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## فهر ست

| صضه | عنوان |
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| 1 | يليس سايبرى؛ الزامات و راهكارهاى ايجاد و بياده سازى شبكه ملى مديريت تبادل اطلاعات و ارتباطات |
| Ir | توزيع بهناى باند بر مبناى إران سريس كيرنه ها با بكاركيرى تكيك AHP فازى |
| H |  |
| r | بهينه سازى زبان يكهارجه ساز بر دوى شبكه اطلاعاتى ناهمكون |
| fy | A Novel Patch Based Digital Signature |
| $\Delta 9$ | طراحى رويكرد امنيتى در شبكه هاى هسكر بيسيم |
| gY | محاسبات كاربردى: تهيين مكان هنسى بيّهنه براى كره هاى متحرك در MANET با استفاده ... |
| Vr |  |
| Ar | بردسى دوش هاى تشخيص رفتار غير عادى در شبكه هاى كامييوترى |
| 19 | شـناسايِى و اولويت بندى عوامل كليدى موفقيت بارك علم و فثاورى خراسـان رضوى |
| 1.1 | RFID بك بروتكل جستجوى بى نام براى سيستم هاى |
| 1. V | شناسايى عوامل موثر بر بياده سازى الكرى توسعه خرشه إى در صنايع توليّى تجهيزات نفت و كاز ... |
| IIV | يك روش جديد براى تثخيص خودرد در تصوير |
| Ira |  |
| Ira | بيش بينى وضعيت خوش حسابى متقاضيان در بازيرداذت تهيلات بانكى بر اساس شبكه هاى بيزين |
| $\|f\|$ | بردسى و بهبود امنيت بروتكل ايتترنت سيار ودرن T |
| 189 |  |
| IbY | رمزنكارى تموير امن و سريع بر بايه نكاشت آثوبناك با ساختار جايكيت- بانشيّى بوسبله ... |
| 19\% | رويكردى جهت انتقال ترافيك ويدئو در شبكه هاى موردى |
| 199 | مانيتّ رينك امنيت حمل و نقل راه آهن از طريق استفاده از شبكه حسكر بى سيم)(WSN) |


| (ivo | عنوان |
| :---: | :---: |
| IVA | ارانه مدلى مبتى بر داهنه براى مديريت اعتماد در محيط ابرى |
| lar | نتش فناورى اطلاعات و ارتباطات (ICT) در آموزش، يُوهش، نوآورى و مديريت دانش: راهكارهايى ... |
| 191 | الطلاعات و سيستم هاى اطلاعاتى در سازمان با تاكيد بر سيستم هاى اطلاعاتى مديدان ارشد. |
| r.r | يك روش بيشنهادى جهت استفاده امن از كارت هاى هوشمنـ جند منظوره |
| P. 9 | لايه امنيتى جديد براىى مقابله با دزدى هويت |
| Y10 | Parallel Calculation of Pi Number as Random Number Generator for Cryptography ... |
| rri | استفاده از منطق فازى براى مكان يابى مناسب فعاليتهاى اقتصادى |
| rra |  |
| rrimer | تاثيرات شبكه هاى VPN: سرمايه كذارى، نظم و امنيت |
| rra | ارايه دوشى جهت الفزايش امنيت در سيستم هاى بانكدارى سيار |
|  | بوستر مقالات |
| Pf\% |  |
| Yar | ايجاد مكادى د ر اهكار در امنيت سايبرى |
| P-9 | دولت همراه و راه كارهاى نوين كسترش امنيت اجتماعى و مقابله با جنك نـم |
| Y80 | راهكارهاى مقابله با جرايم رايانه آى در شهر الكترونيك: رويكرد مديريتى |
| rrr | بستر جرايم رايانه ایى و راه كارهاى مقابله با آن |
| rYq | مرودى بر دويكردهاى مهاجرت سيستم هاى وروثى بها معارى سرويس كرا |
| rav | بيش بينى حركات نرخ ارذ به دوش هاى تكاملى(شبكه عصبى) |
| rar | الرزيابى امنيت در بياده سازى شبكه مخابرات سيار جيد كشبر (EIAICC 2012) |
| Р99 | نتش راديو شناسه در بازكيت سرمايه (ROI) |
| r.a |  |



# A Novel Patch-Based Digital Signature 

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#### Abstract

: In this paper a new patch-based digital signature (DS) is suggested. The proposed approach similar to steganography methods hides the secure messuge in a host image. However, it uses a patch-based key to code/decode the data like cryptography approaches. Both the host image and key patches are randomly, initialized. The proposed approach consists of coding and decoding algorithms. The coding algorithm converts the characters stream of the secret message to the patches stream of the DS image. The final image can be further distorted by noise to hide the source patches. Nevertheless, the decoding algorithm uses the connectivity and compactness properties of patches to decode the secret message. Experimental results demonstrated that it is significantly robust against noise. The proposed approach has been successfully used for digital signature generation.


Keywords: Digital Signature, Patch-Based Image Processing, Steganography, Watermarking

## 1. Introduction

The demand of secure transmission of information has been an issue since the first invented communication methods. Security has a top priority in any organization dealing with confidential data. Whatever is the method we choose for the security purpose, the major issue is the degree of security [1].
The problem of unauthorized copying is of great concern especially to the music, film, book, and, software publishing industries. To overcome this problem,
some invisible information can be embedded in the digital media in such a way that it could not be easily extracted without a specialized technique [2]. Information hiding is an emerging research area, which encompasses applications such as copyright protection for digital media, watermarking, steganography, fingerprinting, graphical passwords, digital signature (DS), and copy deterrence of software [3].
For more details, in watermarking, the message, a low-level signal including
owner identification and a digital time stamp, is directly placed into the host data set (e.g. an image) [4]. The buyer-seller watermarking protocol is a good example of using invisible watermarks for copy deterrence applications [5]. Various techniques have been proposed for publickey watermarking systems, which allow two parties who have never met or exchanged a secret, to send hidden messages over public channels $[6,7]$.
Steganography, which is also considered as invisible watermarking, imperceptibly hides the secret message within the host data $[8,9]$. For example, substituting the message data with the least significant bits of the host data is a well-known frequently-used approach [10-14]. As an example, Aly [11] used the least significant bit method to embed the secret message in the motion vectors of the Pand B -frames in a compressed video.
By using the fingerprint approach, the owner can embed a serial number in the data set. It uniquely indicates the copyright information and thus, any unauthorized use of the data set can be traced [3].
Moreover, one of the most important topics in information security is the user authentication. There is a good security by using the text-based strong password schemes, but memorizing the password is often so difficult and users usually write them down on a piece of paper or save inside the computer. The graphical user authentication (or graphical password), known as an alternative solution, is actually based on this fact that the human tend to remember images better. However, the graphical passwords are vulnerable to five attacks including brute force, dictionary, spyware, shoulder surfing, and social engineering attacks [15].
Besides, by using DS in electronic government, confidentiality, integrity, authenticity, and anti-denial of circulating
documents in network environment can be solved [16, 17]. Jarusombat et al proposed location based DS on mobile devices which increases the security and also compromises with low-computation capability and limited battery life of these devices [18].
However, with the advent of illegal copying of software and pervasive access to the Internet, software protection has gained increasing importance. Therefore, a complete solution is required to provide the software piracy protection capability. It should allow one to protect his/her software applications against piracy, illegal use, or illegitimate copy [19].
Generally speaking, copy-protection techniques can be separated into tokenbased and token-less categories. Although token-based techniques are most common, they simply refuse to run software until a specified token is present [20]. However, they can be simply cracked by removing the checks of tokens from the application code while the software itself remains fully functional. In contrast, typical token-less techniques (such as obfuscation, encryption, watermarking, fingerprinting, and so forth) try to authenticate the user.
In this paper, we propose a new DS generation and verification method which can provide a breakthrough in all the mentioned applications. The proposed approach, called PBIS (patch-based image signature), includes coding and decoding stages. First, the proposed coding algorithm (referred to as C-PBIS) decomposes the secret message to its fundamental characters while the DS image is randomly initialized. Then, for each message character, the corresponding patch in the codex (i.e. a set of randomly generated primary patches) is copied to a randomly-chosen position of the image. After encryption of some essential coding parameters, whole the image is distorted by additive noise.
software licence agreement, secure communication, and so forth.

## Acknowledgements

This work is partially supported by Binatooth Machine Vision and Image Processing Co. affiliated to Khorasan Science and Technology Park. Besides, it is a part of the project Intelligent Industrial Camera with the grant No. 15/13644 of Ferdowsi University of Mashhad.

## Appendix A

Let's $M$ be a matrix of size $e \times f$ whose components are also matrixes of size $g \times h$. The component located in the $r$ th row and $c$ th column of $M$ is represented by $M_{(r, c)}$. Moreover, the component of $p$ th row and $q$ th column of $M_{(r, c)}$ is also indicated by $M_{(r . c)}(p, q)$.
Furthermore, we can equivalently use the indexbased method to uniquely indicate each component of $M$. In more detail, the $i$ th component of $M$, shown by $M_{(i)}$ (where $i$ is the index), corresponds to $M_{(r . c)}$, if and only if:
$i=(c-1) \times e+r$
(35)
or equivalently:
$(r, c)=\left(\bmod (i-1, e)+1,\left[\frac{i-1}{e}\right]+1\right)$
(36)
where [.] returns the integer fraction of a number and $\bmod (a, b)$ computes $a$ modulo $b$. Similarly, the $j$ th component of $M_{i}$ is given by:
$M_{(i)}(j)=M_{(r, c)}\left(\bmod (j-1, g),\left[\frac{j-1}{g}\right]\right)$
(37)

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- Some message source $m$ In order PBIS, th were emp
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$p_{\text {suc }}(w, \eta)=$
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Fig. 5 sh
$e_{m i s}$ versu
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## چچروهشَگر گَامى، صنعتگَر ارجمند،

جناب آقاى مهدى سعادتمند

با سلام و احترام،

دبيرخانه كنفرانس در كمال مسرت و افتخار به اطلاع گرامى مىرساند مقاله شما تحت عنوان

A Novel Patch-Based Digital Signature
جهت سخنرانى شفاهى در كنفرانس پذيرفته شده است.

جهت تكميل موارد ثبت نام، ارائه مقاله، چاپֶ كامل مقاله در كتابپچه مقالات كنفرانس، صرف نهار و پذيرايی، انجام موارد ذيل حداكثر تا تاريخ 1390/11/12 ضرورى مىباشد:

1 -ارسال نسخه نهايى مقاله مطابق با فرمت مقاله كنفرانس
2 -ارسال تصوير فيش بانكى ثبت نام به ايميل eiaicc@azaruniv.edu

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& \text { دبير علمى كنفرانس محسن حيدريان }
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# A Novel Patch-Based Digital Signature 

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For more details, in watermarking, the message, a lowlevel signal including owner identification and a digital time stamp, is directly placed into the host data set (e.g. an image) [4]. The buyer-seller watermarking protocol is a good example of using invisible watermarks for copy deterrence applications [5]. Various techniques have been proposed for public-key watermarking systems, which allow two parties who have never met or exchanged a secret, to send hidden messages over public channels [6, 7].

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contrast, typical token-less techniques (such as obfuscation, encryption, watermarking, fingerprinting, and so forth) try to authenticate the user.

In this paper, we propose a new DS generation and verification method which can provide a breakthrough in all the mentioned applications. The proposed approach, called PBIS (patch-based image signature), includes coding and decoding stages. First, the proposed coding algorithm (referred to as C-PBIS) decomposes the secret message to its fundamental characters while the DS image is randomly initialized. Then, for each message character, the corresponding patch in the codex (i.e. a set of randomly generated primary patches) is copied to a randomly-chosen position of the image. After encryption of some essential coding parameters, whole the image is distorted by additive noise. Finally, the DS image is reshaped to hide its original size from the user.

In the suggested decoding algorithm (referred to as DPBIS), after decryption of the coding parameters, for each patch in the image, the corresponding character is specified by using the nearest neighbor measure.

Experimental results demonstrated significant robustness of PBIS against noise. Furthermore, the computational burden of both the coding and decoding algorithms is small. They are easy and straightforward to implement. Therefore, PBIS can be used in a wide variety of security applications such as user authentication, software license agreement, and so forth.

This paper is organized as follows: the proposed algorithm is explained in Section 2. Experimental results are given in Section 3. Finally, Section 4 is devoted to concluding remarks.

Notations used in this paper are fairly standard. Both sets and matrixes are represented by upper-case letters while the later can be distinguished by italicface symbols. Boldface symbols are also used for vectors. For more details about the index-based representation of matrix/set components, see Appendix A.

## 2. Digital Image Signature

Both C- and D-PBIS, require some primary information including the symbols set $(\mathrm{S})$, codex set $(\mathrm{P})$, and permitted movements matrixes along $x$-axis $\left(D^{x}\right)$ and $y$-axis $\left(D^{y}\right)$ to properly work.

In more detail, the symbols set S, given by the DS images provider (so-called the security administrator), includes all the characters necessary to write the text-based secret message such as alphabets, digits, space, dash, under-line, comma, and so forth, as follows:
$\mathrm{S}=\left\{\mathrm{S}_{(k)} \mid k \in \mathrm{Z}, 0<k \leq L_{\mathrm{S}}\right\}$
where $\mathrm{S}_{(k)}$ represents the $k$ th component of S and $L_{\mathrm{S}}=\|\mathrm{S}\|$
in which ||.|| returns the cardinality of a set or number of components within a matrix.

The matrixes $D_{x}\left(L_{x}=\left\|D_{x}\right\|\right)$ and $D_{y}\left(L_{y}=\left\|D_{y}\right\|\right)$ are used to locate each coding patch in the DS image with respect to the previous patch position.

The codex is a set of $L_{\widetilde{\mathrm{S}}} L_{x} L_{y}+1$ randomly-initialized matrixes of size $w \times w$ (so-called patches) with threedimensional vectorial components. Therefore, we can write:


Fig. 1. A sample codex: each row corresponds to a digit and every column matches to a doublet $(\Delta x, \Delta y)$. The single patch in the last row is the end-patch.

$$
\begin{equation*}
\mathrm{P}=\left\{P_{(i)} \mid i \in \mathrm{Z}, 0<i \leq L_{\mathrm{S}} L_{x} L_{y}+1\right\} \tag{2}
\end{equation*}
$$

where $P_{(i)}$ is the $i$ th patch of the codex. Specifically, the last patch of P (called the end-patch) will be used to indicate the end of a patch stream (see Section 2.1.2). For example, a sample codex, including $10 \times 5 \times 5+1$ patches, with $\mathrm{S}=\{0,1, \ldots, 9\}$ and $D_{x}=D_{y}=[-2,-1,0,1,2]$, is illustrated in Fig. 1.

Excluding the end-patch, P can be simplified to a matrix of size $L_{\mathrm{S}} \times L_{x} L_{y}$, as follows:
$P=\left[\begin{array}{cccc}P_{(1,1)} & P_{(1,2)} & \ldots & P_{\left(1, L_{x} L_{y}\right)} \\ P_{(2,1)} & P_{(2,2)} & \ldots & P_{\left(2, L_{x} L_{y}\right)} \\ \vdots & \vdots & & \vdots \\ P_{\left(L_{\mathrm{S}}, 1\right)} & P_{\left(L_{\mathrm{s}}, 2\right)} & \ldots & P_{\left(L_{\mathrm{s}}, L_{x} L_{y}\right)}\end{array}\right]$
where
$P_{(p, q)}=P_{\left((q-1) L_{\mathrm{s}}+p\right)}$
Furthermore, the patch $P_{(p, q)}$ corresponds to the triplet $\left(\mathrm{S}_{(k)}, \Delta x, \Delta y\right)$ only when $p=k$ and,
$q=L_{y}(\Delta x-1)+\Delta y$
or equivalently:
$\left\{\Delta x=\left[\frac{q-1}{L_{y}}\right]+1\right.$
$\Delta y=\bmod \left(q-1, L_{y}\right)+1$
where $\Delta x \in D_{x}$ and $\Delta y \in D_{y}$. For example, in Fig. 1, $P_{(2,9)}$ corresponds to ( $\mathrm{S}_{(2)}=1, \Delta x=-1, \Delta y=1$ ).

### 2.1 Coding Algorithm

Fig. 2 shows the block diagram of the proposed coding algorithm. C-PBIS treats the secret message as a stream of consequence characters. Indeed, it converts this characters stream to a patches stream within the DS image as follows.

### 2.1.1 Initialization

First, all pixels of the DS image ( $I$ ) are randomly initialized in the range [ 0,255 ]. Indeed, $I$ is an image of size $b \times \alpha b \times 3$ which can be considered as a matrix of size $b \times \alpha b$ with three-dimensional vectorial components. The parameters $b$ and $\alpha$ are integer constants, separately specified for each secret message.

The secret message can be decomposed to its fundamental characters, as follows:
$\mathrm{C}=\left\{\mathrm{C}_{(k)} \mid 1 \leq k \leq L_{\mathrm{C}}\right\} \subset \mathrm{S}$


Fig. 2. The block diagram of C-PBIS
where C is the set of message characters, $\mathrm{C}_{(k)}$ indicates its $k$ th component, and $L_{\mathrm{C}}=\|\mathrm{C}\|$.

As shown in Fig. 3, $I$ is divided into $\alpha$ square blocks (including $B_{0}, B_{1}, \ldots, B_{a-1}$ ), all of size $b \times b$. Except the first block ( $B_{0}$ ) which is reserved to code C-PBIS parameters (see Section 2.1.3), every remaining block can include only one patch. Thus, to preserve the possibility of using all components of $D_{x}$ and $D_{y}$ for localization of patches (see Section 2.1.2), we should have:
$w+\max \left(\max _{\Delta x \in D_{x}}(|\Delta x|), \max _{\Delta y \in D_{y}}(|\Delta y|)\right) \leq b$
where $|$.$| computes the first-order norm (so-called Manhattan$ distance measure) [21].

Besides, the patches stream should be finished by the end-patch. Thus, $\alpha$ should observe the following constraint:
$L_{\widetilde{\mathrm{C}}}+2 \leq \alpha$

### 2.1.2 Patches Stream

Then, the integer parameters $x_{1}$ and $y_{1}$ are randomly initialized in the range $[1, b-w]$ as follows (Let's $k=1$ ):
$1 \leq x_{1}, y_{1} \leq b-w$
They are used to locate the first stream patch in $B_{1}$. Generally, in the $k$ th step $\left(1 \leq k \leq L_{\widetilde{\mathrm{C}}}+1\right)$, the position of the top-left corner of the current patch within $B_{k}$ is specified by $\left(x_{k}, y_{k}\right)$.

To increase the security of the coding algorithm, every $\left(x_{k}, y_{k}\right)$ should be randomly initialized. For achieving this purpose, the parameters $\Delta x_{k}$ and $\Delta y_{k}$ are randomly selected from $D_{x}$ and $D_{y}$, respectively, with observing the following constraints:
$\left\{\begin{array}{l}-x_{k}<\Delta x_{k} \leq b-w-x_{k} \\ -y_{k}<\Delta y_{k} \leq b-w-y_{k}\end{array}\right.$
In each step of the coding algorithm, $\left(\Delta x_{k}, \Delta y_{k}\right)$ is provided to specify the position of the next patch in the image.

Next, if all message characters have been already coded in the image (i.e. $L_{\mathrm{C}} \leq k$ ), the end-patch is selected to specify the end of the stream. Otherwise, the patch corresponded to the triplet $\left(c_{k}, \Delta x_{k}, \Delta y_{k}\right)$ is chosen to specify both the $k$ th message character and the position of the next patch.

Subsequently, the selected patch is copied to the corresponding components of $B_{k}$ as follows:

$$
\begin{equation*}
\boldsymbol{B}_{k}(i, j)=\boldsymbol{P}_{\left(p, L_{y}\left(\Delta x_{k}-1\right)+\Delta y_{k}\right)}(i, j), \quad 1 \leq i, j \leq w \tag{12}
\end{equation*}
$$

such that,
$\boldsymbol{B}_{k}(i, j)=\boldsymbol{I}\left(x_{k}+k b+i-1, y_{k}+j-1\right)$


Fig. 3. The DS image $I$ is divided into $\alpha$ blocks, each of size $b \times b$.


Fig. 4. Six DS images provided for the secret message 0123456789 with the codex of Fig. 1 and $\eta=100 \%$, all of size $36 \times 27$.

For example, according to the above equations, the component located on the top-left corner of the $k$ th patch is copied to the position $\left(x_{k}+k b, y_{k}\right)$ of $I$, equalivalent to the position $\left(x_{k}, y_{k}\right)$ of $B_{k}$.

Afterwards, the position of the next patch is explicitly computed as follows:
$\left\{\begin{array}{l}x_{k+1}=x_{k}+\Delta x_{k} \\ y_{k+1}=y_{k}+\Delta y_{k}\end{array}\right.$
Both $x_{k+1}$ and $y_{k+1}$ are also in the range [ $\left.1, b-w\right]$, because of observing the constraints of Eq. (11) by $\Delta x_{k}$ and $\Delta y_{k}$.

After increasing $k$ by one, the above process is repeated until the patch stream finishes with the end-patch.

### 2.1.3 Coding Algorithm Parameters

Then, some essential parameters of C-PBIS including $b$, $x_{1}$, and $y_{1}$ should be encrypted within $B_{0}$, because they separately alter for each secrete message. For this aim, we take advantage of the index-based representation (see Appendix A) for components of $P$ and $I$.

In more detail, for encrypting $b, x_{1}$, and $y_{1}$, whole components of the patches $P_{b}, P_{x_{1}}$, and $P_{y_{1}}$, respectively, are consecutively copied to the corresponding components of $B_{0}$ as follows:

$$
\boldsymbol{B}_{0}(i)= \begin{cases}\boldsymbol{P}_{b}\left(\bmod \left(i-1, w^{2}\right)+1\right) & 0<i \leq w^{2}  \tag{15}\\ \boldsymbol{P}_{x_{1}}\left(\bmod \left(i-1, w^{2}\right)+1\right) & w^{2}<i \leq 2 w^{2} \\ \boldsymbol{P}_{y_{1}}\left(\bmod \left(i-1, w^{2}\right)+1\right) & 2 w^{2}<i \leq 3 w^{2}\end{cases}
$$

For the sake of importance of coding parameters, the above copy procedure is repeated for $\eta(1 \leq \eta)$ times. Thus, we should have:
$3 \eta w^{2} \leq b^{2} \Rightarrow \sqrt{3 \eta} w \leq b$
Combining the above equation with Eq. (8), we can write:
$w+\max \left(\max _{\Delta x \in D_{x}}(|\Delta x|), \max _{\Delta y \in D_{y}}(|\Delta y|),(\sqrt{3 \eta}-1) w\right) \leq b$
This equation provides a lower limit for the height of $I$.

### 2.1.4 Distortion by Noise

Next, $I$ is altered by additive noise as follows:
$\hat{\mathbf{I}}(i)=\boldsymbol{I}(i)+\gamma \operatorname{rand}(), \quad 1 \leq i \leq \alpha b^{2}$
where the function rand() randomly generates a threedimensional vector (with scalar components in the range $[0,255]$ ) based on the multiplicative congruential approach [22]. The coefficient $\gamma$ also indicates the strength of noise. As demonstrated in experimental results (see Section 3.2), D-PBIS is fairly robust against noise. Therefore, for increasing the security of the algorithm, in this step, $I$ is distorted by noise to hide source patches from the user.

### 2.1.5 Image Reshaping

By copying each component of $\hat{I}$ to the corresponding one with the same index, the final DS image $\bar{I}$ of size $b \beta \times \alpha b / \beta$ is produced as follows:
$\overline{\boldsymbol{I}}(i)=\hat{\boldsymbol{I}}(i), \quad 1 \leq i \leq \alpha b^{2}$
Here, $\beta$ is a randomly-chosen divisor of $\alpha$ as follows:
$\beta \in\{n \in \mathrm{~N} \mid 1<n, \bmod (\alpha, n)=0\}$
The final image is reshaped to hide its true width (i.e. $b$ ) from the user and in turn, improve security of the digital signature.

### 2.1.6 PBIS Key

The primary parameters of the proposed algorithm including P, $\mathrm{S}, D_{x}, D_{y}, w$, and $\eta$ should be specified by the security administrator. Both C-PBIS and D-PBIS should use these parameters with exactly the same values to correctly work. At first glance, it may seem like a constraint, but that can provide a secure method to separate DS images produced by different administrators. In other words, the above primary parameters totally form the encryption key of PBIS. To correctly decode the DS image, this key should be entirely known.

Similar to watermarking and steganography methods, PBIS hides the secure message in a host image. However, it provides a coding key similar to cryptography algorithms.

Anyway, for its very long length, the PBIS key is significantly complex. In more detail, the main part of the key is the codex. It consists of $L_{\widetilde{\mathrm{S}}} L_{x} L_{y}+1$ patches. Each patch includes $w^{2}$ three-dimensional vectorial components whose elements range between 0 and 255 . Therefore, the number of all possible codexes is given by:
$N(\mathrm{P})=256^{3 w^{2}\left(L_{\mathrm{S}} L_{x} L_{y}+1\right)}$
For example, when $L_{\mathrm{S}}=10$ (e.g. once S includes only digits), $L_{x}=L_{y}=3$ (e.g. for $D_{x}=D_{y}=[-1,0,1]$ ), and $w=3$, we have $N(\mathrm{P})=2^{19656} \approx 1.11 \times 10^{5917}$. If a computer evaluates each codex in one nanosecond, it takes more than $2.77 \times 10^{5901}$ years to check all possible cases.

Furthermore, C-PBIS uses a number of parameters, including $b, \alpha, \beta$, and ( $x_{1}, y_{1}$ ), which should be separately initialized for each secret message, with observing Eqs. (17), (9), (20), and (11), respectively (see Section 2.1.3). Therefore, as illustrated in Fig. 4, even for the same secret message, each time, C-PBIS provides a different DS image because of randomly initialization of the DS image, using different values for the above parameters, and altering the final DS image with noise.

### 2.2 Decoding Algorithm

Once the PBIS key is given, decoding of the DS image is straightforward. Generally, for the candidate patch $\bar{P}$, the most similar patch in the codex is given by using the firstorder norm as follows:
$m=\operatorname{index}\left(\min _{j}\left(\operatorname{sum}_{i=1}^{w^{2}}\left(\overline{\boldsymbol{P}}(i)-\boldsymbol{P}_{j}(i)\right)\right)\right)$
Although we take advantage of the above similarity function for its simplicity, higher order norms or cross-correlation measure, also, can be alternatively used.

### 2.2.1 Initialization

Initially, to decrypt the exclusive coding parameters, including $b, \alpha, x_{1}$, and $y_{1}$, the first $3 \eta w^{2}$ components of $\bar{I}$ (i.e. $\overline{\boldsymbol{I}}(1)$ to $\overline{\boldsymbol{I}}\left(3 \eta w^{2}\right)$ ) are divided into $3 \eta$ patches (including $\bar{P}_{1}, \bar{P}_{2}, \ldots$, and $\bar{P}_{3 \eta}$ ) such that each consists of $w^{2}$ components. According to Section 2.1.3, all the patches
$\bar{P}_{1}, \bar{P}_{4}, \ldots, \bar{P}_{3 \eta-2}$ correspond to $P_{b}$. Thus, $b$ can be obtained as the median of indexes of all matched patches as follows:
$b=\underset{k=1}{\operatorname{median}}\left(\operatorname{index}\left(\min _{j}\left(\operatorname{wu}_{i=1}^{w^{2}}\left(\mid \overline{\boldsymbol{P}}_{3 k-2}(i)-\boldsymbol{P}_{j}(i)\right)\right)\right)\right)$
Similarly, we have:
$x_{1}=\underset{k=1}{\eta} \underset{\operatorname{mian}}{ }\left(\operatorname{index}\left(\min _{j}\left(\operatorname{sum}_{i=1}^{w^{2}}\left(\overline{\boldsymbol{P}}_{3 k-1}(i)-\boldsymbol{P}_{j}(i)\right)\right)\right)\right)$
$y_{1}=\underset{k=1}{\eta} \operatorname{mian}^{\eta}\left(\operatorname{index}\left(\min _{j}\left(\operatorname{sum}_{i=1}^{w^{2}}\left(\left|\overline{\boldsymbol{P}}_{3 k}(i)-\boldsymbol{P}_{j}(i)\right|\right)\right)\right)\right)$
Obviously, $\alpha$ is given by:
$\alpha=\|\bar{I}\| / b$
Therefore, $\hat{I}$ can be obtained by reshaping $\bar{I}$ to a matrix of size $b \times \alpha b$, according to Eq. (19). It is worth to note that there is no way to obtain $I$ from $\hat{I}$, because of distortion by unknown additive noise. Instead, we can decrypt the secret message through the similarity measure of Eq. (22).

### 2.2.2 Characters Stream

Similar to the approach used in C-PBIS, we should convert the patch stream of the DS image to the characters stream of the secret message.

Generally, in the $k$ th step (initially, set $k=1$ ) of the decoding algorithm, the position of the top-left corner of the current patch, of size $w \times w$, in $\hat{I}$ (shown by $\hat{P}_{k}$ ) is given by $\left(k b+x_{k}, y_{k}\right)$. In this case, the $k$ th character of the secret message can be specified by obtaining the most similar patch in the codex as follows:
$\left(p_{k}, q_{k}\right)=\operatorname{index}\left(\min _{(p, q)}\left(\operatorname{sum}_{i=1}^{w^{2}}\left(\left|\hat{\boldsymbol{P}}_{k}(i)-\boldsymbol{P}_{(p, q)}(i)\right|\right)\right)\right)$
Obviously, $\mathrm{S}_{p_{k}}$ specifies the $k$ th character of the secret message. Furthermore, according to Eq. (6), to obtain the position of the next patch in $\hat{I}$, we should have:
$\left(x_{k+1}, y_{k+1}\right)=\left(\left[\frac{q_{k}-1}{L_{y}}\right]+1, \bmod \left(q_{k}-1, L_{y}\right)+1\right)$
After augmenting $k$ by one, the above process is repeated until the patch stream finishes with the end-patch.

## 3. Experimental Results

The performance of DIS was evaluated using three different codexes with $w=3,5$, and 7. All the experimental results were obtained by an Intel Core2Duo $2.0-\mathrm{GHz}$ Laptop with 3-GB main memory using MATLAB environment.

### 3.1 Producing the Codex

In all experimental evaluations, the symbols set included only digits and $D_{x}=D_{y}=[-2,-1,0,1,2]$ Consequently, each codex includes 251 patches.

Furthermore, in each codex, the patches should be as diverse as possible to improve the performance of D-PBIS against noise. In other words, more dissimilar patches can be better distinguished from each other.

Therefore, we provided a simple and effective algorithm to produce diverse patches. In more detail, after initialization of the first patch, a new one is randomly produced. The
patch will be added to the codex, if it observes the following constraint:

$$
\begin{equation*}
\theta<\min _{j=1}^{k-1}\left(\frac{1}{w^{2}} \operatorname{sum}_{i=1}^{w^{2}}\left(\left|\boldsymbol{P}_{k}(i)-\boldsymbol{P}_{j}(i)\right|\right)\right) \tag{29}
\end{equation*}
$$

where $\theta$ is the threshold of minimum acceptable difference between patches. Otherwise, a new patch is randomly generated. The above procedure repeated until all required patches are initialized.

We experimentally obtained $\theta=62$. By using the above approach, three sets of patches with $w=3,5$, and 7 were made.


Fig. 5. Variations of (top) $p_{\text {suc }}$, (centre) $e_{\text {fail }}$, and (bottom) $e_{m i s}$ versus $\eta$ for different values of $w$.

### 3.2 Robustness against Noise

The proposed algorithm is significantly secure, because of:

- Using very long key
- Randomly initialization of some parameters of C-PBIS for each secure message
- Distortion of the DS image by additive noise

Indeed, C-PBIS produces different DS images for even the same secure message. This may be the most important and unparalleled property of the proposed algorithm. For example, Fig. 4 illustrates six different DS images provided for the secure code 0123456789 with the codex of Fig. 1 and $\eta=100 \%$.


Fig. 6. The developed software for PBIS (GUI texts are in Farsi).
Furthermore, the statistical analysis methods are not useful to discover the PBIS key because; both the host image and coding patches are generated by using the same randomnumber generation method. Moreover, it is also employed to distort the final DS image.

On the other hand, although patch-based image processing methods are well-known and frequently-used, PBIS can be counted as the first patch-based algorithm to generate digital signatures. D-PBIS takes advantage of compactness and connectivity of patches to decode the DS image. Thus, it should properly work even for an altered DS image.

To test performance of D-DIS against noise, three different codex sets with $w=3,5$, and 7 were employed. $D_{x}$, $D_{y}$ and S were also chosen as the same as those used in Fig. 1. $\eta$ was increased by the step of $5 \%$ ranging from $80 \%$ to $150 \%$. In each step, the same secure code (i.e. 123456789) was coded and then decoded for 1000 times. In decoding of the secure message, three situations may take place:

- The secure message is successfully decoded.
- The decoding algorithm fails because of wrong encryption of the coding parameters.
- Some characters of the decrypted message mismatch with those of the source message.
In order to evaluate the performance of D-PBIS, the following evaluation measures were employed:
$p_{\text {suc }}(w, \eta)=\frac{\text { Number of successes }}{1000} \times 100 \%$
$e_{\text {fail }}(w, \eta)=\frac{\text { Number of failures }}{1000} \times 100 \%$
$e_{m i s}(w, \eta)=\frac{\text { Number of mismatches }}{1000} \times 100 \%$
$e_{m i s}^{k}(w, \eta)=\frac{\text { Number of mismatches of the } k \text { th digit }}{1000} \times 100 \%$
where $p_{\text {suc }}, e_{\text {fail }}, e_{\text {mis }}$, and $e_{m i s}^{k}$ computes the percents of successful decoding attempts, decoding failures, whole message mismatches, and mismatches of the $k$ th character, respectively. Obviously, we have:
$p_{\text {suc }}(w, \eta)=100 \%-e_{\text {fail }}(w, \eta)-e_{\text {mis }}(w, \eta)$
$e_{m i s}(w, \eta)=\sum_{k=1}^{L_{\tilde{C}}} e_{m i s}^{k}(w, \eta)$
Fig. 5 shows variations of $p_{s u c}, e_{\text {fail }}$, and $e_{m i s}$ versus $\eta$ for different values of $w$. For all values of $w$ with $\eta \leq 80 \%$, DPBIS was quite successful to decode all DS images ( $p_{\text {suu }}=100 \%$ ). Although $p_{\text {suc }}$ decreases by increasing $\eta$, its sensitivity to noise significantly improved by augmenting $w$; such that for $\eta=150 \%$, we have $p_{\text {suc }}=99.4 \%$ with $w=7$.

For every values of $\eta$ and $w, e_{m i s}$ was approximately 2 times greater than $e_{\text {fail }}$. In other words, from every three unsuccessful decoding attempts, D-PBIS failed only for once.

As demonstrated, D-PBIS may sometimes fail to decode the distorted DS image. Therefore, after finishing C-PBIS, it is necessary to check correct decoding of the image. In this case, if D-PBIS fails, a new DS image should be produced. Fig. 6 illustrates the developed software for PBIS.

## 4. Conclusion

In this paper, a new patch-based algorithm for digital signature generation and verification was proposed. It uses a set of randomly generated patches to code a set of character symbols. Indeed, C-PBIS converts the characters stream of the secret message to the patches stream of the DS image. CDIS uses a very long key which considerably improves the security of provided DS images. Besides, both the host image and codex patches are initialized by using the same random-number generator method. It is also employed to further distort the final DS image. For all these reasons, the proposed algorithm is very secure against statistical analysing methods.

D-PBIS decodes the DS image by using a simple similarity measure. Actually, it takes advantage of the compactness and connectivity of patches. For this reason, DPBIS was significantly robust against noise. Experimental results demonstrated that D-PBIS successfully decoded $99.4 \%$ of DS images generated by C-PBIS (with $w=7$ and $\eta=150 \%$ ).

Although DIS is originally proposed for digital signature applications, it can be used for a wide variety of security applications such as user authentication, software licence agreement, secure communication, and so forth.

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## Appendix A

Let's $M$ be a matrix of size $e^{\times f}$ whose components are also matrixes of size $g \times h$. The component located in the $r$ th row and $c$ th column of $M$ is represented by $M_{(r, c)}$. Moreover, the component of $p$ th row and $q$ th column of $M_{(r, c)}$ is also indicated by $M_{(r, c)}(p, q)$.

Furthermore, we can equivalently use the index-based method to uniquely indicate each component of $M$. In more detail, the $i$ th component of $M$, shown by $M_{(i)}$ (where $i$ is the index), corresponds to $M_{(r, c)}$, if and only if:
$i=(c-1) \times e+r$
or equivalently:
$(r, c)=\left(\bmod (i-1, e)+1,\left[\frac{i-1}{e}\right]+1\right)$
where [.] returns the integer fraction of a number and $\bmod (a, b)$ computes $a$ modulo $b$. Similarly, the $j$ th component of $M_{i}$ is given by:
$M_{(i)}(j)=M_{(r, c)}\left(\bmod (j-1, g),\left[\frac{j-1}{g}\right]\right)$

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