vector space $R^{n}$ endowed with the Lorentzian scalar product defined by $\left.\langle X, Y\rangle=x_{1} y_{1}+\ldots+x_{n-1} y_{n-1}-x_{n} y_{n}\right)$. We give two methods for construction of the helix hypersurfaces in Lorentzian space $L^{n}$. Then we obtain a local characterization of all helix hypersurfaces of $L^{n}$. Then by using of eikonal functions as a tool, we study higher codimensional helices in Lorentzian spaces. In fact, we prove a theorem which gives a method to construct helix submanifolds of $L^{n}$. Finally we give the main result of this paper, which gives a necessary and sufficient condition for a manifold $M$ to be immersed as a helix in some Lorentzian space.


Mathematics Subject Classification: 53C30, 57S25.
Keywords: Helix sabmanifolds, Eikonal function, Timelike direction.

[^261]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

## $C$-LIFTING MODULES

M. J. Nematollahi ${ }^{1}$


#### Abstract

A module $M$ is called lifting if every submodule $A$ of $M$ can be written as $A=N \oplus S$ such that $N$ is a direct summand of $M$ and $S \ll M$. Lifting modules generalize projective supplemented modules. We call a module $M, C$-lifting if every submodule $A$ of $M$ can be written as $A=B+C$ such that $B$ is a direct summand of $M$ and $C$ is a cosingular module. We prove that every right $R$-module $M$ is $C$-lifting if and only if every right $R$-module is the sum of an injective module and a cosingular module.


Mathematics Subject Classification: Primary 16D40, Secondary 16D50.
Keywords: lifting module, co-singular module, projective module, injective module.

[^262]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran<br>\section*{GENERALIZED CENTRAL SERIES OF ABELIAN GROUPS}<br>MOHAMMAD NAGHSHINEH, MOHAMMAD REZA R. MOGHADDAM<br>Ferdowsi University of Mashhad, Mashhad, Iran.<br>Islamic Azad University,<br>Mashhad Branch, Iran


#### Abstract

In this paper we try to classify all finite abelian p- groups with multipliers of the same order.


Mathematics Subject Classification: Primary 20D45, 20D25; Secondary 20E34.

Keywords: Autocommutator subgroup, autocentral series, generalized central series.

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran 

# A new Algorithm for computing Sagbi-Gröbner Bases 

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Abdolali Basiri

## Hassan Noori


#### Abstract

This paper introduces a new efficient algorithm for computing SAGBIGr bases for an ideal in a polynomial ring $K\left[x_{1}, \cdots, x_{n}\right]$ whose polynomials are invariant by the action of a finite group. This algorithm computes successive SAGBI-Gr bases degree by degree. The advantage of this algorithm lies in the fact that it replaces the classical polynomial reduction by the simultaneous reduction of several polynomials in order to avoid as much as possible intermediate computations.


Mathematics Subject Classification: 13P10, 13A50.
Keywords: SAGBI-Gröbner bases, Invariant ring.

[^263]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A Calculus and Algebra of Functions Derived from Directed Graph Algebras 

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#### Abstract

Shallon invented a means of deriving algebras from graphs, yielding numerous examples of so-called graph algebras with interesting equational properties. Here we study directed graph algebras, derived from directed graphs in the same way that Shallons undirected graph algebras are derived from graphs. Also we will define a new function on graphic plane, that obtained by Cartesian product of two simple graphs pn, that we will say from now the graph function. Next we will discuss algebraic opratoins on graph functions. Finally we suggest a new algebra, the graph function algebra (KM-Algebra), which is very similar to directed graph algebras.


Mathematics Subject Classification: 20D15; Secondary 20E34;
Keywords: Direct Product, Directed Graph, Graph Function, Shallon Algebra, KM-Algebra

Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Some results on normal Cayley Graph of abelian groups with Valency Six 

Siamak Firouzian

Mostafa Nouri ${ }^{1}$


#### Abstract

A Cayley graph $\Gamma=\operatorname{Cay}(G, S)$ is called normal if the right regular representation of $G$ is a normal subgroup of the automorphism group of $\Gamma$. In this paper, we give a classification of normal connected undirected Cayley graphs on non-cyclic abelian groups of valency 6 .


Mathematics Subject Classification: 05C25,20B25.
Keywords: Cayley graph, Normal edge-transitive, automorphism group.

[^264]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran 

# solving large-scale linear programming problems 

Hamidreza Navidi ${ }^{1}$

Parvin Khosravi


#### Abstract

The aim of this work is to find an exact least 2-norm solution to a primal constrained linear programming problem in the standard form. More over we can generate an exact solution to the dual programming problem using the exact least 2-norm solution to the primal problem. This hybrid algorithm converges to the correct optimal solution independent of the values of the given starting point. Numerical results for a subset of problems from the Netlib collection and a subset of generated large-scale linear programs are given.


Mathematics Subject Classification: Primary 46N10, Secondary 62M45, 90C30.

Keywords: Newton method, strong Wolf conditions, penalty function, least 2-norm solution.

[^265]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> The Annihilating-Product-One side-Ideal graph 

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#### Abstract

For a commutative ring R with identity, the annihilating-ideal graph of $R$, denoted $A G(R)$, is the graph whose vertices are the nonzero annihilating ideal of R with two distinct vertices joined by an edge when the product of the vertices is zero. This article extend the definition of the annihilating ideal graph to non-commutative rings.


Mathematics Subject Classification: 16U99, 05C50, 16S50.
Keywords: The Annihilating-ideal graph, The Annihilating-Product-One side-Ideal graph.

# Perturbations of regular operators and regular $A$-Fredholm operators between Hilbert $C^{*}$-modules Convergent Iterative Scheme 

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#### Abstract

This paper is devoted to study perturbations of regular operators and $A$-Fredholm operators. In particular, we show that a compact perturbation of a regular $A$-Fredholm operator is $A-$ Fredholm.


Mathematics Subject Classification: Primary 74A55, 46L08, Secondary 47L60, 47A53.

Keywords: Hilbert $C^{*}$-modules, regular operator, $A$-Fredholm operators, perturbation.

[^266]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Optimality Conditions on $C *$-Convex sets 

Ismail Nikoufar

Payam noor University,<br>Malekan, Iran.

Mathematics Subject Classification: 47L07
Keywords: $C^{*}$-convex set, $C^{*}$-exterme point, $*$-homomorphism.

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> On the entropy rate of ergodic Markov chains 

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## Nikooravesh ${ }^{1}$

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#### Abstract

In this paper an approximation for entropy rate of an ergodic Markov chain via sample path simulation is calculated. It is demonstrated that the estimated Markov chain entropy rate of a sample path not only converges to the correct entropy rate but also does exponentially faster.


Mathematics Subject Classification: Primary 60J10, Secondary 94A17.

Keywords: ergodic Markov chain, entropy rate, estimation, convergence.

[^267]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran 

# Cesaro Supermodular Order and Archimedean Copula 

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#### Abstract

In This paper, we introduce Cesaro supermodular order. For this new order, we show that it almost fulfills all desirable properties of a multivariate positive dependence order. Finally,we consider different issue related extended Archimedean copula and positive dependence.


Mathematics Subject Classification: 60F15.
Keywords: Positive dependent random vectors, Cesaro supermodular order, Archimedean copula.

[^268]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> on topological interpretation of Baer invariants of groups 

Z. Vasagh ${ }^{1}$

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## B. Mashayekhy

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#### Abstract

In this talk we extend the topological interpretation of nilpotent multipliers of a group $G$ to the Baer invariant of $G$ with respect to an arbitrary variety. Moreover we present a topological proof for the commutativity of Baer invariants with direct limits.


Mathematics Subject Classification: Primary 57M07, Secondary 20J05, 55 U 10 .

Keywords: Baer invariant, Simplicial groups, Moore complex, Variety of groups, Direct limit, Nilpotent multiplier.

[^269]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# A new analytical method to solve Fredholm's integral equations 

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## H. Vosughi ${ }^{1}$

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#### Abstract

This paper shows that the homotopy analysis method (HAM), the well-known method to solve ODEs and PDEs, can be applied as well as to solve linear and nonlinear Fredholm integral equations with high accuracy. Comparison of the present method with Adomian decomposition method (ADM), which is well-known to solve integral equations, reveals that the ADM is only special case of the present method.


Mathematics Subject Classification: 45B05; 45Exx, 45A05.
Keywords: Homotopy analysis method, Fredholm integral equation, Adomian decomposition method

[^270]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Submodules Of Multiplication Modules 

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#### Abstract

Let $R$ be a commutative ring with identity and $M$ be a unitary $R$ module. In this paper we consider only multiplication modules, then investigate some properties of submodules of multiplication modules and find some essential results.


[^271]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# RADIUS OF STARLIKE AND PARTIAL SUM PROPERTY FOR HOLOMORPHIC FUNCTIONS DEFINED BY KOMATU OPERATOR 

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#### Abstract

In this paper we investigate some important properties of a holomorphic functions with negative coefficients by using Komatu operator. We provide necessary and sufficient conditions, radius of starlikeness, convexity and some result for this class.


Mathematics Subject Classification: Primary 30C45.
Keywords: holomorphic, Convex, Starlike functions, Komatu operator.

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Anti-synchronization of the hyperchaotic Qi system and hyperchaotic Lorenz system 

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#### Abstract

This paper investigates the anti-synchronization problem between hyperchaotic Qi system and hyperchatic Lorenz system. Two different anti-synchronization schemes are proposed. Active control is applied when system parameters are known and adaptive control is employed when system parameters are unknown or uncertain. Based on the Lyapunov stability theorem, controllers and update laws of parameters are designed. Numerical simulations are presented to demonstrate the validity and effectiveness of the proposed methods.


Mathematics Subject Classification: Primary 74H65, Secondary 37N35, 37N30.

Keywords: Anti-synchronization, Uncertain parameter, Hyperchaotic Qi system, Hyperchaotic Lorenz system, Active control, Adaptive control.

[^272]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Skew polynomial rings over zip rings 

E. Hashemi ${ }^{1}$


#### Abstract

Faith [?] called a ring $R$ right zip provided that if the right annihilator $r_{R}(X)$ of a subset $X$ of $R$ is zero, then $r_{R}(Y)=0$ for a finite subset $Y \subseteq X$. In this note first we show that if $R$ is a reversible $(\alpha, \delta)$ compatible ring, then $R$ is right ( $\alpha, \delta$ )-McCoy. Then we prove that $R$ is right zip if and only if $R[x ; \alpha, \delta]$ is right zip, when $R$ is reversible $(\alpha, \delta)$ compatible. Also we give some examples of ( $\alpha, \delta$ )-compatible rings.


Mathematics Subject Classification: Primary 16D25, 16D60, Secondary 16S34, 16S36.

Keywords: Zip rings, McCoy rings, reversible rings.

[^273]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> solution of nonlinear cubic-quintic Duffing using Homotopy analysis method(HAM) 

M. Hashemi ${ }^{1}$<br>F. Hemati

A. Hashemi


#### Abstract

In this paper, we use HAM for periodic solution of nonlinear cubicquintic Duffing. This method help us to obtain frequency in the form of approximation series of convergence control parameter $(\hbar)$.

Mathematics Subject Classification: Primary 00X00; Secondary 00X00,


 00X00.Keywords: Homotopy analysis method, nonlinear problems.

[^274]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Minimizing of energy integral of fractional order via interpolation 

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#### Abstract

We consider existence of a unique surface $f:[0,1]^{3} \rightarrow \Re$ such that it passes some arbitrary points on the unit cubic domain and minimizes the energy integral of fractional order on $[0,1]^{3}$. The procedure of finding the solution will also be shown. This generalizes the proposed methods of $[1,4]$.


Mathematics Subject Classification: Primary 41A50, Secondary 42A10, 42A15.

Keywords: Fourier series, Energy integral, Interpolation, Hilbert spaces.

[^275]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Orthogonal Spline Collocation for Nonlinear Elliptic Boundary Value Problems 

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## R.Yarmohamadi ${ }^{1}$

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#### Abstract

In this study, a general nonlinear elliptic differential equation is considered. The orthogonal spline collocation (OSC) method is used to approximate the solution. At first collocating the differential equation at the so-called Gaussian points then replacing in the equation with a Hermite bicubic spline that vanishes on $\partial \Omega$. The basic advantage of spline collocation methods in comparison with finite element Galerkin methods is the computation of the coefficients of the algebraic equations is faster since no quadratures need to be evaluated. The OSC methods for linear boundary value problems provide optimal order error estimates.


Keywords: Orthogonal spline collocation, Boundary value problem, Gaussian quadrature.

[^276]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Some results on the bipartite edge frustration of graphs 

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#### Abstract

The smallest number of edges that have to be deleted from a graph $G$ to obtain a bipartite spanning subgraph is called the bipartite edge frustration of $G$ and denoted by $\varphi(G)$. In this paper we obtain some new results of this quantity.


Mathematics Subject Classification: 05C76, 09E10.

Keywords: Bipartite graph, bipartite edge frustration.

[^277]
# A weighted algorithm based on variational iteration method for identifying heat transfer coefficient 

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#### Abstract

In this paper, we consider an inverse problem of heat equation with Robin boundary condition for identifying heat transfer coefficient. The numerical solution is developed by using a weighted algorithm based on variational iteration method. This method uses initial and boundary conditions simultaneously and effectively for constructing the solution. Using this method a rapid convergent sequence can be obtained which tends to the exact solution of the problem.


Mathematics Subject Classification: Primary 35K05, Secondary 80A23, 35A15.

Keywords: Heat transfer coefficient, Inverse problems, Variational iteration method.

[^278]
# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran 

# PRIME M-IDEALS AND M-PRIME SUBMODULES 

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#### Abstract

Let $M$ be a fixed left $R$-module. For a left $R$-module $X$, we introduce the notion of $M$-prime (resp. $M$-semiprime) submodule of $X$ such that in the case $M=R$, which coincides with prime (resp. semiprime) submodule of $X$. Other concepts encountered in the general theory are $M$ - $m$-system sets, $M$ - $n$-system sets, $M$-prime radical and M-Baer's lower nilradical of modules. Relationships between these concepts and basic properties are established. In particular, we identify certain submodules of $M$ (called "prime $M$-ideals") that play a role analogous to that of prime (two-sided) ideals in the ring $R$. Also, we investigate the prime $M$-ideals, $M$-prime submodules and $M$-prime radical of Artinian modules.


Mathematics Subject Classification: Primary 16D80, Secondary 16D99.
Keywords: Prime $M$-ideal; $M$-prime submodule; $M$-m-system set.

[^279]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Comparison the methods of gauss-quadrature for approximating of integrals involving the Gegenbauer weight-function 

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#### Abstract

In this paper, we try by using gauss quadrature formula on the integrals as follows : $$
\begin{equation*} \int_{a}^{b}\left(1-x^{2}\right)^{\lambda-\frac{1}{2}} f(x) d x \tag{1} \end{equation*}
$$ where $\left(1-x^{2}\right)^{\lambda-\frac{1}{2}}$, with $\lambda>-\frac{1}{2}$, is the Gegenbauer weight-function, compare the numerical results with Clenshaw - Curtis quadrature [2]. The numerical results illustrate the gauss quadratures are better than Clenshaw - Curtis quadrature [2].


[^280]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# Approximate identity in abstract Segal algebras the Gegenbauer weight-function 

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A. Yousofzadeh ${ }^{1}$<br>Department of Mathematics, Karaj<br>Branch, Islamic Azad University, Karaj, Iran.


#### Abstract

Let $G$ be a locally compact group. It has been proved that an abstract Segal algebra with respect to $L^{1}(G)$ admits a bounded approximate identity if and only if it is a Segal algebra. Hear, we investigate when an abstract Segal algebra with respect to an arbitrary Banach algebra admits a bounded approximate identity.


Mathematics Subject Classification: Primary 46H25, Secondary 43A15.
Keywords: Banach algebras, bounded approximate identities, Segal algebras.

[^281]Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

# SOME PROPERTIES OF HOSOYA AND MERRIFIELD-SIMMONS INDICES OF A GIVEN GRAPH 

KH.FATHALIKHANI

## H.YOUSEFI-AZARI

Tehran University, Tehran, Iran.


#### Abstract

The hosoya index of a graph $\mathrm{G}, \mathrm{Z}(\mathrm{G})$,is defined as the total number of its matchings,while the Merrifield-Simmons in- dex, $\mathrm{i}(\mathrm{G})$,is the total number of independent sets of G.In this pa- per,first we calculate the hosoya index of a special group of trees called'caterpillars'and then find a lower bound for $\mathrm{i}(\mathrm{G})$.Finally, we gain some relations between these two indices which are based on a few number of graph functions.


Keywords: hosoya index, Merrifield-Simmons index, k-vertex color- ing, lexicographic product, strong product.

Foreign Speakers

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Differential Subordination For a Class of Univalent Functions 

S. Gholizadeh Hamidi and S. Abd Halim

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Malaysia

## On Free Action of Semiprime Rings

Mehsin Jabel Atteya and Dalal Ibraheem Resan
Department of Mathematics
Al-Mustansiriyah University-College of Education
Iraq

## The Numerical Solution of Partial differential Algebra Equations (PDEs) By Multivariate Pade Approximation

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Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference<br>12-15 September 2010, University of Urmia, Urmia-Iran

## Investigation Shape Optimization Problem Using Neural Networks

C. I. Zeynaloy, A. A. Nifityev and K. Majidzadeh<br>Deprtment of Mathematics, Baki State University,

## On Generalized Derivations With Commutativity of Semiprime Rings

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Department of Mathematics
Al-Mustansiriyah University-College of Education Iraq

## Dual Generalized Quaternions in Spatial KInematics

M. Jafari and Y. Yayli

Deprtment of Mathematics, Ankara University, Turkey

# Abstract of $41^{\text {st }}$ Annual Iranian Mathematics Conference <br> 12-15 September 2010, University of Urmia, Urmia-Iran <br> Compact And Cocompact Lattice And m-Adictopology 

A. Molkhasi and Mamedov

## List of Participants

| 1 | Abbasi | Somayeh | * |
| :---: | :---: | :---: | :---: |
| 2 | Abbasi | Naser | * |
| 3 | Abbasi | Mahdieh | * |
| 4 | Abbasi Shokat Abad | Masoumeh | * |
| 5 | Abd Halim | Suzeini | * |
| 6 | Abdolali Zadeh | Yousef |  |
| 7 | Abdollah Pour | Mohammad Reza | * |
| 8 | Abdollahi | Alireza |  |
| 9 | Abedi Zadeh | Fahimeh | * |
| 10 | Abkar | Ali |  |
| 11 | AboAli | Irandokht | * |
| 12 | Abolfathi | Mohammad Ali | * |
| 13 | Abrishami Moghaddam | Majid | * |
| 14 | Adib | Majid | * |
| 15 | Adib | Marjan | * |
| 16 | Adl Abad | Ali |  |
| 17 | Aghalari | Rasul | * |
| 18 | Aghashiri | Somayeh | * |
| 19 | Aghayan | Masoud | * |
| 20 | Aghdasi | Elham | * |
| 21 | Ahangari | Fatemeh | * |
| 22 | Ahmadi | Ghasem | * |
| 23 | Ahmadi | Parviz | * |
| 24 | Ahmadi Balf | Fatemeh | * |
| 25 | Ahmadi Dalir | Karim | * |
| 26 | Ahmadi Ladari | Ali Reza | * |
| 27 | Ahmadi Tarakameh | Ali | * |
| 28 | Ahmadi Varzani | Zahra | * |
| 29 | Ahmadian | Davood | * |
| 30 | Aim Pour |  | * |
| 31 | Akbari | Majid |  |
| 32 | Akbari | Zohreh | * |
| 33 | Akbari Tootkaboni | Mohammad | * |
| 34 | Akbarifard Dastghiri | Farideh | * |
| 35 | Akhavan Ghasabzadeh | Fahimeh | * |
| 36 | Akhondi Khalkhili | Hasan | * |
| 37 | Alaie | Zakieh |  |
| 38 | Alavi | Roghiyeh | * |
| 39 | Aleteymour | Samira |  |
| 40 | Alhivaz |  | * |
| 41 | Ali Akbari |  | * |
| 42 | Ali Khani | Saied |  |
| 43 | Ali Mohammadi | Mohsen | * |
| 44 | Ali Mohammadi | Roshanak | * |


| 45 | Ali Mohammadi | Davood | * |
| :---: | :---: | :---: | :---: |
| 46 | Ali Moradi | Mohammad Reza | * |
| 47 | Ali Niyaie Fard | Farid | * |
| 48 | Ali Panah | Amjad | * |
| 49 | Ali Pour Yengeje | Amir | * |
| 50 | Ali Reza Mirhosseini | Marziyeh | * |
| 51 | Alizadeh | Behrooz |  |
| 52 | Aman | Masoud | * |
| 53 | Amin Ghafari | Mina | * |
| 54 | Amini | Behnam | * |
| 55 | Amini Dehkharghani | Behnam | * |
| 56 | Aminkhah | Mozhgan | * |
| 57 | Amiri | Habib | * |
| 58 | Amiri | Rama | * |
| 59 | Amiri Bashli | Meysam | * |
| 60 | Amiri Bideshki | Mohsen | * |
| 61 | Amirshekari | Zeynab | * |
| 62 | Amjadi | Hanieh |  |
| 63 | Amoozegar | Samaneh | * |
| 64 | Amoozgar | Tayebeh | * |
| 65 | Amyari | Maryam | * |
| 66 | Ansar | Kheironnesa | * |
| 67 | Anvarzade Maraghi | Amin |  |
| 68 | Arab Tash | Mostafa | * |
| 69 | Arasteh | Fatemeh | * |
| 70 | Ardin | Nadia | * |
| 71 | Arefi Jamal | Ali Akbar | * |
| 72 | Ariannezhad | Masoud | * |
| 73 | Arjmandfar | Abbas | * |
| 74 | Arjmandinia | Parviz |  |
| 75 | Armandnezhad | Ali | * |
| 76 | Armanfar | Samaneh | * |
| 77 | Asadi | Fatemeh | * |
| 78 | Asadi | Mohammad Ali | * |
| 79 | Asadi | Reza |  |
| 80 | Asadi Golzar | Ziba | * |
| 81 | Asgari | Mohammad Sadegh |  |
| 82 | Asghari | Mohammad Sadegh | * |
| 83 | Asghari | Mohsen |  |
| 84 | Asgharzadeh | Akbar | * |
| 85 | Asgharzadeh | Mohsen | * |
| 86 | Ashiani | Akram | * |
| 87 | Ashouri | Fatemeh | * |
| 88 | Ashrafi | Nahid | * |


| 89 | Ashri | Siamak | * |
| :---: | :---: | :---: | :---: |
| 90 | Atabaki | Motahhareh |  |
| 91 | Ataei | Mohammad Javad | * |
| 92 | Atari | Maryam | * |
| 93 | Atteya | Mehsin Jabel | * |
| 94 | Aval | Fatemeh |  |
| 95 | Avaz Zade | Zakiyeh | * |
| 96 | Avaz Zade | Zeinab | * |
| 97 | Azad | Azizollah | * |
| 98 | Azad | Kobra |  |
| 99 | Azadi | Ghodratollah | * |
| 100 | Azami | Jafar | * |
| 101 | Azanchiler | Habib | * |
| 102 | Azarpanah | Fariborz | * |
| 103 | Azhdari | Parvin | * |
| 104 | Azim Pour | Sohrab |  |
| 105 | Azimi Dezfuli | Maryam |  |
| 106 | Azizpour | Esmaeil | * |
| 107 | Baba Ahmadi Milani | Zahra | * |
| 108 | Babaie | Ameneh | * |
| 109 | Babazadeh | Elnaz | * |
| 110 | Babelian | Esmaeil |  |
| 111 | Bagheri | Ameneh | * |
| 112 | Bagheri | Saied | * |
| 113 | Bagheri Kholenjani | Nayereh | * |
| 114 | Bagherian | Javad | * |
| 115 | Baghershahi | Narges | * |
| 116 | Bahrami | Mohammad | * |
| 117 | Bahrami Ziabari | Reihaneh | * |
| 118 | Bakefayat | Zahra | * |
| 119 | Bakhshande | Roohollah | * |
| 120 | Bakic | Damir | * |
| 121 | Bandpei | Zeynab | * |
| 122 | Barani | Ali | * |
| 123 | Barooghi Bonab | Fahimeh | * |
| 124 | Barsagh | Zohreh |  |
| 125 | Barzgar | Fatemeh | * |
| 126 | Bazargan Lari | Abdolreza | * |
| 127 | Bazyar | Mohammad | * |
| 128 | Bazyari | Meysam | * |
| 129 | Behboudi AsI | Manouchehr | * |
| 130 | Behravesh | Houshang | * |
| 131 | Behzad | Mehdi |  |
| 132 | Behzadi | Ali |  |


| 133 | Beigi Rizi | Zahra | * |
| :---: | :---: | :---: | :---: |
| 134 | Beitollahi | Arman | * |
| 135 | Biglari Gholilou | Fahimeh |  |
| 136 | Bohluli | Somayeh |  |
| 137 | Borhanifar | Abdollah |  |
| 138 | Bouzhabadi | Reza | * |
| 139 | Breaz | Valer Daniel |  |
| 140 | Celik | Ercan | * |
| 141 | Chakoshi | Mahnaz | * |
| 142 | Dadipour | Farzad | * |
| 143 | Damirchi | Javad | * |
| 144 | Dana | Mansour |  |
| 145 | Danaei | Reza | * |
| 146 | Daneshvar | Sahand | * |
| 147 | Darabi | Ali | * |
| 148 | Darabi | Bayaz | * |
| 149 | Darania | Parviz |  |
| 150 | Darvishzadeh | Mohammad | * |
| 151 | Darzi | Rahamt | * |
| 152 | Dastjerdi | Mohammad Taghi | * |
| 153 | Davoodi Darzi | Mohammad |  |
| 154 | Davoodi Jedi | Narges | * |
| 155 | Dehghan | Hosein |  |
| 156 | Dehghan | Mohammad Ali | * |
| 157 | Dehghan Harati | Ali | * |
| 158 | Dehghani Darmian | Mehdi | * |
| 159 | Dehghani Tazekand | Eisa | * |
| 160 | Dibachi | Hosein | * |
| 161 | Dinarvandi | Somayeh | * |
| 162 | Dorri | Fatemeh | * |
| 163 | Dujella | Andre | * |
| 164 | Ebadian | Ali | * |
| 165 | Ebrahimi | Akbar |  |
| 166 | Ebrahimi | Faezeh | * |
| 167 | Ebrahimi | Sara |  |
| 168 | Ebrahimi | Sepideh | * |
| 169 | Ebrahimi Vishki | Hamid Reza | * |
| 170 | Ebrahimikhah | Hadi | * |
| 171 | Edalat Zadeh | Behrooz | * |
| 172 | Eghdami | Hosein | * |
| 173 | Emami | Mozhgan | * |
| 174 | Eram | Zahra | * |
| 175 | Esfahani | Amin | * |
| 176 | Eskandari | Khadijeh |  |


| 177 | Eskandari | Rasul | * |
| :---: | :---: | :---: | :---: |
| 178 | Eskandarzadeh | Maryam | * |
| 179 | Eslahchi | Mohammad Reza | * |
| 180 | Eslami | Zeynab |  |
| 181 | Eslamian | Mohammad | * |
| 182 | Esmaeili | Roghayeh | * |
| 183 | Esmaeili Fallah | Hajar | * |
| 184 | Etebar |  | * |
| 185 | Etefagh | Mina |  |
| 186 | Ezati | Reza | * |
| 187 | Fadayi | Jasem | * |
| 188 | Fahimi | Hamed | * |
| 189 | Fakhari | Elham | * |
| 190 | Fakharzadeh Jahromi | Ali Reza | * |
| 191 | Fakheri | Siyamak |  |
| 192 | Falah Eslamluo | Haniyeh | * |
| 193 | Falahati | S | * |
| 194 | Falahati Mrost | Somayeh |  |
| 195 | Falati | Mehdi | * |
| 196 | Fallah Gol |  | * |
| 197 | Faraj Zadeh | Ali | * |
| 198 | Faramarzi Sales | Asadollah | * |
| 199 | Farhad Toski | Zahra | * |
| 200 | Fariborzi Araghi | M | * |
| 201 | Farnoosh | Rahman | * |
| 202 | Farokhi Hersini | Parvaneh | * |
| 203 | Farshbaf Moghimi | Mohammad Bagher |  |
| 204 | Farzi | Maliheh | * |
| 205 | Fathali | Jafar | * |
| 206 | Fathali Khani | Khadijeh |  |
| 207 | Fayaz Behroz | Seyedeh Robab |  |
| 208 | Fayaz Movaghar | Afshin | * |
| 209 | Fazeli | Somayeh | * |
| 210 | Feyzabadi | Naser | * |
| 211 | Feyzollahi Onsorodi | Ebrahim | * |
| 212 | Foladi | Hamid | * |
| 213 | Forogh | Sodabeh |  |
| 214 | Forozanfar | Farzaneh |  |
| 215 | Garshasbi | Morteza |  |
| 216 | Gashoul | Zahra | * |
| 217 | Ghadiri Anari | Maryam | * |
| 218 | Ghaemi | Mohammad Reza | * |
| 219 | Ghafouri | Asiyeh | * |
| 220 | Ghahremani | Hougher | * |


| 221 | Ghanbari | Kazem | * |
| :---: | :---: | :---: | :---: |
| 222 | Ghani Fara Shahi | Arash | * |
| 223 | Gharailoo | Zahra |  |
| 224 | Ghasem Nejad |  | * |
| 225 | Ghasemi | Maryam |  |
| 226 | Ghasemi | Mohsen | * |
| 227 | Ghasemi Honari | Taher | * |
| 228 | Ghasemi Kamalvand | Mojtaba | * |
| 229 | Ghasemiyan | Elham | * |
| 230 | Ghayekhlou | Somayeh | * |
| 231 | Ghazanfari | Bahman | * |
| 232 | Ghezelbash | Fatemeh | * |
| 233 | Ghobadi pour | Norouz | * |
| 234 | Gholam Zadeh | S. Mohammad |  |
| 235 | Gholami | Gholam Hosein | * |
| 236 | Gholami Dokht Haroni | Somayeh |  |
| 237 | Gholi Nejad Malekshah | Shaban Ali |  |
| 238 | Gholizadeh Hamidi | S | * |
| 239 | Ghorban Zadehivari | Saba |  |
| 240 | Ghorbani | Mohammad Reza | * |
| 241 | Ghorbani | Shokofeh | * |
| 242 | Ghorbani | Zahra | * |
| 243 | Ghorbani | Maryam | * |
| 244 | Gilasi | Farzaneh | * |
| 245 | Golchin | Akbar | * |
| 246 | Golzarpour | Javad | * |
| 247 | Habibi | Parastoo | * |
| 248 | Hadadi | M. R | * |
| 249 | Hadadi Fard | Fazel | * |
| 250 | Hafezieh | Roghayeh | * |
| 251 | Haghighatnia | Parisa | * |
| 252 | Haghighi | Ahmad Reza | * |
| 253 | Haj Abotalebi | Narges | * |
| 254 | Haj Sadeghi | Maryam | * |
| 255 | Haji Badali | Ali | * |
| 256 | Haji Shabani | Mahmood | * |
| 257 | Hakamipour | Noushin | * |
| 258 | Hakimi Parouch | Mahdieh | * |
| 259 | Halimi | Mohammad | * |
| 260 | Hamidi | Safoura |  |
| 261 | Hamzeh Nezhad | Mehdi | * |
| 262 | Harizavi | Habib | * |
| 263 | Hasani | Hosein | * |
| 264 | Hasani | Khadijeh | * |


| 265 | Hasanzadeh | Fatemeh | * |
| :---: | :---: | :---: | :---: |
| 266 | Hashemi | Ebrahim | * |
| 267 | Hashemi Garmdarreh | S. Mohammad Jafar | * |
| 268 | Hazrati | Ali Reza |  |
| 269 | Heidari | Mohammad Taghi | * |
| 270 | Heidari | Zohreh | * |
| 271 | Hejazi | S. Reza | * |
| 272 | Hemmati |  | * |
| 273 | Hemmatian Dehkordi | Parisa | * |
| 274 | Hoseini | Mohammad Hossein | * |
| 275 | Hoseini | S. Mohammad | * |
| 276 | Hoseini | S. Sara | * |
| 277 | Hoseini Darbarzi | S. Ghasem | * |
| 278 | Hoseinpouri | Mehdi | * |
| 279 | Houmi | Behnaz |  |
| 280 | Houshyar Ghahremanlou | Noushin | * |
| 281 | Houshyar Ghahremanlou | Kheirollah |  |
| 282 | Ilaghi Hoseini | Azadeh | * |
| 283 | Irandoust | Safar | * |
| 284 | Irandousti |  | * |
| 285 | Irani | Yavar | * |
| 286 | Iranmanesh | Anis | * |
| 287 | Iranmanesh | Farzad |  |
| 288 | Iranmanesh | Mehdi | * |
| 289 | Iranmanesh | Mohammad Ali |  |
| 290 | Iranpanah | Nasrollah | * |
| 291 | Isvand | Davood | * |
| 292 | Ivaz | Karim |  |
| 293 | Izadi | Javad | * |
| 294 | Izadian | Jalaleddin | * |
| 295 | Jabbari | Mohammad |  |
| 296 | Jabbari | Mousa | * |
| 297 | Jabbarzadeh | Mohammad Reza | * |
| 298 | Jaf | Farzaneh | * |
| 299 | Jafari | Fatemeh | * |
| 300 | Jafari | Hosein | * |
| 301 | Jafari | Mehdi | * |
| 302 | Jafari | Zeynab | * |
| 303 | Jafari | Zohreh | * |
| 304 | Jafari Khaledi | Majid | * |
| 305 | Jafarian Amiri | Seyed Majid | * |
| 306 | Jafariani | Somayeh | * |
| 307 | Jahan Panah Bavaryani | Sirus |  |
| 308 | Jahed Hour | Ramin | * |


| 309 | Jahedi | Khadijeh | * |
| :---: | :---: | :---: | :---: |
| 310 | Jahedi | Sedigheh |  |
| 311 | Jalal Zadeh | Leila | * |
| 312 | Jalali Pour | Somayeh | * |
| 313 | Jalalian | Sahar | * |
| 314 | Jalilian | Reza | * |
| 315 | Jamali | Hasan | * |
| 316 | Jan Nesari |  | * |
| 317 | Javani | Kobra |  |
| 318 | Javanmard | Farshideh | * |
| 319 | Javanmardi | Sara | * |
| 320 | Jelodari | Mohammad |  |
| 321 | Jodeiri Akbarfam | Ali Asghar | * |
| 322 | Jokar | Asghar | * |
| 323 | Jokar | Mahmood | * |
| 324 | Jokar | Zahra | * |
| 325 | Kafash Dost | Somayeh | * |
| 326 | Kamalgharibi | Hadiseh | * |
| 327 | Kamari | Osman | * |
| 328 | Kamel Mir Mostafayi | Ali Reza | * |
| 329 | Kamrani | Saeid |  |
| 330 | Kamyabi |  |  |
| 331 | Kamyabi Gol | Robab | * |
| 332 | Karamali | Gholamreza | * |
| 333 | Karamoz | Neda | * |
| 334 | Kardost | Mobina | * |
| 335 | Karimi | Kobra | * |
| 336 | Karimi Jafar beighlou | Saied | * |
| 337 | Karimiyan | Saleh | * |
| 338 | Kashfi | Mahnaz | * |
| 339 | Kazemi | Iraj | * |
| 340 | Kazemi | Mohammad Bagher |  |
| 341 | Kazemi | Manoochehr | * |
| 342 | Kazemi Blgshir | Mohammad Bagher | * |
| 343 | Kazemi Fard | Ahmad | * |
| 344 | Kazemi Pileh Drgh | Adel |  |
| 345 | Keighobadi | Somayeh | * |
| 346 | Keramat lou | Mahmood | * |
| 347 | Keshavarz Kohjerdi | Fatemeh |  |
| 348 | Khademi | Ali | * |
| 349 | Khademi | S. Nematollah | * |
| 350 | Khademlou | S | * |
| 351 | Khaki | Raheleh | * |
| 352 | Khalili | Jamal | * |


| 353 | Khalili | Valiollah | * |
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| 354 | Khalili | Yaser | * |
| 355 | Khalili | Najib Agha |  |
| 356 | Khalili | Zakieh | * |
| 357 | Khalilzadeh | Rasul |  |
| 358 | Khame Chi | Pouyan | * |
| 359 | Khani | Ali | * |
| 360 | Khanjani Shiraz | Rashed | * |
| 361 | Khanpouri | Mohammad |  |
| 362 | Khasteh | Abouzar | * |
| 363 | Khatib Zadeh | Hadi | * |
| 364 | Khatibi Aghda | Davood | * |
| 365 | Khazaeili | Mohammad | * |
| 366 | Khazal | Mohammad |  |
| 367 | Kheibari | Samad | * |
| 368 | Kheiri | Hosein | * |
| 369 | Khodadadi | Roya |  |
| 370 | Khojali | Ahmad | * |
| 371 | Khojaste Salkouyeh | Davood | * |
| 372 | Khosh Nomian | Azam |  |
| 373 | Khoshnam | Foad | * |
| 374 | Khoshnevisan | Azam |  |
| 375 | Khosravi | Somayeh | * |
| 376 | Kiakajouri | Sara | * |
| 377 | Komeil | Ali Reza |  |
| 378 | Komeili | Mojtaba |  |
| 379 | Kouhi | Maryam | * |
| 380 | Kuzucuoglu | Mahmut | * |
| 381 | Lalehzari | Reyhaneh | * |
| 382 | Lali dastjerdi | Hojatollah | * |
| 383 | Lameei | Sanaz | * |
| 384 | Lashkaripour | Rahmatollah | * |
| 385 | Latifi | Ali |  |
| 386 | Latifi | Dariush | * |
| 387 | Latifi | Masoud |  |
| 388 | Loghmani | B | * |
| 389 | Lotfi Parsa | Morteza | * |
| 390 | Mafi | Amir | * |
| 391 | Maghsudi | Somayeh | * |
| 392 | Mahdavi Amiri | Nezameddin | * |
| 393 | Mahdieh Najaf Abadi | Fereshteh | * |
| 394 | Mahmood Fakhe | Souran | * |
| 395 | Mahmoodi | Eisa | * |
| 396 | Mahmoodi | S. Mohammad | * |


| 397 | Mahmoodi | Yaghub |  |
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| 398 | Mahmoodian | S.Ebadollah | * |
| 399 | Mahmoodian | Somayeh | * |
| 400 | Mahmoodvand | Rahim | * |
| 401 | Majedi | Somayeh |  |
| 402 | Majidian | Hasan | * |
| 403 | MajidZadeh | K | * |
| 404 | Malek Ghayeni | Farid(Mohammad) | * |
| 405 | Maleki | Manzar | * |
| 406 | Maleknezhad | Khosro | * |
| 407 | Mamedov |  | * |
| 408 | Mansuri Kaleibari | Mozhgan | * |
| 409 | Mashhadi | Samaneh | * |
| 410 | Mashhoudi | Shahed | * |
| 411 | Masoudipor | Najmeh | * |
| 412 | Masoumi | Mohammad Hossein | * |
| 413 | Masouri | Zahra | * |
| 414 | Masroori | Naser | * |
| 415 | Matinfar | Mashallah | * |
| 416 | Mazandarani | Mehran | * |
| 417 | Mazloumi | Zahra | * |
| 418 | Medghalchi | Ali Reza |  |
| 419 | Mehdi | Eisa |  |
| 420 | Mehdipor | Ali |  |
| 421 | Mehdipour | Mohammad Javad | * |
| 422 | Mehdipour Shirayeh | Ali | * |
| 423 | Mehrang | Shiva |  |
| 424 | Mehrdonya | Iraj |  |
| 425 | Mehrjouie | Ali |  |
| 426 | Mehrshad | Saeid | * |
| 427 | Mehryar | Fatemeh | * |
| 428 | Memarzadeh Kermani | Maryam | * |
| 429 | Merikh Bayat | Farshad | * |
| 430 | Mir Ali Ashrafi | Zeynab | * |
| 431 | Mirhossein Khani | Ghasem | * |
| 432 | Miri | Mohammad Reza | * |
| 433 | Mirshafaei | Seyed Reza | * |
| 434 | Mirzapour | Farzollah | * |
| 435 | Modallelian | Malihe | * |
| 436 | Moeini | Maryam | * |
| 437 | Moeini | Mitra | * |
| 438 | Mofidi | Hamid Reza | * |
| 439 | Moghaddam Far | Ali Reza | * |
| 440 | Moghaddasi | Gholam Reza | * |


| 441 | Moghimi | Mohammad Bagher | * |
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| 442 | Moghimian | Mahdieh | * |
| 443 | Mohammadalizadeh | Benyamin | * |
| 444 | Mohammadalizadeh | Roohollah | * |
| 445 | Mohammadi | Eisa | * |
| 446 | Mohammadi | Fakhroddin | * |
| 447 | Mohammadi | Nasrin | * |
| 448 | Mohammadi | Samaneh | * |
| 449 | Mohammadi Hasanabadi | Mozhgan |  |
| 450 | Mohammadi Mosannan | Elham |  |
| 451 | Mohammadi Motlagh | Nader |  |
| 452 | Mohammadi Nezhad | Haj Mohammad | * |
| 453 | Mohammadikhah | Sadegh | * |
| 454 | Mohammadpour | Adel | * |
| 455 | Mohammadpour | Afsaneh | * |
| 456 | Mohammadpour | Mozhgan |  |
| 457 | Mohammadpouri | Akram |  |
| 458 | Mohammadzadeh | Ahmad |  |
| 459 | Mohammadzadehfar | Samaneh |  |
| 460 | Mohebi | Hosein | * |
| 461 | Mohsen Yari | Ali |  |
| 462 | Mohtasham | Somayeh | * |
| 463 | Mokarram | Reza | * |
| 464 | Mokhtari Aghdam | Payam | * |
| 465 | Molaei | Habib | * |
| 466 | Molkhasi | A | * |
| 467 | Molla Haji Aghaie | Mohsen | * |
| 468 | Momeni Masuleh | Seyed Hojatollah | * |
| 469 | Moradi | Marzieh | * |
| 470 | Moradi | Mohammad Reza | * |
| 471 | Moradi | Sirus | * |
| 472 | Morassaei | Ali | * |
| 473 | Motamedi Motlagh | Nader | * |
| 474 | Motiei | Samaneh | * |
| 475 | Musapour | Mansureh | * |
| 476 | Musavi | Nazila |  |
| 477 | Musavi | Hamid | * |
| 478 | Musavi Samar | Mohammad |  |
| 479 | Musazadeh | Kamran | * |
| 480 | Nabardi | Kamran | * |
| 481 | Nabati | Parisa | * |
| 482 | Nabavi Sales | Seyed Sadegh | * |
| 483 | Naderi | Bashir | * |
| 484 | Naderi | Masoumeh |  |


| 485 | Naghshineh Fard | Mohammad | * |
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| 486 | Najafalizadeh | Saeid | * |
| 487 | Najafi | Esmaeil | * |
| 488 | Najafi | Marzieh | * |
| 489 | Najafi | Mohaddeseh | * |
| 490 | Najafi | Seyed Mojtaba | * |
| 491 | Najafi Dolatabadi | Ardavan | * |
| 492 | Najafi Saghezchi | Behzad | * |
| 493 | Najafian | Seyed Mohsen | * |
| 494 | Najafzadeh | Shahram | * |
| 495 | Najati | Abbas | * |
| 496 | Namjo | Mehran | * |
| 497 | Namvari Laleh | Roghayeh |  |
| 498 | Narimani | Ghasem | * |
| 499 | Naserian | Javad | * |
| 500 | Nasiri | Fahimeh |  |
| 501 | Nasiri | Jila | * |
| 502 | Nasrabadi | Mohammad Mehdi | * |
| 503 | Navidi | Hamid Reza | * |
| 504 | Nazari | Akbar | * |
| 505 | Nazari | Ali Mohammad | * |
| 506 | Nazari | Mahboubeh | * |
| 507 | Nazari | Mehdi | * |
| 508 | Nazemi | Seyed Zahra | * |
| 509 | Nazemian | Javad | * |
| 510 | Nematollahi | Mohammad Javad | * |
| 511 | Nezamdoust | Sajjad |  |
| 512 | Niftiyev | A. A. | * |
| 513 | Nikoofar | Esmaeil | * |
| 514 | Nikooravesh | Zohreh | * |
| 515 | Nikouie | Moharram | * |
| 516 | Nili Sani | Hamid Reza |  |
| 517 | Nobari | Elham | * |
| 518 | Nosrati Sahlan | Monireh | * |
| 519 | Nourbakhsh | Mohammad Reza | * |
| 520 | Nouri | Hasan | * |
| 521 | Nouri | Mahdieh | * |
| 522 | Nouri | Zahra | * |
| 523 | Nouri Joybari | Mostafa | * |
| 524 | Nozari | Azam | * |
| 525 | Nozari rad | Razieh | * |
| 526 | Omidi | G. R | * |
| 527 | Omoomi | Behnaz |  |
| 528 | Oskuie | Elnaz | * |


| 529 | Ostadbashi | Saeid | * | 573 | Ravaie | Soheila | * |
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| 530 | Ostadzad | Mohammad Hossein | * | 574 | Razaghi | Fatemeh |  |
| 531 | Ostovar | Aydin | * | 575 | Razavi | S. Hamed |  |
| 532 | Pahlusai | Behnaz |  | 576 | Razavi | Asadollah | * |
| 533 | Paknafs | Ali |  | 577 | Refahi Sheikhani | Amir Hossein | * |
| 534 | Panahi | Hanieh | * | 578 | Reihani Ardabili | Parastoo | * |
| 535 | Panahi | Mehdi | * | 579 | Resan | Dalal ibrahim | * |
| 536 | Panahi | Pari | * | 580 | Reza Ali | Esmaeil |  |
| 537 | Parastar | Hajar |  | 581 | Rezaei | Saber | * |
| 538 | Parvaneh | Foroud | * | 582 | Rezaei | Zeynab | * |
| 539 | Parvardeh | Afshin | * | 583 | Rezaei | Bahman | * |
| 540 | Paryab | Khalil | * | 584 | Rezaei Kamani |  | * |
| 541 | Pazhouh | Behrouz |  | 585 | Rezvan | Mohammad Reza | * |
| 542 | Pidni | Fariba |  | 586 | Rezvani | Zakieh | * |
| 543 | Pir Asghari | M | * | 587 | Rishi Tusi | Reyhaneh |  |
| 544 | Pirmohammadi | Gholamreza | * | 588 | Roohani Nasab | Nahid |  |
| 545 | Pishbin | Marjan | * | 589 | Roomi | Vahid | * |
| 546 | Pour Amian | Ahmad Reza |  | 590 | Roosta Pisheh | Pouria |  |
| 547 | Pour Hoseini | Maryam | * | 591 | Rostami Bashmani | Majid | * |
| 548 | Pour Salavati | Nasrollah | * | 592 | Saberi Najafi | Hashem | * |
| 549 | Pourmahmoud | Jafar | * | 593 | Saberi Nick | M | * |
| 550 | Pourvali | Zahra | * | 594 | Sabet Ghadam | Fatemeh | * |
| 551 | Rabani | Morteza |  | 595 | Sabori | Sara | * |
| 552 | Rabiei | Ghafar |  | 596 | Saddedin | Seifollah |  |
| 553 | Raei | Marzieh |  | 597 | Sadeghi | Hiro |  |
| 554 | Raeiat Pisheh | Shahram | * | 598 | Sadeghi | Akram |  |
| 555 | Rafeie Rad | M | * | 599 | Sadigh Behzadi |  | * |
| 556 | Rafiei | Masoumeh | * | 600 | Saed Panah | Fardin | * |
| 557 | Rafizadeh | Samira | * | 601 | Safa | Hesam | * |
| 558 | Rahimi | Asghar | * | 602 | Safapour | Ahmad | * |
| 559 | Rahimkhani | Shima |  | 603 | Safari | Sabriyeh | * |
| 560 | Rahimpour | Hosein | * | 604 | Safdari | Ali | * |
| 561 | Rahmani | Arsalan | * | 605 | Sahafi | Mohammad Reza | * |
| 562 | Rahmani | Morteza | * | 606 | Sahebi | Manoochehr | * |
| 563 | Rahmani | Somayeh | * | 607 | Saied Panah | Fardin | * |
| 564 | Rahmati | Mohammad Reza | * | 608 | Saiedi | Ahmad | * |
| 565 | Rajabi | Setareh | * | 609 | Sajjadi | Saba |  |
| 566 | Rajabzade Moghadam | Mohammad Reza | * | 610 | Sajjadiyan | Mehri | * |
| 567 | Ramezani | Jafar |  | 611 | Sal Moslehiyan | Mohammad |  |
| 568 | Ranjbari | Asghar | * | 612 | Salami | Sajad | * |
| 569 | Rashidi | Seyed Salah | * | 613 | Salehiyan Matiklayi | Behzad | * |
| 570 | Rashidinia | Jalil | * | 614 | Salem Kar | Ali Reza | * |
| 571 | Rashidpor | Zahra | * | 615 | Salimi | Hamideh |  |
| 572 | Rasuli | Saied | * | 616 | Salimi Absardi | Fatemeh | * |


| 617 | Salimi Kandeh | Mina |  | 661 | Siyami | Azam |  |
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| 618 | Salmani Gharaei | Kamran | * | 662 | Sohrabi | Saeid | * |
| 619 | Samadi | Babak | * | 663 | Soleimani | Mohammad ali | * |
| 620 | Samiei Paghaleh | Ameneh |  | 664 | Soleimani | Fatemeh | * |
| 621 | Sanami | Abolfazl | * | 665 | Soleimani Fard | Masoumeh |  |
| 622 | Sanatghar | Alireza | * | 666 | Soleimani Nia | Mahsa | * |
| 623 | Sanchooli | Mahmoud | * | 667 | Soleimani Varki | Mohammad | * |
| 624 | Sarbaz Janfada | Ali | * | 668 | Soleimanpour Bakefayat | Azhdar | * |
| 625 | Saremi |  | * | 669 | Soltan Zadeh | Fahimeh |  |
| 626 | Sargezi | Sima | * | 670 | Tabatabaie Shorijeh |  | * |
| 627 | Sayareh | Abdolreza | * | 671 | Tabibi Mamaghani | Javad |  |
| 628 | Seiedi | Narjes | * | 672 | Taghavi | Ali | * |
| 629 | Seifi | Jalil | * | 673 | Taheri | Mahsa | * |
| 630 | Seifolah Zadeh | Somayeh | * | 674 | Tahmasbi | Saied |  |
| 631 | Shaban | Somayeh | * | 675 | Tajbakhsh | Hadiseh |  |
| 632 | Shafiei | Mohammad | * | 676 | Tajik | Maryam |  |
| 633 | Shafiei | Batol |  | 677 | Talaie Firozjaie | Behnam | * |
| 634 | Shafiei Apourvari | Maryam | * | 678 | Talebi Rostami | Ali Asghar |  |
| 635 | Shafiei Babaei | Sara | * | 679 | Talebi Rostami | Yahia |  |
| 636 | Shafighi | Nazila | * | 680 | Taleshiani |  |  |
| 637 | Shah Dostfar | Mahdiyeh | * | 681 | Taleshiyan | Abolfazl |  |
| 638 | Shahabi | Mahnaz | * | 682 | Tari | Abolfazl |  |
| 639 | Shahbazpour | Khalil | * | 683 | Tarmandi | Masoumeh |  |
| 640 | Shahi | Nazila | * | 684 | Tavakolli | Ali | * |
| 641 | Shahraki | Somayeh | * | 685 | Tavalaie | Hamid | * |
| 642 | Shahriyari | Mohammad | * | 686 | Tayefeh | Behruz |  |
| 643 | Shahsavar | Faezeh | * | 687 | Torabi | Mohsen | * |
| 644 | Shajareh Pour Salevati | Nasrollah | * | 688 | Torki | Marzieh | * |
| 645 | Shakouri | Bita | * | 689 | Torkzadeh Tabrizi | Lida | * |
| 646 | Shams | Saeid | * | 690 | Uloumi | Alireza | * |
| 647 | Shamsi Deilami |  | * | 691 | Vaezpour | Mansur |  |
| 648 | Shamsi zarghar | Arman | * | 692 | Vafaie | Vajiheh | * |
| 649 | Sharif Zadeh | Mehri | * | 693 | Vahed | Tahmineh | * |
| 650 | Sharifi | Kamran | * | 694 | Valaie | Leila | * |
| 651 | Sharifi | Hesam aldin | * | 695 | Varmazyar | Rezvan | * |
| 652 | Sharifi Far | Serveh |  | 696 | Vazvaie |  | * |
| 653 | Shayanfar | Nikta | * | 697 | Vesagh | Zohreh | * |
| 654 | Sheikoleslami | Zahra |  | 698 | Vosoughi | Hosein | * |
| 655 | Shikare | M. M. | * | 699 | Yarahmadi | Zahra | * |
| 656 | Shiraziyan | Mohammad | * | 700 | Yarmohammadi | Raheleh | * |
| 657 | Shojayi | Behrooz | * | 701 | Yayli | Yusuf | * |
| 658 | Shokr Pour | Raheleh | * | 702 | Yazdanian |  | * |
| 659 | Shokri | Javad | * | 703 | Yazdi | Faezeh | * |
| 660 | Shorvarzi | Batool |  | 704 | Yazraghi | Najmeh Sadat |  |


| 705 | Yekkeh Fallah |  | $*$ |
| :---: | :--- | :--- | :---: |
| 706 | Yigider | M | $*$ |
| 707 | Yousef Zadeh | Akram | $*$ |
| 708 | Yousefi Azari | Vahideh | $*$ |
| 709 | Yusefzadeh | Elham |  |
| 710 | Zabihi | Fatemeh | $*$ |
| 711 | Zamani | Yousef | $*$ |
| 712 | Zamani | Mohammad Reza |  |
| 713 | Zameni ateni | Manoochehr | $*$ |
| 714 | Zare Moghadam | Hossein | $*$ |
| 715 | Zarghar | Mansour | $*$ |
| 716 | Zarrin | Mohammad |  |
| 717 | Zeinali | Homa | $*$ |
| 718 | Zeynaloy | C. I. | $*$ |
| 719 | Zibaie | Sadegh | $*$ |
| 720 | Ziyadi | Roghayeh |  |
| 721 | Zolfaghari |  | $*$ |

# حكــدهمقالات <br> -• $\because$ 





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