# Application of Taguchi Optimization Method in Active Vibration Control ofa Smart Beam

Alireza Akbarzadeh<sup>1,a</sup>, Mohsen Fallah<sup>2,b</sup>,

Navid Mahpeykar<sup>3,c</sup> and Nader Nabavi<sup>4,d</sup>

<sup>1, 2, 3, 4</sup> Faculty of Mechanical Engineering, Ferdowsi University of Mashhad, Mashhad, Iran

<sup>a</sup>Ali\_Akbarzadeh\_T@yahoo.com,<sup>b</sup>Desolids@gmail.com

<sup>c</sup>Navid.mhp@gmail.com,<sup>d</sup>S.Nader.Nabavi@gmail.com

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Abstract. Cantilevered beams can serve as a basic model for a number of structures used in various fields of industry, such as airplane wings, turbine blades and robotic manipulator arms. In this paper, the active vibration control of a smart cantilevered beam with a piezoelectric patch is studied. Additionally, the optimization of influential parameters of piezoelectric actuator for the purpose of vibration suppression is performed. Initially, the finite element modeling of the cantilevered beam and its piezoelectric patch is described and the implementation of a control system for vibration suppression is introduced. Transient response of the system under impact loading, with and without controller, is simulated using ANSYS. Taguchi's design of experiments method is used to investigate the effect of five geometric parameters on the vibrational behavior of the system. It is shown that, optimal selection of levels for geometry of the piezoelectric actuator and sensor, can dramatically improve the dynamic response of the smart beam.

#### Introduction

A smart structure can be defined as a structure or structural component with bonded or embedded sensors and actuators coupled with a control system which enables the structure to respond to the external stimuli in order to suppress the undesired effects or enhance the desired effects [1].Piezoelectric materials have been used extensively as the distributed sensors and actuators in a wide range of applications, such as shape control, vibration suppression and noise attenuation [2]. Many studies have focused on the modeling of piezoelectric direct and inverse effects [3–5]. Commonly, the finite element method is used to solve the coupled electromechanical systems.

The purpose of active vibration control is to reduce the unwanted vibrations of a mechanical system by means of modifying the system's structural response [6]. In an active structure, sensors detect vibrations while actuators influence the structural response of the system. The controller must suitably manipulate the sensor's signal and modify the system's response which leads to an acceptable suppression of vibration. Application of smart structures to vibration control may be found in[7]. Literature reviews show that much research on active vibration control, hybrid control and optimal placement and sizing of the actuators have been carried out, concerning the piezoelectric smart structures, and significant achievements have been obtained [8–10].

The performance of vibration control for flexible structures depends on the applied voltage, location of the piezoelectric actuator or sensor and dimensions of piezoelectric actuator [11]. In the present paper the active vibration control of a smart beam under impact loading is investigated using finite element method. The optimal dimensions and location of piezoelectric actuator and sensor is obtained using Taguchi method. Results showthat using the optimal parameters settings, the unwanted vibrations of the smart beam is effectively suppressed.

#### **Piezoelectric Smart Structure**

**Finite Element Model.** In this study SOLID45 and SOLID5elements are used to model the beam and the piezoelectric actuator, respectively. The finite element model is shown in Fig.1. Cantilever boundary condition is applied to fix the nodes at the beam's support. The voltage degree of freedom is coupled for the nodes at the top and bottom surfaces of the actuator. The beam and the piezoelectric actuator are made of aluminum and PZT-5H [12], respectively. The dimensions and properties of beam are reported in Table 1.



Figure 1 Finite element model of the smart beam

Figure 2 The configuration of smart beam

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Table	1Dime	ensions	and	mecha	nical	pro	perties	of	the	cantil	ever	bear	n

В	eam Dimension	ns	Mechanical Properties					
Thickness	Width	Length	Elastic Modulus	Density	Poisson's ratio			
2 [mm]	30 [mm]	500 [mm]	68e9 [Pa]	2800 [kg/m <sup>3</sup> ]	0.3			

The time step is commonly chosen as  $dt = 1/(20f_n)$ , where  $f_n$  is the highest natural frequency to be considered. However, as changing piezoelectric actuator size affects the beam's natural frequency, for all cases a fixed time step is used $dt = 0.005 \text{ sec} < 1/(20f_1)$ , where  $f_1$  is the first vibration mode of the structure. In the transient analysis, coefficients of Rayleigh damping are defined as  $\alpha = \beta = 0.001$ .

**Control Algorithm.** In this study a Direct Strain Feedback Control (DSFC) is utilized to calculate the required active voltage to the piezoelectric patch in order to damp out the unwanted vibrations. A smart beam under impact loading is shown in Fig. 2. An impact force in the form of a step,  $F_0=2$  N, is applied at the beam's tip. It is then removed during the subsequent steps. At each time step, the straine at the sensor locationis calculated from the finite element model. The reference input is zero in order to suppress the vibration.  $K_s$ ,  $K_c$  and  $K_v$  are the sensor, control and power amplification factors and are chosen to be 1000, 1000 and 5.5, respectively. In this study only the proportional control is considered. Deflection at beam's tip,  $D_t$  is observed and used in evaluating the performance of the control algorithm. The macro, which calculates the active voltage based on the applied closed control loop, is developed in ANSYS parametric design language and is given in Table 2.

*do,t,2*dt,tim,dt	Va =-235*Wa
Read Sensor Displacement Data	*endif
*get,U1,node,N1,u,x	Apply Piezoelectric Voltage
*get,U2,node,N2,u,x	cmsel,s,TOP
err=0-Ks*(U2-U1)/SIZ	d,all,volt,Va !Top Electrodes
Define Piezoelectric Voltage	allsel,all
Va=Kc*Kv*err	time,t
*if, Va,gt,235*Wa,then	solve
Va=235*Wa	*enddo
*elseif, Va,lt,-235*Wa,then	

Table 2 Direct Strain Feedback Control (DSFC) macro

#### **Design of Experiments**

The five parameters shown in Fig. 2,namely location  $(D_A)$ , length  $(L_A)$ , width  $(H_A)$  and thickness $(W_A)$  of piezoelectric patch and sensor's position  $(D_S)$  are the most influential factors which affect the performance of the control system. To find an optimum setting for these parameters, different levels are selected for each parameter as presented in Table 3.

Parameters	Levels of each parameter								
T arameters	Level 1	Level 2	Level 3	Level 4	Level 5				
Length of PZT patch	L <sub>A</sub>	50	75	100	125	150			
Width of PZT patch	H <sub>A</sub>	10	15	20	25	30			
Thickness of PZT patch	WA	1	1.5	2	2.5	3			
Actuator's distance from support	D <sub>A</sub>	0	15	30	45	60			
Sensor's distance from support	Ds	50	60	70	80	90			

Table 3Selected levels for the system setup parameters

\*all dimensions are in [mm]

The goal is to reach maximum damping ratio or minimum settling time. Based on Table 3, there are  $5^{5}=3125$  different configurations. It is not reasonable to carry out this number of experiments to find the optimum setup. Taguchi's L25 orthogonal array is used to produce only 25 experiments [13]. Taguchi method allows calculation of the optimal parameter levels with only 25 configurations.

#### **Results and Discussion**

**Finite Element Results**. Combinations of the L25 array are shown in Table 4. It shows ANSYS simulation results and corresponding outputs, damping ratio ( $\zeta$ ) and the settling time (T<sub>s</sub>).

Table 4 Simulation results obtained by finite element program based on Taguchi's L25 orthogonal

Test #	L <sub>A</sub>	H <sub>A</sub>	$W_A$	$D_A$	Ds	ζ	$T_{S}[s]$	Test #	L <sub>A</sub>	H <sub>A</sub>	WA	$D_A$	Ds	ζ	$T_{s}[s]$
1	50	10	1	0	50	0.0171	5.67	14	100	25	1	30	90	0.0524	1.81
2	50	15	1.5	15	60	0.0117	7.69	15	100	30	1.5	45	50	0.0162	5.10
3	50	20	2	30	70	0.0046	18.80	16	125	10	2.5	15	90	0.0124	5.72
4	50	25	2.5	45	80	0.0042	20.41	17	125	15	3	30	50	0.0076	9.21
5	50	30	3	60	90	0.0032	27.03	18	125	20	1	45	60	0.0518	1.89
6	75	10	1.5	30	80	0.0153	5.82	19	125	25	1.5	60	70	0.0226	3.76
7	75	15	2	45	90	0.0076	11.07	20	125	30	2	0	80	0.0217	3.05
8	75	20	2.5	60	50	0.0128	6.78	21	150	10	3	45	70	0.0085	8.56
9	75	25	3	0	60	0.0049	15.13	22	150	15	1	60	80	0.0426	2.33
10	75	30	1	15	70	0.0447	2.10	23	150	20	1.5	0	90	0.049	1.52
11	100	10	2	60	60	0.0142	6.09	24	150	25	2	15	50	0.0267	2.52
12	100	15	2.5	0	70	0.0111	6.36	25	150	30	2.5	30	60	0.0131	5.15
13	100	20	3	15	80	0.0063	11.22								

array

Damping ratio is calculated by means of logarithmic decrement with the following equations,

$$\delta = (1/n) \times (\ln (x_1/x_{n+1})).$$
(1)

$$\zeta = 1/ \left[ 1 + ((2\pi)/\delta)^2 \right]^{\frac{1}{2}}.$$
(2)

Where  $\delta$  is the logarithmic decrement,  $\zeta$  is damping ratio,  $x_1$  and  $x_{n+1}$  are the first and  $(n+1)^{\text{th}}$  peak amplitudes of the vibrations respectively. Settling time with two percent criterion is also calculated using the following equation,

$$T_s = 3.9/(\zeta w_n).$$
 (3)

**Taguchi** Analysis. Damping ratio ( $\zeta$ ) and settling time (T<sub>s</sub>) are considered as the outputs of each testin Table 4.TheSN (Signal to Noise) ratios for all levels of each parameter are calculated and shown in Tables 5 and 6.

Da: Ds

Response Table for Signal to Noise Ratios										
Larger is better										
Level	La	На	Wa	Da	Ds					
1	-43.63	-37.63	-28.21	-36.02	-36.57					
2	-37.95	-37.98	-33.97	-35.85	-37.03					
3	-36.30	-36.10	-38.16	-37.74	-37.43					
4	-34.48	-36.75	-40.05	-38.57	-37.71					
5	-32.83	-36.73	-44.78	-37.01	-36.44					
Range	10.80	1.88	16.57	2.72	1.26					
Rank	2	4	1	3	5					

Table 5Taguchi Analysis: ζ versus La; Ha; Wa; Table 6Taguchi Analysis: T<sub>s</sub> versus La; Ha; Wa; Da: Ds

Response Table for Signal to Noise Ratios											
	Smaller is better										
Level	La	На	Wa	Da	Ds						
1	-38.59	-31.94	-23.89	-29.58	-30.60						
2	-32.54	-32.23	-28.43	-29.64	-31.33						
3	-30.38	-30.42	-31.92	-31.86	-31.60						
4	-28.20	-30.87	-33.63	-33.05	-31.87						
5	-26.35	-30.60	-38.20	-31.93	-30.66						
Range	12.24	1.88	14.31	3.47	1.27						
Rank	2	4	1	3	5						

Referring to Table 5 and 6, levels with highest SN ratiosare selected as optimum levels. These configurations optimize both damping ratio and settling time as shown in Table 7. The variables thickness and length of the piezoelectric patch have the highest range and are therefore the most influential variables.

Optimization Criterion	L <sub>A</sub>	H <sub>A</sub>	W <sub>A</sub>	D <sub>A</sub>	D <sub>S</sub>
Maximum Damping Ratio	150	20	1	15	90
Minimum Settling Time	150	20	1	0	50

Table 7 Taguchi's suggested optimum configuration

Figures 3 and 4 present the outputs of all 25 tests from Table 4as well as the two suggested optimal cases, in terms of vibrations frequency. It is obvious that nearly 70% of L25 simulation outputs for damping ration are below 0.02. However, Taguchi has suggested a configuration with damping ratio greater than 0.075. Similarly, 60% of the L25 simulation outputs for settling time are greater than 5 seconds while Taguchi's S/N ratio analysis suggests a configuration which has a settling time of less than 1.5 seconds.Fig. 5 illustrates the response of the system for the two optimum configurations based on settling time and damping ratio. In these plots, vibrations of the system for the two optimum configurations are compared with and without the implementation of control loop.



Figure 5 Comparison of system's response with and without applying the optimum control setup

## Conclusion

Utilizing an efficient control methodalong with optimum selection of piezoelectric actuator and sensor dimensions, improves the functionality of smart structures in suppression of unwanted vibrations. In this paper, the optimal placement and sizing of piezoelectric actuator and sensor is obtained using Taguchi design of experiments method. According to S/N ratio plots, the thickness and length( $W_A$  and  $L_A$ ) of the piezoelectric patch have considerable influence in comparison with other parameters. It is shown that by applying the optimized active vibration control, the vibrations are dampedsignificantly faster. A combination of finite element solutions and optimization analysis based on design of experiments methods can help the designer to configure the smart structure efficiently without the need to perform extensive experiments.

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## Key Engineering Materials II

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