

Integration of strategic and operational attributes to calculate the optimal cultivation of crops

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ARTICLE INFO

Keywords:

Optimal cultivation
Multi-attribute optimization model (MAOM)
Sustainability
Risk-averse UTA (UTilité Additive)
Linear optimization model

ABSTRACT

Determining the optimal quantity of crops is crucial for establishing a sustainable cultivation pattern when multiple potential crops are available. To address this issue, we propose a novel hybrid multi-attribute optimization model (MAOM) based on two steps. Firstly, we calculate the sustainability score of candidate crops by taking into account strategic criteria categorized in terms of sustainability, including economic, social, and environmental dimensions. To ensure a more reliable choice, we develop a risk-averse UTA (UTilité Additive) to adjust the trade-off among the criteria of alternatives in multi-criteria decision-making (MCDM) problems. Secondly, we develop a linear optimization model to calculate the optimal amount of candidate crops based on the sustainability score and operational criteria. We employ this framework to determine the optimal cultivation pattern in Khorasan Razavi, Iran. The results suggest that Dried Garlic, Turnip, Forage, Millet, and Khasil are suitable crops for the six-month period of spring and summer, while Potato, Fodder Beet, Shah Seed, and Mung Bean are the optimal alternatives for the six-month period of autumn and winter among the 46 candidate crops. Finally, a conclusion is drawn and recommendations for further research are proposed.

1. Introduction

In recent years, agriculture's contribution to the global economy has been increasing, with its share in the gross domestic product (GDP) rising from 17.8% in 2019–20 to 19.9% in 2020–21 (Kapil, 2021). Agriculture has the potential to benefit the economy, society, and environment, but it can also have negative impacts on these areas if the wrong cultivation methods are used (Chen, Li, & Jin, 2016). Previous research on optimal cultivation patterns has mainly focused on operational criteria such as resource utilization optimization. However, there is growing awareness that sustainable agriculture requires the consideration of strategic criteria, including economic, social, and environmental factors (W. Chen et al., 2016).

Two main challenges make it difficult to include these strategic criteria in the agricultural decision-making process. Firstly, it requires the development of new models that can effectively balance multiple dimensions. Historically, decisions in agriculture have been based on operational criteria, such as the availability of workers and water. However, when strategic criteria such as environmental sustainability,

social impact, and economic viability are added, a more comprehensive approach is needed to help decision-makers find a good balance between these different factors. Additionally, different stakeholders may have different priorities and trade-offs between these dimensions, making it difficult to agree on the best way to grow crops. Farmers may prioritize maximizing their profits, while environmentalists may focus on reducing agriculture's impact on natural ecosystems. Consumers may prioritize the accessibility and affordability of certain crops, while government officials may be interested in promoting certain crops for their economic benefits. Achieving a harmonious balance between these various priorities and compromises requires a comprehensive strategy that considers the requirements and concerns of all stakeholders involved. Therefore, there is a dilemma in which the criteria associated with the two levels must be addressed.

As the first contribution, this study proposes a multi-attribute optimization model (MAOM) to consider both the strategic and operational levels. The proposed model can take into account a broad spectrum of criteria that have a significant impact on the selection process and incorporate experts' perspectives.

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<https://doi.org/10.1016/j.eswa.2023.121238>

Received 8 November 2022; Received in revised form 21 June 2023; Accepted 16 August 2023

Available online 25 August 2023

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Although multi-criteria decision-making (MCDM) methods have the potential to simplify decision-making, the trade-offs inherent in these methods may not result in appropriate choices in the long run, as the current literature suggests. MCDM methods may lead to the selection of an option with a higher weight in certain criteria, which may not be better in terms of other criteria. In other words, an alternative with strong performance in a few criteria may hide its weaknesses in other criteria (Wang, 2012). The allowance of unrestricted trade-offs between the criteria of each alternative, which is permissible in compensatory MCDM methods, may lead to the overlooking of a better alternative that aligns with decision-makers' preferences (Kheybari, 2021; Kheybari & Ishizaka, 2022). Therefore, in MCDM problems, it is essential to consider decision-makers' preferences while avoiding being excessively swayed by higher-weighted preferences. Reducing the risks associated with trade-offs in MCDM methods is of utmost importance. A sophisticated method to achieve this objective is to emphasize the shortcomings of each option during the assessment process. For this purpose, this paper proposes a risk-averse UTA (UTilité Additive) model in a two-level framework to determine the optimal cultivation pattern, which is the second contribution of this paper. The proposed model is used to compare different crops at the strategic level, and the optimal level of cultivation for each crop is calculated based on operational constraints using the score of each crop as a parameter of the objective function. Finally, the developed model is applied to a real case in Iran.

Taking into account the reasons discussed and the literature reviewed, this investigation seeks to:

- propose a more comprehensive framework of criteria classified as economic, social, and environmental dimensions;
- propose a risk-averse UTA method to calculate the weights of criteria at the strategic level that applies to multi-criteria problems;
- propose an MAOM using the output of a risk-averse UTA and considering operational criteria to determine the optimal cultivation pattern; and
- evaluate the proposed framework in a real-world case study.

The structure of this study is as follows: Section 2 reviews the literature on the cultivation pattern problem and identifies research gaps. Section 3 outlines the methodology employed in this investigation. Section 4 details the case study. Section 5 presents the results of applying the proposed methodology to the case study. Section 6 provides managerial implications for the proposed methodology. Finally, Section 7 offers conclusions and suggestions for future research.

2. Literature review

In order to develop the proposed framework, we conducted an investigation of studies attempting to address and solve the problem of optimal cultivation patterns. As we aimed to identify criteria at both the strategic and operational levels, we reviewed papers that employed Multi-Attribute Decision-Making (MADM) methods as methodologies. It is noteworthy that the text and tables of the studies were used to identify criteria at the two levels employed in the text.

Studies on the selection of optimal cultivation patterns using MCDM techniques can be classified into two main categories: Multi-Objective Decision Making (MODM) and MADM. Most studies have focused on two primary objectives: maximizing net returns from the proposed cultivation pattern and minimizing costs associated with the selected cultivation pattern. However, depending on the case being studied, individual scholars may have adopted other objectives (Sarker & Quaddus, 2002). MODM is the most commonly employed method in the literature, and it can be divided into two classes: Class A, which comprises studies that have employed multi-objective programming, and Class B, which encompasses those that have utilized single-objective programming.

As an example of the studies in class A Mainuddin, Gupta, and Onta

(1997) proposed an optimal cropping plan with a multi-objective analysis using the Analytic Hierarchy Process (AHP) in Thailand, with the aim of maximizing both economic net benefit and irrigated area while taking into account the preferences of the decision makers. Ren et al. (2019) proposed a multi-objective stochastic fuzzy programming and AHP method for agricultural water and land optimization allocation in China, considering multiple uncertainties. The objectives of the model were to maximize net benefit, agricultural water productivity, and minimize irrigation area. The model was tested under multiple uncertainties related to a water shortage, and the results provided decision makers with the optimal water irrigation level and land resources. Regulwar and Gurav (2011) proposed a multi-objective fuzzy linear programming (MOFLP) approach to irrigation planning under uncertainty in India, with the objectives of net benefits, crop/ yield production, employment generation/labor requirement, and manure utilization. The fuzzy concept was employed to account for uncertainty in the proposed model. Daghighi, Nahvi, and Kim (2017) proposed a multi-objective linear programming model for the purpose of locating an optimal cultivation pattern in Fars Province, Iran. This water resources planning model was designed to assist decision-makers in selecting an appropriate cultivation pattern, optimizing the exploitation of surface water resources, and determining the method of allocating water across different farm crops while minimizing the negative impacts of water scarcity.

As an example of the studies falling into class B, O. Heady (1954) employed a simplified linear programming approach to identify an optimal crop pattern, with the aim of determining the most profitable crop within the confines of land, capital, cultivation capacity, and labor. Itoh, Ishii, and Nansaki (2003) developed a linear model that accounted for the fuzziness and randomness of land and labor resources. Abedi, Peykani, and Kalashami (2011) employed a linear programming (LP) approach to assess the comparative advantage of corn in comparison to other competitor crops in optimal cultivation patterns in Kermanshah province, Iran. The performance of eight different crops was evaluated under two scenarios (with and without rotation) in eight states of Kermanshah. The results indicated that corn had a comparative advantage in all the states. Abedi et al. (2011) employed a LP approach to assess the comparative advantage of corn in comparison to other competitor crops in optimal cultivation patterns in Kermanshah province, Iran. The performance of eight different crops was evaluated under two scenarios (the existence and lack of rotation) in eight states of Kermanshah. The results indicated that corn had a comparative advantage in all the states.

Singh, Jaiswal, Reddy, Singh, and Bhandarkar (2001) developed a linear programming model to determine an optimal cropping pattern with respect to different water availability levels in India, with the objective of maximizing net return. The results indicated that wheat provided the most consistent profit among the eight crops. Garg and Dadhich (2014) conducted an investigation into an integrated non-linear single-objective mathematical model for optimal cropping pattern and irrigation scheduling under deficit irrigation. Variables such as deficit levels were incorporated into the model in order to maximize the net return. The results indicated that the optimal net financial return was increased by 92.5%, and the total optimal cropped area was enhanced by 109.7%. Additionally, there have been a few studies that have considered both single and multi-object. For example, Amini Fasakhodi, Nouri, and Amini (2010) proposed a Multi-Objective Fractional Goal Programming (MOFGP) approach to identify an optimal crop pattern in agricultural systems, with the aim of maximizing two ratios concurrently: net return/water consumption and labor employment/water consumption. The results indicated that the MOFGP solution was more advantageous than both Fuzzy Programming (FP) and LP models. Sarker and Quaddus (2002) conducted a study to explore the application of both single- and multi-objective models to address a nationwide crop-planning problem. They demonstrated how the information obtained from LP models can be incorporated into its goal programming (GP) counterpart to provide enhanced insights and decision support in a

Table 1
A comparison between our study to the most relevant ones in literature.

| Studies | Eco. | Soc. | Env. | Technique(s) used | Risk of Decision Maker's (DM's) attitude |
|--------------------------------|------|------|------|---|--|
| Huang and Zhang (2020) | ✓ | ✓ | × | AHP, Fuzzy TOPSIS | Not considered |
| Honar et al. (2021) | × | ✓ | ✓ | AHP, TOPSIS, PROMETHEE, ELimination and ChoiceExpressingReality (ELECTRE) | Not considered |
| Mainuddin et al. (1997) | × | × | ✓ | AHP | Not considered |
| Amini Fasakhodi et al. (2010) | × | × | ✓ | Multi-objective Fractional Goal Programming | Not considered |
| Ren, Li, and Zhang (2019) | × | × | ✓ | Multi-objective Fuzzy Stochastic Programming | Not considered |
| Devatha and Thalla (2019) | × | × | ✓ | SAW, WPM, TOPSIS, PROMETHEE | Not considered |
| Agha et al. (2012) | × | × | ✓ | AHP, PROMETHEE | Not considered |
| Mohammadian and Heydari (2019) | × | × | ✓ | Fuzzy Goal Programming | Not considered |
| Daghighi et al. (2017) | × | × | ✓ | Linear Programming | Not considered |
| Singh et al. (2001) | ✓ | ✓ | ✓ | Linear programming | Not considered |
| Chen et al. (2021) | × | × | ✓ | Two-way ANOVA and optimization | Not considered |
| Sedighkia et al. (2023) | × | × | ✓ | Regression and Genetic Algorithm | Not considered |
| Hasanzadeh Saray et al. (2022) | × | × | ✓ | Regression Analysis and Mixed Integer Linear Programming | Not considered |
| Tofighy et al. (2005) | ✓ | × | × | Bayesian information criterion and smooth filters | Not considered |
| This study | ✓ | ✓ | ✓ | UTA, risk-averse UTA, Linear Programming | Considered |

third-world country.

Despite the fact that MADM methods consider both quantitative and qualitative criteria in the decision-making process, including the selection of optimal cultivation patterns, there are fewer studies that address this problem using MADM methods. Furthermore, MADM techniques encompass a wide range of criteria compared to mathematical programming models, as the latter are more likely to result in a lack of feasible regions for the problem when a high number of variables and constraints are present. This constraint does not exist in. As a result, the utilization of MADM methods has been found to provide a more diverse and widespread set of criteria than those offered by mathematical programming models. Studies concerning cultivation patterns with a MADM approach have taken into account criteria that are closely related

to economic, social, psychological, and cultural factors. For instance, Devatha and Thalla (2019) employed four MADM methods, namely Simple Additive Weighting (SAW), Weighted Product Method (WPM), Preference Ranking Organization Method for Enrichment Evaluations (PROMETHEE), and Technique for Order Preference by Similarity to Ideal Solution (TOPSIS), to prioritize cropping alternatives in India. The results obtained by the MADM methods were compared to those of a non-linear optimization model, with wheat identified as the most profitable crop. Agha, Nofal, and Nassar (2012) used AHP and PROMPTEE to address the cultivation pattern problem for government lands in the Gaza Strip under both normal and resistant economic conditions. Their objective was to rank crops based on economic, financial, marketing, environmental, technical, political, and social criteria. Huang and Zhang

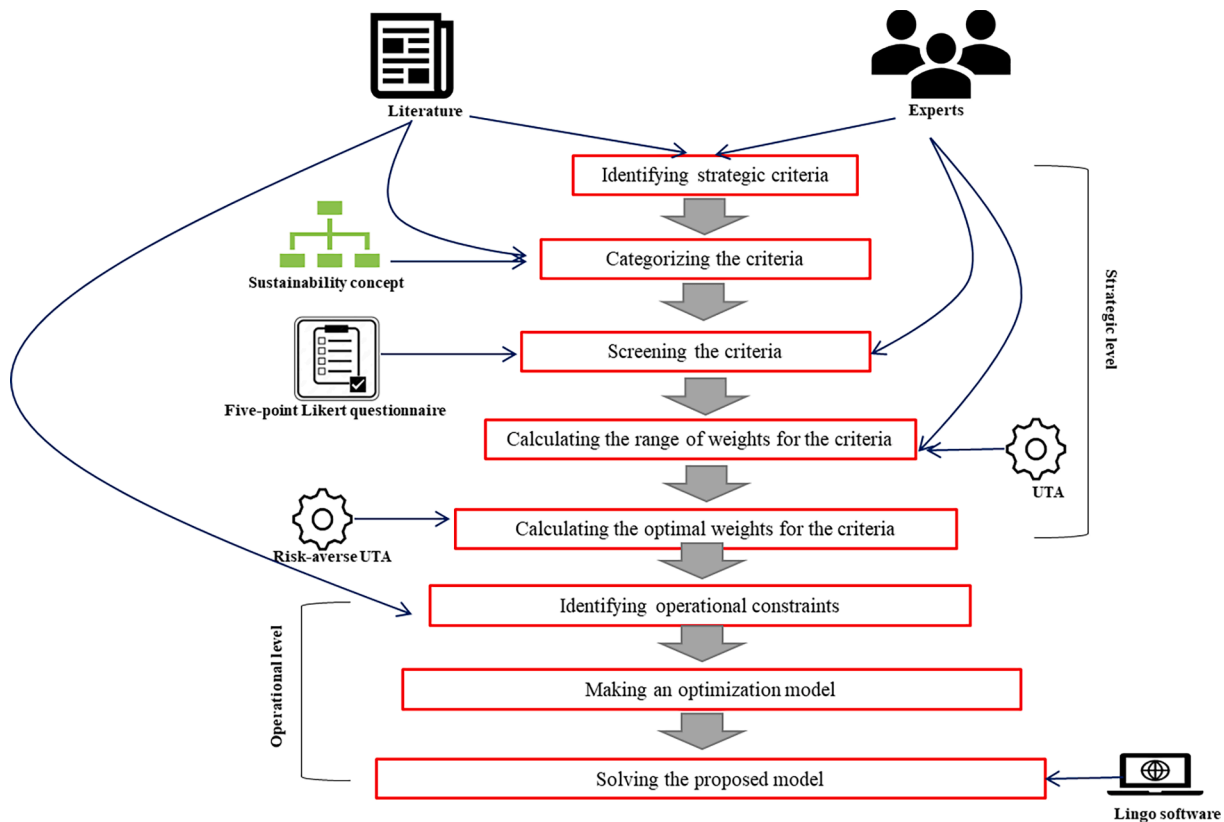


Fig. 1. Research Steps.

(2020) proposed an optimal economic crop model that combined AHP for generating criteria weights and Fuzzy TOPSIS for ranking crops to improve farmers' income and soil and water conservation in Taiwan. The study found that palm was the optimal crop.

Additionally, there is a body of research that examines the use of Statistical Analysis for the purpose of optimizing cultivation. An overview of this stream was conducted by Wu et al. (2022). Furthermore, Sedighkia et al. (2022) proposed an integrated optimization framework for agricultural planning that links an environmental flow model, drought analysis, a cropping pattern model, and deficit irrigation functions using regression models. The framework incorporates a genetic algorithm to generate an optimal plan for cropping patterns and irrigation supply that minimizes ecological impacts on the river ecosystem. The model is capable of minimizing ecological impacts on the river ecosystem in all hydrological conditions while also providing a sustainable plan for agricultural and environmental management.

Contemplating the studies in the literature, we found the following research gaps:

- Research conducted to date has largely been quantitative in nature, utilizing MCDM methods and not taking into account qualitative criteria, which require MADM techniques. Additionally, while some studies have employed statistical analysis to assess quantitative criteria, few have considered qualitative criteria, and none have considered both quantitative and qualitative criteria simultaneously. Previous research has addressed the economic, social, and environmental dimensions associated with the strategic level but has not utilized the output of the strategic level at the operational level or has simply considered the operational level while disregarding the strategic level. However, our study has not only implemented the strategic level but has also employed its output for the operational level, which has been demonstrated by a MAOM. Consequently, it encompasses a greater number of criteria. Additionally, several studies that have incorporated environmental criteria into their statistical analysis have neglected to consider the risk factor in their optimization problem ((J.-H. Chen et al., 2021), (Sedighkia, Fathi, Razavi, & Abdoli, 2023), (Saray et al., 2022)).
- According to the sustainability framework, although a long-lasting cultivation should be beneficial in terms of economy, society, and environment, there is a lack of research in the literature that comprises sustainability with detailed criteria for optimal cultivation selection. For example, Huang and Zhang (2020) considered soil and water conservation as two elements of sustainability for social and economic aspects, while Honar, Ghazali, and Nikoo (2021) examined the social and economic aspects of cultivation patterns from the perspective of stockholders. Additionally, Mainuddin et al. (1997) and Amini Fasakhodi et al. (2010) have both studied water management as an environmental criterion in sustainability. As a result, the effective criteria have been divided into three categories: those associated with human beings, society, and governmental regulations are categorized as society factors; those that either improve or worsen the environment are categorized as environmental factors; and the remaining criteria are considered economic criteria.
- As presented in Table 1, Singh et al. (2001) is the only work in the literature that considers all three dimensions of the cultivation pattern problem. However, this work does not consider the risk involved in weighing criteria or the opinions of decision-makers. Our study has addressed this shortcoming by including all sustainable dimensions, demonstrating the comprehensiveness of our investigation.

3. Methodology

The research depicted in Fig. 1 comprises eight steps. The first four steps, which concern the introduction and literature sections, are related to the strategic level. The modeling step, which is based on the output of

a risk-averse UTA and optimization model, is associated with the operational level. Consequently, the proposed framework, MAOM, encompasses both the strategic and operational levels.

At the strategic level, relevant criteria were initially extracted from previous studies in the literature. Subsequently, experts were asked to provide their preferred criteria using a five-point Likert scale. Criteria were screened based on a threshold for the coefficient of variation (CV) of the scored criteria. After experimenting with a range of threshold values, a threshold of 3.2 was chosen as it ensured the number of sub-criteria within each dimension was balanced in comparison to other dimensions (Salamirad, Kheybari, Ishizaka, & Farazmand, 2023). After the screening of criteria, the same experts were asked to select their top five crops and rank them among all those cultivable in Khorasan Razavi province. The number five was selected to provide the experts with an appropriate level of discrimination power. A high number of chosen crops can make it difficult for the experts to differentiate between them, while a low number may lead to an inadequate level of accuracy. In the subsequent step, the experts' priorities were provided to the UTA to obtain a range for the weight of each criterion. A risk-averse UTA was developed to identify the optimal weights of the criteria. These weights were then used to calculate the sustainability score of the candidate crops. Finally, after reviewing the literature on optimal cultivation selection, operational constraints were extracted.

In the operational step, a linear optimization problem was formulated to identify the optimal amount of cultivation for each crop, utilizing the output of the risk-averse UTA as coefficients of the objective function. This step was crucial, as operational constraints such as water, area, and human or machine resources had to be taken into account when cultivating crops that had been identified as sustainable at the strategic level. The mathematical model was solved using LINGO. In the following subsections, we provide a detailed account of each step.

3.1. UTAa

The UTilité Additive (UTA) was initially proposed by Acquet-Lagrezze and Siskos (Jacquet-Lagrezze & Siskos, 1982) in 1981. UTA can be used to prioritize different performance metrics that are important for the nonlinear service system, such as customer satisfaction, service quality, and efficiency. The weights of these metrics can be determined based on expert judgment or through a survey of system users. UTA can then be used to rank different control strategies based on their performance on these metrics, which can be used to select the best strategy for the nonlinear service system. The purpose of UTA is to identify the decision maker's preference model within the criteria involved in decision making, so that the output generated by its application is most similar to the actual decisions made. The utilization of the summability utility model as a methodology for MADM problems has been demonstrated in several studies. This model requires the decision-maker to prioritize a reference set of options according to their preferences (Beuthe & Scannela, 2001). This has been demonstrated to be effective in addressing the issue of dependent criteria when estimating a utility function. This model is able to solve the problem of having dependent criteria while estimating the utility function. Providing sensitivity analysis on the optimal answer is another advantage of this method. This method has many applications for ranking alternatives in many areas, such as selection material in engineering (Athawale, Kumar, & Chakraborty, 2011) and road building (Rezaeinia, 2022).

There are several studies extending the UTA method. For example, Angilella, Greco, Lamantia, and Matarazzo (2004) developed a non-additive utility function in the framework of the so-called fuzzy integrals, which permits modeling preference structures of Decision Makers (DMs) with interaction between criteria. Or Chhipi-Shrestha, Kaur, Hewage, and Sadiq (2018) proposed a UTA where conflicting criteria can be considered. However, there is no study about UTA extension where the risk attitude of DMs during their ranking process is considered. We explain in the next sub-section how we extend UTA such

that it can consider risk in the evaluation process. We extended the UTA method proposed and applied in the literature (Angilella et al., 2004; Chhipi-Shrestha et al., 2018; Rezaeinia, 2022) by considering the risk-averseness of DMs in the weighting process, as explained in the next sub-section. Moreover, we discuss the details of the UTA model in Appendix A.

3.2. Risk-averse UTA

In the evaluation process, decision makers often seek to minimize the weaknesses of alternatives. To this end, the developed risk-averse UTA model highlights the weaknesses of each alternative by seeking the best weight in the possible range for each criterion. To further emphasize the weaknesses of alternatives, the concept of Data Envelopment Analysis (DEA) is utilized in the risk-averse UTA model. The optimization model (1) is conducted to obtain weights that emphasize the shortcomings of the alternatives, thus avoiding the application of a single set of weights to all alternatives.

$$\text{Minimize } \sum_j w_{ij} u_{ij}$$

Subject to:

$$\sum_j w_{ij} = 1 \forall i$$

$$w_j^{*l} \leq w_{ij} \leq w_j^{*u} \forall j \tag{1}$$

Model 1 presents the risk-aversion rationale as a method of selecting the optimal weight point by minimizing the output of alternatives. The proposed model ensures that the chosen alternative surpasses any criterion whose weight is set to the lowest possible value. In other words, by controlling the trade-off, the risk of the evaluation is reduced. w_{ij} is the weight of criterion j for the alternative i , and w_j^{*u} and w_j^{*l} are the upper and lower bounds of criterion j (c_j) calculated by the UTA. u_{ij} is the normalized value of alternative i for criterion j which are calculated by Eqs. (2) and (3).

$$u_{ij} = \frac{x_{ij} - \min_i(x_{ij})}{\max_i(x_{ij}) - \min_i(x_{ij})} \forall i \text{ and positive } j \tag{2}$$

$$u_{ij} = \frac{\max_i(x_{ij}) - x_{ij}}{\max_i(x_{ij}) - \min_i(x_{ij})} \forall i \text{ and negative } j \tag{3}$$

where x_{ij} indicates the score of alternative i in criterion j .

Finally, the candidate alternatives were ranked by calculating the overall score of the alternative using the simple weighted sum function presented in Eq. (4).

$$s_i = \sum_j u_{ij} w_{ij} \forall i \tag{4}$$

3.3. Optimal cultivation model

In this section, the aim is to identify an optimal set of crops. To achieve this aim, the year of cultivation is divided into two six-month periods. Based on the experts' opinion, potential crops for each season are grouped and considered as candidates for cultivation. Prior to presenting the linear mathematical model, the parameters and decision variables are defined.

Notations

There are two groups of crops to be cultivated because warmness and

coolness of weather directly affect the behavior of crops. This classification has been recognized by the experts.

Indices

i : Set of crops for cultivation ($i \in I$)

j : Set of cities ($j \in J$)

Parameters.

D_i : A vector showing the upper level of demand for crop i (measured by kilogram per square meter).

a_i : A vector illustrating the area required to cultivate one unite of crop i (measured by square meter per kilogram).

AT_j : A vector showing the available area in city j (measured by square meter).

p_i : A vector showing the required power supplied by human and machine resources to cultivate one unite of crop i (measured by horse power per hour).

PT_j : A vector illustrating the available power supplied by human and machine resources in city j (measured by horse power per hour).

w_t : A vector illustrating shows the water amount required to cultivate one unite of crop i (measured by cubic meter per kilogram).

WT_j : A vector illustrating the available amount of water in city j (measured by cubic meter).

s_i : A vector showing the suitability index obtained by cultivating one unit of crop i .

Decision Variables

x_{ij} : A matrix illustrating the amount of crop i that is cultivated in city j .

Objective function.

We consider a single-objective function. Equation (5) calculates the total sustainability obtained by cultivated crops.

$$\text{Maximize } \sum_i \sum_j s_i x_{ij} \tag{5}$$

Constraints.

To consider limitations of the cultivation pattern, we have the following constrains:

The set of constraints (6) expresses upper bound demand for each crop. The constraints guarantee that at most how much from each crop should be cultivated.

$$\sum_j x_{ij} \leq D_i \forall i \tag{6}$$

The set of constrains (7) states the available power supplied by human and machine resources in each city. These constraints guarantee that the consumed machine and human resources do not exceed their available counterparts in each city. In fact, each city has a limited number of machine and human resources that must be considered when a crop is to be cultivated.

$$\sum_i p_i x_{ij} \leq PT_j \forall j \tag{7}$$

The set of constraints (8) denotes the amount of available water in each city. These constraints guarantee that the consumed machine resources do not exceed their available counterpart resources.

$$\sum_i w_t x_{ij} \leq WT_j \forall j \tag{8}$$

The set of constraints (9) expresses the available area in each city. These constraints guarantee that the available land limit for each city has been considered.

$$\sum_i a_i x_{ij} \leq AT_j \forall j \tag{9}$$

4. Case study

According to the report of the World Bank in 2017, the labor

Table 2
Experts information.

| Respondents | Faculty member | Experienced farmer | Average years of work experience |
|-----------------------|----------------|--------------------|----------------------------------|
| Screening criteria | 12 | 8 | 12.6 |
| Filling questionnaire | 6 | 2 | 15.5 |

proportion of the agriculture sector to the total number of employed people in the world is equal to 26.5% while this proportion has been estimated at 17.6% in Iran based on Iran Statistics Center (The World Bank (2021), 2021). Specifically, our case study has been conducted in Khorasan Razavi, which is one of the top five provinces in Iran when it comes to talking about the most arable area. Khorasan Razavi is a province located in northeastern Iran. Mashhad is the center and capital of the province. This province has a population of 6,434,501 and has 33 cities. It is also the second-largest province in Iran. The area of the province is 118,854 square kilometers, which makes it the fifth largest province in Iran and occupies seven percent of the area of Iran.

Even though the province has numerous advantages, its agriculture industry has faced some difficulties in choosing which crops to cultivate because of the water shortage crisis and environmental challenges over the last decade. In addition, according to the Mashhad University of Medical Sciences statistics, this province has been tremendously involved in the COVID-19 outbreak from 2020 to 2022. Hence, its

human resource availability has become a serious concern for the agriculture industry in this province. As a result, a sustainable cultivation pattern would be extremely advantageous for this province. It goes without saying that similar provinces can be benefited by our proposed sustainable framework. The potential crops for cultivation are collected by using an online questionnaire, and then experts give the score of each crop with respect to the criteria. Subsequently, the optimal weights are calculated, and then the optimal amount of crops is determined.

4.1. Data collection

Generally speaking, data sources in our paper are divided into two classes. Data of the UTA method that is gathered by experts' opinions as mentioned in Table 2. The data enables us to calculate the weight of each criteria. In the second group of data, which is considered the strategic level of our investigation, we have used data from the Statistical Center of Iran (2022) and Ministry of Agriculture (2022). To run the optimization model, which is actually the operational level of our study, we obtained the data for the model's parameters by using the Statistical Center of Iran and the Ministry of Agriculture of Jihad.

We regarded the opinion of Khorasan Razavi Agricultural Jihad experts and researchers of the department of agriculture, Ferdowsi University of Mashhad. The number of experts is 20, all of whom are adept, as detailed information provided in Table 2 about their expertise and work experience attests. To have access to and exchange information with the experts, we have utilized their online profiles. We asked the

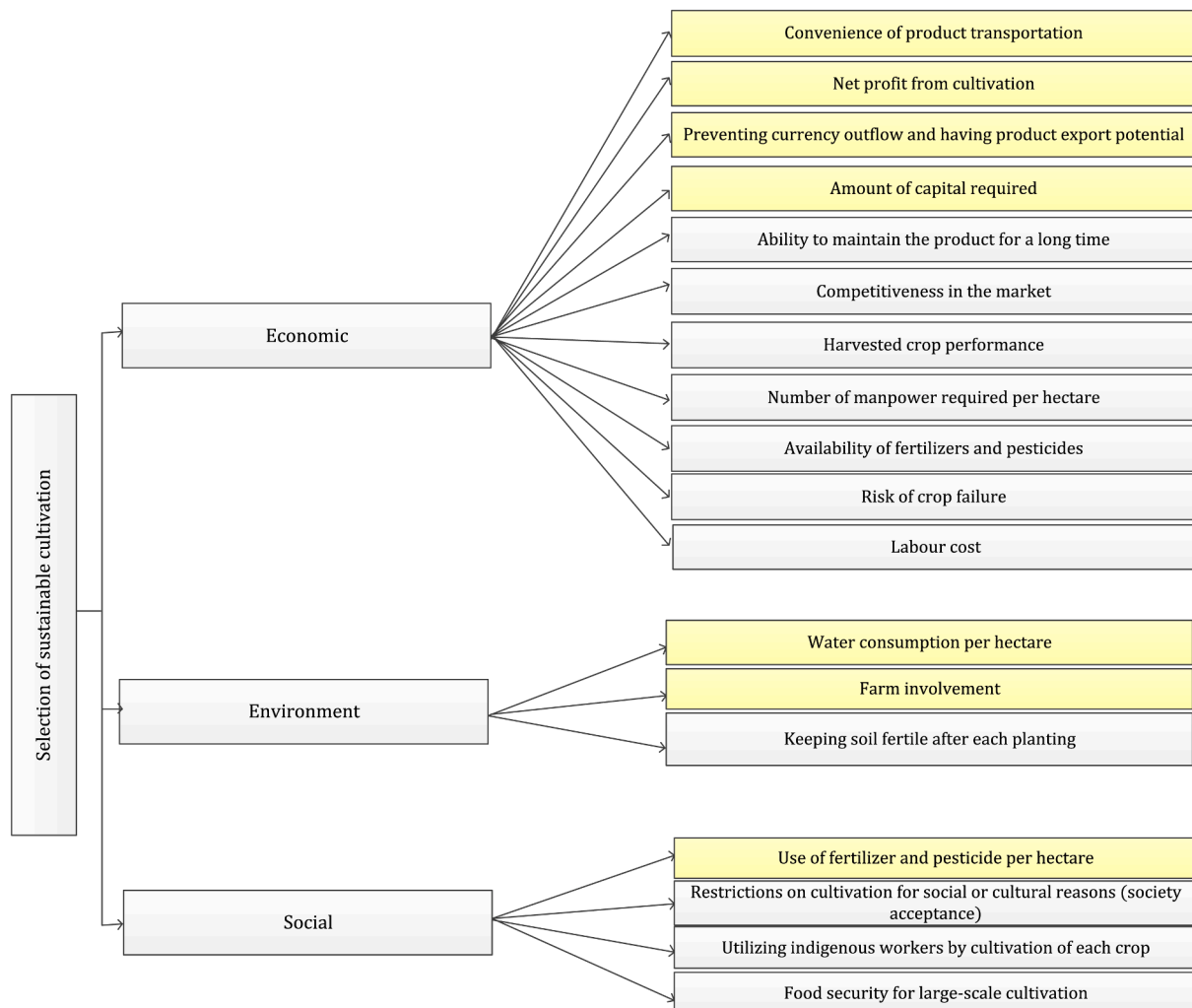


Fig. 2. Screened criteria in terms of sustainable cultivation.

Table 3
Upper and lower bounds of criteria.

| Criterion | Lower bound | Upper bound | Weight (middle) | Rank |
|--|-------------|-------------|-----------------|------|
| Net profit from cultivation (C_1) | 0 | 0.7243 | 0.3621 | 3 |
| Amount of capital required (C_2) | 0 | 0.4438 | 0.2219 | 6 |
| Usage of fertilizer and pesticide per hectare (C_3) | 0 | 0.4440 | 0.2220 | 5 |
| Convenience of crop cultivation (C_4) | 0 | 0.9034 | 0.4517 | 1 |
| Farm involvement (C_5) | 0 | 0.4356 | 0.2178 | 7 |
| Water consumption per hectare (C_6) | 0 | 0.9020 | 0.4510 | 2 |
| Preventing currency outflow and having crop export potential (C_7) | 0 | 0.4918 | 0.2459 | 4 |

Table 4
Weight of each dimension.

| Main Level | Weight | Rank |
|-----------------------|--------|------|
| Economic dimension | 0.5899 | 1 |
| Social dimension | 0.1022 | 3 |
| Environment dimension | 0.3079 | 2 |

experts to identify any missing criteria that we had not covered in the literature. In this step, we gave the criteria in the three dimensions (economy, society, and environment) as mentioned in Section 2. Then, we asked the experts to score the criteria by filling out a questionnaire based on a five-point Likert scale, with 1 being the lowest and 5 being the highest.

4.2. Criteria screening

Following data collection, criteria screening was conducted to optimize the reliability of comparisons between criteria (Kheybari, Ishizaka, & Salami-rad, 2021; Kheybari, 2023) and to enhance the discrimination power of the experts (Wanke, Barros, & Emrouznejad, 2016). Using a threshold of 3.2 for the coefficient of variation (CV) measure, we selected seven criteria (out of 19), which are highlighted in yellow in Fig. 2.

5. Results and discussion

In this section, the local weights of the criteria at each main level are calculated. The UTA stipulates the optimal range of the weights for any criterion by averaging the intervals obtained from the experts' opinions. To analyze the experts' opinions, we selected the middle of the optimal ranges as the local weight of their corresponding criteria. In order to determine the optimal weight, the output of the risk-averse UTA is utilized as the objective function coefficients of the mathematical model proposed in Section 3.2. For more detailed investigation, the codes related to original UTA, risk-averse UTA, and MAOM can be seen in Online Appendix, respectively.

5.1. Local weight of criteria

After the UTA model has been used, the lower and upper limits of each criterion are found by taking the minimum and maximum weights from the UTA. Subsequently, the mean of the lower and upper bounds is calculated (Table 3). As mentioned, the mean value of the lower and upper bounds is utilized to analyze the weights.

Table 4 presents the weights of the three sustainability dimensions. The weight of each main dimensions is determined by summing its corresponding sub-level weights. For instance, the economic dimension score is calculated by summing the weights of its respective components.

As C_1 (net profit from cultivation), C_2 (amount of capital required), C_4 (convenience of crop cultivation), and C_7 (preventing currency outflow and having crop export potential) are associated with the economic dimension, the score is equal to 0.5899. The economic dimension has been given the highest priority out of the three. This may be because of the sanctions put on Iran, which have stopped agricultural centers from using modern technology. It may also be because of a lack of investment, traditional farming, and a weak economy, which has made it much harder to take risks.

Table 3 demonstrates that C_4 (convenience of crop cultivation) is of the highest importance among the economic sub-criteria due to the fact that transportation cost is a major factor for crop cultivation in Khorasan Razavi. Furthermore, the quality of crops for export necessitates that suppliers pay the utmost attention to the appearance of the crop. Since C_5 (farm involvement) and C_6 (water consumption per hectare) are both components of the environment dimension, its score is equal to 0.3079. As shown in Table 3, C_6 (Water consumption per hectare) has more weight than C_5 (farm involvement) mainly because Khorasan Razavi is considered to have a cold semi-arid climate, meaning that it has a low rate of rain. On the other hand, since it is a wide province, C_5 (farm involvement) is not a big issue. Finally, since only C_3 (usage of fertilizer and pesticide per hectare) belongs to the social dimension, its score is equal to 0.1022.

5.2. Optimal weight of criteria and alternative assessment

In this section, the crops are evaluated using the optimal weight of criteria obtained from risk-averse UTA. The optimal weight of the criteria can be calculated using the risk-averse UTA by utilizing the optimal range of weight of criteria (Table 3) and the normalized decision matrix (Table A in Appendix B). Examination of Table 5 reveals that the opinions of experts are most consistent in C_2 compared to the other criteria. In fact, sample standard deviations for C_1 to C_7 are 0.0357, 0.0024, 0.0218, 0.0702, 0.0062, 0.0519, and 0.0155, respectively.

Table 6 presents the overall score of the risk-averse UTA, which is obtained by the summation of the resulting weights for each crop (Equation (4)). Additionally, the overall score of the original UTA for each crop is calculated by taking the average score of eight experts. Upon examining Table 6, it can be seen that A_7 , A_{35} , and A_{11} are the top three crops in terms of risk-averse UTA overall scores, while A_5 , A_1 , and A_{46} are the bottom three among the 46 crops.

5.3. Analyzing the results of risk-averse UTA and original UTA

Discussion of the rankings of A_{29} and A_{32} is conducted in order to analyze the outcomes of the suggested methodology. When the risk-averse UTA was applied, the rank of A_{29} shifted from 8 to 15, while the rank of A_{32} moved from 20 to 14. This suggests that, when the risk-averse factor is taken into account in the initial ranking, criteria with weaker performance in the original UTA can outperform in the risk-averse condition. As illustrated in Fig. 3, A_{29} outperforms A_{32} for more than half of the criteria (five out of seven; C_1 , C_3 , C_5 , C_6 , and C_7); however, A_{29} performs significantly weaker in C_2 and C_4 .

The results presented in Table 6 demonstrate that the weaknesses of A_{29} were not taken into account in the assessment process with the original UTA, resulting in A_{29} obtaining a higher rank than A_{32} (rank 8 versus rank 20). To address this issue and prevent any irreversible consequences, the risk-averse UTA emphasizes the weaknesses of alternatives in the optimal range of weights determined by the original UTA. To put it in other words, the risk-averse UTA model gives the upper bound of the weight to the criteria where the crops do not outperform and underrates the other criteria. In this vein, as depicted in Fig. 4, by lowering the weight of the criteria where the alternatives (crops) outperform (i.e. C_1 , C_3 , C_5 , C_6 , and C_7 for A_{29} and C_2 and C_4 for A_{32}) and adding it to the criteria where the crops perform poorly (i.e. C_2 and C_4 for A_{29} and C_1 , C_3 , C_5 , C_6 , and C_7 for A_{32}), we are able to magnify the weaknesses of alternatives in the weight range determined by the

Table 5
Optimal weights obtained by using risk-averse UTA.

| Crops | C ₁ | C ₂ | C ₃ | C ₄ | C ₅ | C ₆ | C ₇ |
|--|----------------|----------------|----------------|----------------|----------------|----------------|----------------|
| Baghala (A ₁) | 0.1083 | 0.0102 | 0.0122 | 0.5038 | 0.0670 | 0.1407 | 0.1577 |
| Onion (A ₂) | 0.1083 | 0.0102 | 0.0122 | 0.5038 | 0.0670 | 0.1407 | 0.1577 |
| Tomato (A ₃) | 0.1037 | 0.0148 | 0.0122 | 0.5038 | 0.0670 | 0.1407 | 0.1577 |
| Red pepper (A ₄) | 0.1704 | 0.0102 | 0.0122 | 0.3499 | 0.0670 | 0.2265 | 0.1637 |
| Leafy vegetables (A ₅) | 0.1083 | 0.0102 | 0.0122 | 0.5038 | 0.0670 | 0.1407 | 0.1577 |
| Glandular vegetables (A ₆) | 0.1704 | 0.0102 | 0.0122 | 0.4357 | 0.0670 | 0.1407 | 0.1637 |
| Potato (A ₇) | 0.1704 | 0.0148 | 0.0323 | 0.3224 | 0.0744 | 0.2219 | 0.1637 |
| Dried garlic (A ₈) | 0.0649 | 0.0102 | 0.0122 | 0.5034 | 0.0674 | 0.2196 | 0.1222 |
| Sangolak (A ₉) | 0.1083 | 0.0102 | 0.0511 | 0.5038 | 0.0740 | 0.0948 | 0.1577 |
| Clover (A ₁₀) | 0.1365 | 0.0102 | 0.0122 | 0.3499 | 0.0670 | 0.2627 | 0.1615 |
| Turnip and forage (A ₁₁) | 0.1704 | 0.0079 | 0.0511 | 0.4357 | 0.0740 | 0.0971 | 0.1637 |
| Carrots (A ₁₂) | 0.1083 | 0.0079 | 0.0511 | 0.5038 | 0.0740 | 0.0971 | 0.1577 |
| Millet (A ₁₃) | 0.1704 | 0.0079 | 0.0122 | 0.3499 | 0.0693 | 0.2265 | 0.1637 |
| Khasil (A ₁₄) | 0.1960 | 0.0079 | 0.0122 | 0.4357 | 0.0693 | 0.1407 | 0.1381 |
| Fodder beet (A ₁₅) | 0.1704 | 0.0079 | 0.0122 | 0.3499 | 0.0693 | 0.2265 | 0.1637 |
| Fodder Corn (A ₁₆) | 0.1704 | 0.0148 | 0.0122 | 0.3499 | 0.0670 | 0.2219 | 0.1637 |
| Cluster Corn (A ₁₇) | 0.1195 | 0.0079 | 0.1342 | 0.3751 | 0.1030 | 0.0971 | 0.1631 |
| Alfalfa (A ₁₈) | 0.1704 | 0.0148 | 0.0122 | 0.3499 | 0.0670 | 0.2219 | 0.1637 |
| Corn (A ₁₉) | 0.1037 | 0.0148 | 0.0122 | 0.5038 | 0.0670 | 0.1407 | 0.1577 |
| Khakshir (A ₂₀) | 0.1083 | 0.0102 | 0.0122 | 0.5038 | 0.0670 | 0.1407 | 0.1577 |
| Watermelon seed (A ₂₁) | 0.1083 | 0.0102 | 0.0122 | 0.5038 | 0.0670 | 0.1407 | 0.1577 |
| Sunflower (A ₂₂) | 0.1083 | 0.0102 | 0.0122 | 0.5038 | 0.0670 | 0.1407 | 0.1577 |
| Broom (A ₂₃) | 0.1488 | 0.0148 | 0.0122 | 0.5038 | 0.0670 | 0.1407 | 0.1126 |
| Pumpkin seed (A ₂₄) | 0.1704 | 0.0102 | 0.0122 | 0.3499 | 0.0670 | 0.2265 | 0.1637 |
| Jo (A ₂₅) | 0.1704 | 0.0102 | 0.0122 | 0.3499 | 0.0670 | 0.2265 | 0.1637 |
| Maize (A ₂₆) | 0.1704 | 0.0102 | 0.0122 | 0.3499 | 0.0670 | 0.2265 | 0.1637 |
| Shaltook (A ₂₇) | 0.1704 | 0.0102 | 0.0122 | 0.3499 | 0.0670 | 0.2265 | 0.1637 |
| Wheat (A ₂₈) | 0.1365 | 0.0102 | 0.0122 | 0.3499 | 0.0670 | 0.2627 | 0.1615 |
| Canola (A ₂₉) | 0.0630 | 0.0148 | 0.0122 | 0.5038 | 0.0690 | 0.1796 | 0.1577 |
| Sesame (A ₃₀) | 0.1083 | 0.0102 | 0.0122 | 0.5038 | 0.0670 | 0.1407 | 0.1577 |
| Golrang (A ₃₁) | 0.0921 | 0.0148 | 0.0511 | 0.5038 | 0.0856 | 0.0948 | 0.1577 |
| Shah seed (A ₃₂) | 0.1704 | 0.0102 | 0.0122 | 0.3499 | 0.0670 | 0.2265 | 0.1637 |
| Sugar beet (A ₃₃) | 0.1037 | 0.0148 | 0.0122 | 0.5038 | 0.0670 | 0.1407 | 0.1577 |
| Cotton (A ₃₄) | 0.1037 | 0.0148 | 0.0511 | 0.5038 | 0.0740 | 0.0948 | 0.1577 |
| Tobacco (A ₃₅) | 0.0649 | 0.0079 | 0.0122 | 0.4215 | 0.0693 | 0.2627 | 0.1615 |
| Mendab (A ₃₆) | 0.1083 | 0.0102 | 0.0122 | 0.5038 | 0.0740 | 0.1337 | 0.1577 |
| Pea (A ₃₇) | 0.0649 | 0.0102 | 0.0122 | 0.5038 | 0.0670 | 0.2196 | 0.1222 |
| Dried baghala (A ₃₈) | 0.1083 | 0.0102 | 0.0122 | 0.5038 | 0.0740 | 0.1337 | 0.1577 |
| Lentils (A ₃₉) | 0.1488 | 0.0102 | 0.0122 | 0.5038 | 0.0700 | 0.1722 | 0.0828 |
| Bean (A ₄₀) | 0.1083 | 0.0102 | 0.0122 | 0.5038 | 0.0670 | 0.1407 | 0.1577 |
| Mung bean (A ₄₁) | 0.1704 | 0.0148 | 0.0122 | 0.4311 | 0.0670 | 0.1407 | 0.1637 |
| Cucumber (A ₄₂) | 0.1083 | 0.0102 | 0.0122 | 0.5038 | 0.0670 | 0.1407 | 0.1577 |
| Melon (A ₄₃) | 0.1083 | 0.0079 | 0.0122 | 0.5038 | 0.0693 | 0.1407 | 0.1577 |
| Pumpkin family (A ₄₄) | 0.1083 | 0.0102 | 0.0122 | 0.5038 | 0.0670 | 0.1407 | 0.1577 |
| Watermelon family (A ₄₅) | 0.1083 | 0.0102 | 0.0511 | 0.5038 | 0.0740 | 0.0948 | 0.1577 |
| Eggplant (A ₄₆) | 0.1083 | 0.0102 | 0.0122 | 0.5038 | 0.0670 | 0.1407 | 0.1577 |

experts to the extent that is feasible. Hence, the proposed model demonstrates that after underscoring the criteria in which the alternatives have higher risks, we should select A₃₂ as a more suitable alternative than A₂₉ because it has fewer weaknesses and a more uniform performance score compared with A₂₉.

5.4. Analyzing the results of optimization cultivation model

In this case study, 46 crops are divided into two groups, Group A and Group B, based on their climatic features. Group A consists of 16 crops that can be cultivated during the warm period (the first six months of a year), while Group B consists of 30 crops that can be cultivated during the semi-cold or cold period (the second six months of a year). The values of parameters for the linear optimization problem for Groups A and B are presented in Appendix B (Table B for Group A and Table C for Group B). The optimal cultivation magnitudes for crops in Groups A and B are detailed in Tables D-F in Appendix B, respectively.

As demonstrated in Table 7, the optimal cultivation pattern model was applied to crops in Group A, resulting in the selection of Crops 8, 13, 11, and 14 as the optimal solution, with respective ranks of 43, 3, 7, and 6. Notably, Crops 11, 13, and 14 achieved the highest possible value of their respective demands, indicating the strategic dimension of the MAOM. It is noteworthy that Crop 8 has achieved approximately half of

its maximum demand due to its low rank (43) and its ability to satisfy operational constraints, as evidenced by the values of its respective parameters in the model.

As demonstrated in Table 8, the same reasoning applies to crops in Group B. Specifically, the demand constraint is the primary factor, provided that the other constraints are satisfied. From the 30 crops, those with sustainability ranks of 1, 10, 14, and 5 (i.e., crops 7, 15, 32, and 41, respectively) were chosen. If the selection of only four crops from Group B was to be made without taking operational-level criteria into account, then it would be reasonable to select the four crops with the highest rankings. However, our linear mathematical model suggests otherwise, as we are confronted with certain constraints in the real-world environment that are taken into consideration in our cultivation model (operational level). It is observed that crops with ranks 7, 15, and 32 have achieved their highest levels of demand, whereas crop number 41 has not yet reached its peak demand. An intriguing outcome is related to the fact that crops with ranks 4, 8, 9, and 11 have not been chosen. This is likely due to the fact that these crops have significantly lower demand in comparison to crops with ranks 1, 10, 14, and 5. In our objective function, the decision variable is maximized, thus the model seeks to identify crops that satisfy the constraints while also having a high potential value of cultivation. For instance, Crop 2 has a high demand, however, due to its low rank, the model will not select it as the

Table 6
Ranking result of risk-averse UTA and original UTA.

| Alternatives | Risk-averse UTA | | Original UTA | |
|-----------------|-----------------|------|---------------|------|
| | Overall score | Rank | Overall score | Rank |
| A ₁ | 0.1459 | 45 | 0.2139 | 45 |
| A ₂ | 0.2074 | 36 | 0.2953 | 35 |
| A ₃ | 0.1917 | 40 | 0.2731 | 42 |
| A ₄ | 0.2509 | 30 | 0.2846 | 37 |
| A ₅ | 0.1414 | 46 | 0.2113 | 46 |
| A ₆ | 0.3606 | 17 | 0.3797 | 25 |
| A ₇ | 0.6215 | 1 | 0.5906 | 1 |
| A ₈ | 0.1859 | 43 | 0.2544 | 44 |
| A ₉ | 0.3257 | 25 | 0.4215 | 17 |
| A ₁₀ | 0.3130 | 26 | 0.3274 | 29 |
| A ₁₁ | 0.5256 | 3 | 0.5433 | 2 |
| A ₁₂ | 0.2331 | 32 | 0.3527 | 27 |
| A ₁₃ | 0.4730 | 7 | 0.4652 | 7 |
| A ₁₄ | 0.4913 | 6 | 0.4991 | 4 |
| A ₁₅ | 0.4526 | 10 | 0.4507 | 9 |
| A ₁₆ | 0.4445 | 11 | 0.4285 | 15 |
| A ₁₇ | 0.3505 | 20 | 0.3868 | 24 |
| A ₁₈ | 0.4598 | 9 | 0.4380 | 13 |
| A ₁₉ | 0.3574 | 18 | 0.4329 | 14 |
| A ₂₀ | 0.2011 | 38 | 0.2938 | 36 |
| A ₂₁ | 0.2541 | 29 | 0.3318 | 28 |
| A ₂₂ | 0.2008 | 39 | 0.2752 | 40 |
| A ₂₃ | 0.2332 | 31 | 0.3041 | 34 |
| A ₂₄ | 0.4242 | 12 | 0.4192 | 18 |
| A ₂₅ | 0.4644 | 8 | 0.4490 | 10 |
| A ₂₆ | 0.5117 | 4 | 0.4801 | 6 |
| A ₂₇ | 0.4240 | 13 | 0.4189 | 19 |
| A ₂₈ | 0.3564 | 19 | 0.3601 | 26 |
| A ₂₉ | 0.3929 | 15 | 0.4608 | 8 |
| A ₃₀ | 0.2273 | 33 | 0.3174 | 32 |
| A ₃₁ | 0.2908 | 27 | 0.3872 | 23 |
| A ₃₂ | 0.4069 | 14 | 0.4087 | 20 |
| A ₃₃ | 0.2615 | 28 | 0.3194 | 31 |
| A ₃₄ | 0.3621 | 16 | 0.4408 | 11 |
| A ₃₅ | 0.5699 | 2 | 0.5421 | 3 |
| A ₃₆ | 0.3312 | 24 | 0.4271 | 16 |
| A ₃₇ | 0.2058 | 37 | 0.2743 | 41 |
| A ₃₈ | 0.3452 | 21 | 0.4385 | 12 |
| A ₃₉ | 0.3370 | 22 | 0.4004 | 22 |
| A ₄₀ | 0.3329 | 23 | 0.4066 | 21 |
| A ₄₁ | 0.4984 | 5 | 0.4814 | 5 |
| A ₄₂ | 0.1910 | 41 | 0.2783 | 38 |
| A ₄₃ | 0.2104 | 35 | 0.3131 | 33 |
| A ₄₄ | 0.1905 | 42 | 0.2778 | 39 |
| A ₄₅ | 0.2211 | 34 | 0.3235 | 30 |
| A ₄₆ | 0.1787 | 44 | 0.2586 | 43 |

optimal set of solutions.

Considering the practical constraints in the province investigated in our case study, we observe that even top crops in terms of risk-averse UTA output may not be selected, proving how realistic our optimal cultivation model is. For example, as shown in Table 6, according to risk-averse overall score, A₇, A₃₅, A₁₁, A₂₆, and A₄₁ are among the top 5 with respect to the risk-averse overall score; however, according to Table 7, A₈, A₁₁, A₁₃, and A₁₄ for group A and A₇, A₁₅, A₃₂, and A₄₁ for group B

are selected when we consider operational constraints. As it can be seen, A₇, A₁₁, and A₄₁ are common between what the risk-averse overall score and our optimization problem choose. This result reveals that our MAOM appropriately captures the strategic and operational dimensions of the proposed framework. Moreover, currently in the province, A₈, A₁₃, A₁, and A₁₇ in group A and A₇, A₁₅, A₄₃, and A₄₄ in group B are cultivated. According to Tables 7 and 8, we observe some differences between what actually happens and our suggested optimization model. To be more specific, for group A, our optimization problem chooses A₁₁ and A₁₄ instead of A₁ and A₁₇ and for group B, A₃₂ and A₄₁ instead of A₆ and A₄₃. There is an important note behind this difference signifying why our optimal cultivation pattern is better than what happens in the real case. To prove this fact, it suffices to refer to the objective function value for the two cases:

For group A, in the real situation, A₁ and A₁₇ have respective values of 9000 and 9624, and given their risk-averse overall scores of 0.1459 and 0.3505, the objective function is 4686.3120 (according to Eq. (5)); however, according to our model’s suggestion, A₁₁ and A₁₄ have respective values of 47,619 and 55,248 and considering their respective risk-averse overall scores of 0.5256 and 0.4913, the objective function, according to Eq. (5), is equal to 52171.8888. Hence, since our model presents a higher objective function, it is better (remember that the objective function is the sustainability score of the cultivation pattern). Our inference is that the reason for satisfying upper demand for crops with a not-that-high rank in risk-averse UTA is having decent performance in operational constraints (the constraints of our optimization model); i.e., the entire focus on the cultivation of these crops over the long-term is not justifiable.

Similarly, for group B, the similar reasoning is valid. To sum up, since our optimization model’s output both is similar to the output of risk-averse overall scores and considers operational constraints, it results in a more sustainable cultivation pattern. We also reported time execution for the optimization models in Table G of Appendix B.

5.5. Sensitivity analysis of the optimal cultivation model

After consulting with experts, it was determined that the only parameter in the optimal cultivation model that can be considered uncertain is demand. The experts provided four plausible scenarios based on their past experience. To this end, in order to assess the sensitivity of our primary results presented in Sections 7 and 8 for Groups A and B of products, four scenarios were considered in which the demand for the products was increased by 10%, 20%, 40%, and 60%, respectively. It was found that the selection of products for cultivation remained the same after implementing new scenarios, suggesting that the proposed optimal cultivation model is approximately robust with respect to demand changes of up to 60%. This result was presented for both Group A and Group B of products in Table 9. It was observed from the preceding sub-sections that A₇, A₈, A₁₁, A₁₃, A₁₄, A₁₅, A₃₂, and A₄₁ were selected as optimal crops (for group A and B) to be cultivated. An example of the effects of a 10% increase in demand, as seen in Table 9, is that A₃₂ and A₄₁ are no longer selected as the optimal products in the new scenario

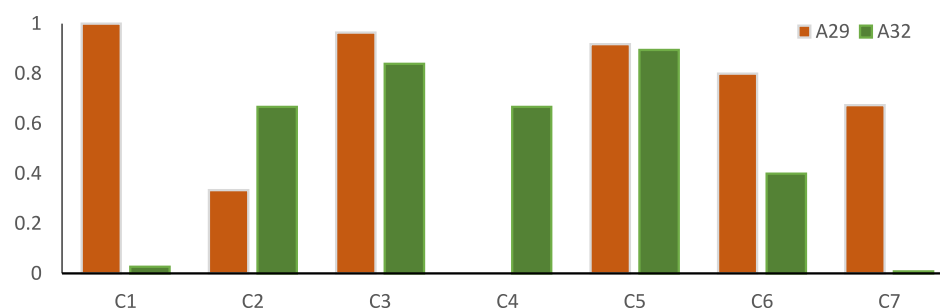


Fig. 3. Normalized value of A₂₉ and A₃₂.

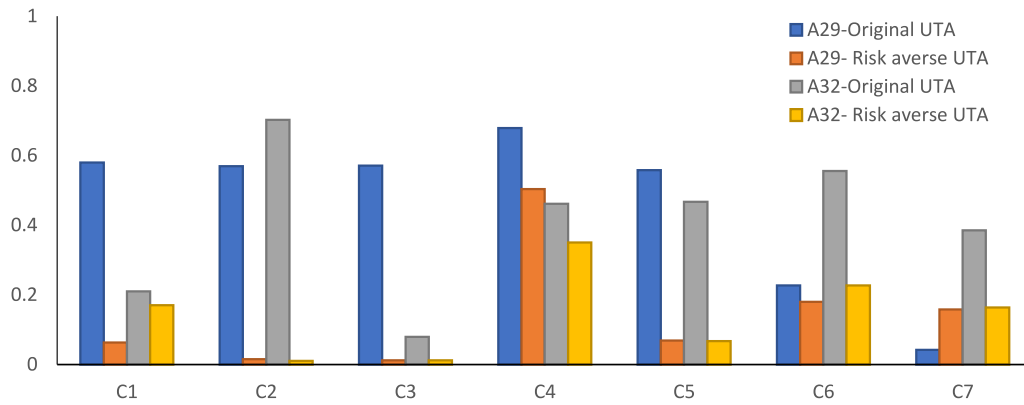


Fig. 4. The respective performance of A₂₉ and A₃₂ on criteria in which they practice within the evaluation process based on the original and risk-averse UTA.

Table 7

Optimal set of solution for crops in group A.

| Crop | Rank | Optimal Cultivation | D _i |
|-----------------|------|---------------------|----------------|
| A ₁ | 45 | 0 | 9000 |
| A ₈ | 43 | 20483.8105 | 41,666 |
| A ₉ | 25 | 0 | 1170 |
| A ₁₁ | 3 | 47,619 | 47,619 |
| A ₁₃ | 7 | 17,857 | 17,857 |
| A ₁₄ | 6 | 55,248 | 55,248 |
| A ₁₇ | 20 | 0 | 9624 |
| A ₁₉ | 18 | 0 | 600 |
| A ₂₄ | 12 | 0 | 2702 |
| A ₂₇ | 13 | 0 | 4000 |
| A ₂₈ | 19 | 0 | 1751 |
| A ₃₅ | 2 | 0 | 2481 |
| A ₃₆ | 24 | 0 | 1175 |
| A ₃₇ | 37 | 0 | 2500 |
| A ₃₈ | 21 | 0 | 1004 |
| A ₄₀ | 23 | 0 | 1169 |

Table 8

Optimal set of solution for crops in group B.

| Crop | Rank | Optimal Cultivation | D _i |
|-----------------|------|---------------------|----------------|
| A ₂ | 36 | 0 | 45,454 |
| A ₃ | 40 | 0 | 38,461 |
| A ₄ | 30 | 0 | 20,000 |
| A ₅ | 46 | 0 | 23,255 |
| A ₆ | 17 | 0 | 26,315 |
| A ₇ | 1 | 32,786 | 32,786 |
| A ₁₀ | 26 | 0 | 7032 |
| A ₁₂ | 32 | 0 | 6024 |
| A ₁₅ | 10 | 50,505 | 50,505 |
| A ₁₆ | 11 | 0 | 6896 |
| A ₁₈ | 9 | 0 | 3508 |
| A ₂₀ | 38 | 0 | 700 |
| A ₂₁ | 29 | 0 | 1533 |
| A ₂₂ | 39 | 0 | 3003 |
| A ₂₃ | 31 | 0 | 800 |
| A ₂₅ | 8 | 0 | 6301 |
| A ₂₆ | 4 | 0 | 3974 |
| A ₂₉ | 15 | 0 | 925 |
| A ₃₀ | 33 | 0 | 1388 |
| A ₃₁ | 27 | 0 | 3484 |
| A ₃₂ | 14 | 51,020 | 51,020 |
| A ₃₃ | 28 | 0 | 2403 |
| A ₃₄ | 16 | 0 | 2617 |
| A ₃₅ | 22 | 0 | 1404 |
| A ₄₁ | 5 | 3792.4602 | 20,325 |
| A ₄₂ | 41 | 0 | 19,880 |
| A ₄₃ | 35 | 0 | 35,714 |
| A ₄₄ | 42 | 0 | 28,328 |
| A ₄₅ | 34 | 0 | 23,809 |
| A ₄₆ | 44 | 0 | 31,250 |

Table 9

Outcomes of the optimal cultivation model following an increase in demand.

| Scenario | Product Number | Rank | Optimal Cultivation | Demand |
|---------------------|----------------|------|---------------------|---------|
| Demand + 10% Demand | 7 | 1 | 36064.6 | 36064.6 |
| | 8 | 43 | 45832.6 | 45832.6 |
| | 11 | 3 | 52380.9 | 52380.9 |
| | 13 | 7 | 19642.7 | 19642.7 |
| Demand + 20% Demand | 14 | 6 | 60772.8 | 60772.8 |
| | 15 | 10 | 29738.7 | 55555.5 |
| | 17 | 20 | 6800.3 | 10586.4 |
| Demand + 40% Demand | 7 | 1 | 39343.2 | 39343.2 |
| | 8 | 43 | 49999.2 | 49999.2 |
| | 11 | 3 | 57142.8 | 57142.8 |
| | 13 | 7 | 21428.4 | 21428.4 |
| Demand + 60% Demand | 14 | 6 | 66297.6 | 66297.6 |
| | 15 | 10 | 17954.1 | 60,606 |
| | 17 | 20 | 4105.6 | 11548.8 |
| | 7 | 1 | 41526.5 | 45900.4 |
| | 8 | 43 | 54858.3 | 58332.4 |
| Demand + 60% Demand | 11 | 3 | 66666.6 | 66666.6 |
| | 13 | 7 | 24999.8 | 24999.8 |
| | 14 | 6 | 77347.2 | 77347.2 |
| | 7 | 1 | 29723.5 | 52457.6 |
| Demand + 60% Demand | 8 | 43 | 48608.4 | 66665.6 |
| | 11 | 3 | 76190.4 | 76190.4 |
| | 13 | 7 | 28571.2 | 28571.2 |
| | 14 | 6 | 88396.8 | 88396.8 |

compared to the before-change state. Furthermore, in all four scenarios, A₇, A₈, A₁₁, A₁₃ and A₁₄ remain optimal, indicating that these products are the most reliable ones in terms of dealing with demand uncertainty.

6. Managerial implications

The study suggests a framework that combines qualitative and quantitative criteria with an optimization approach to address both short-term and long-term concerns in MCDA contexts. The research introduces a risk-averse UTA method that considers both experts' opinions and the information in the decision matrix to avoid anchoring bias in the weighting process. The proposed methodology eliminates the complexity associated with the application of probabilistic or fuzzy methods in decision-making. Moreover, the MAOM can reduce the dimensions of complex problems, making them feasible to solve. The framework can be used in various areas, including multi-level supply chain management, healthcare system optimization, and financial markets, where the complexity of the situation can be overwhelming. The proposed methodology can suggest alternatives with the fewest weaknesses, leading to satisfaction in the long term, even in crises such as the emergent need for hospital location. The current weighting

methods that rely solely on experts' opinions can lead to a preference for certain criteria, ultimately resulting in suboptimal alternatives. The proposed method can consider both experts' opinions and the information in the decision matrix, ensuring a comprehensive evaluation and weighting of criteria. The proposed method yields the following insights:

- Organizations can effectively consider both short-term and long-term concerns in their decision-making process by utilizing strategic and operational criteria.
- The proposed MAOM reduces the risk of the decision-making process.
- When there is a lack of information regarding potential alternatives, when the alternatives are only known to experts, or when a crisis situation necessitates the selection of alternatives, current methods may be effective in the short-term, but they may not take into account the long-term implications of the alternatives as the MAOM can.

7. Conclusions and future studies

This study proposed a Multi-Attribute Optimization Model (MAOM) to determine the optimal amount of cultivation of crops considering both strategic and operational criteria in order to promote sustainable agricultural development. The framework of strategic criteria was divided into economy, society, and environment dimensions and used to calculate the sustainability score of candidate crops in the first step. In order to reduce the risk of low-scoring criteria, a risk-averse UTA was developed in this step. In the second step, a linear mathematical model was developed to calculate the optimal amount of candidate crops, taking into account the results of risk-averse UTA as the parameter of the objective function and operational criteria as constraints.

We employed the MAOM in Khorasan Razavi, Iran. An analysis of the local weight of strategic criteria revealed that the three dimensions had varying levels of importance, with the economic dimension being the most significant. An analysis of the local weight of sub-criteria in the three dimensions revealed that *convenience of crop cultivation, water consumption per hectare, and usage of fertilizer and pesticide per hectare* are the most significant factors from *economic, social, and environmental* perspectives.

In this study, the risk-averse UTA was used to figure out the sustainability scores of 49 candidate crops, and the crops were then ranked according to their scores. The highest and lowest scores were achieved by Potato and Leafy vegetables, respectively. Furthermore, a comparison between the original UTA and the risk-averse UTA revealed that the latter was able to effectively adjust the trade-off between decision-making criteria by determining the optimal weight for each. Finally, the optimization problem yielded the result that Dried garlic, Turnip and forage, Millet, and Khasil should be cultivated during the spring and summer months, while Potato, Fodder beet, Shah seed, and Mung bean are recommended for the autumn and winter months. Moreover, sensitivity analysis on the proposed model showed that our results are approximately robust with respect to demand uncertainty. This outcome can be valuable for policymakers by helping them to formulate policies, allocate resources, and promote economic stability in the agricultural sector. For example, policymakers can use the proposed framework to

design policies that incentivize farmers to cultivate that particular crop. This can help ensure a stable supply of the crop even if demand fluctuates.

In this study, we used multi-criteria decision-making (MCDM) methods to come up with a hierarchical structure of criteria to figure out how sustainable crops are. This suggested structure provides valuable insights for both scholars and policymakers. Scholars can use the criteria to enhance and create agricultural machinery and seeds for sustainable production, while policymakers can use the framework of criteria to rank farmers' concerns and devise sustainable strategies to address them.

This work is limited in that, although we have attempted to cover more criteria by taking into account a sustainability index, it may not be the most comprehensive in terms of sustainability. Future research should consider other operational issues such as workforce allocation, irrigation scheduling, transportation of raw materials, and produced crops to better proxy real-life situations in optimal cultivation patterns. Moreover, other mathematical programming, such as stochastic programming can model the uncertainty of parameters at operational level more appropriately. Such an extension for the proposed model will provide decision-makers with more accurate results. In addition, if our proposed model applies to a wider scope (country), the size of the problem gets bigger and needs meta-heuristic algorithms for providing efficient solutions. Therefore, devising a meta-heuristic algorithm for a large-scale version of our proposed framework is beneficial. Finally, even though this study extends UTA method by considering risk-averse factor in decision-making process, since uncertainty is intertwined with decision-making context (Chun-Yueh, 2022), a combination of reinforcement learning (Zamfirache, Precup, Roman, & Petriu, 2022) and UTA is appreciated to include both risk factor and uncertainty for multi-criteria decision-making problems.

CRedit authorship contribution statement

Mohammad Reza Mehrpour: Conceptualization, Investigation, Resources, Validation, Data curation, Formal analysis, Software, Visualization, Writing - original draft, Writing - review & editing. **Siamak Kheybari:** Conceptualization, Investigation, Methodology, Resources, Validation, Data curation, Formal analysis, Project administration, Software, Supervision, Visualization, Writing - original draft, Writing - review & editing. **Jagjit Singh Srail:** Validation, Conceptualization, Investigation, Writing - original draft, Writing - review & editing. **Abbas Rohani:** Resources, Validation, Conceptualization, Data curation, Funding acquisition, Investigation, Writing - original draft, Writing - review & editing.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

Data will be made available on request.

Appendix A

Applying the UTA model entails the following assumptions:

- A set of criteria as $\{g_1, g_2, \dots, g_n\}$ is defined in which n denotes the number of decision criteria.
- A_R includes the options that are ranked by the decision maker.
- Possible values for different options within criterion i in real interval is defined such that g_i^* and g_i^* denote the worst and best level of criterion i in a non-decreasing real interval.

- The value of option a in criterion i is equal to $g_i(a)$ and $g(a)$ that shows the performance of option a in n decision criteria.
- As the performance of an option increases, its preference increases. In other words, we have:

$$g_i(a) > g_i(b) \Leftrightarrow a P b \quad \forall i$$

$$g_i(a) = g_i(b) \Leftrightarrow a I b \quad \forall i \tag{A1}$$

Where P is called the strict preference relation and I the indifference relation.

- Marginal utility function of alternative a for criterion i is denoted by $u_i(g_i(a))$, and global utility function of alternative a is denoted by $U(a)$. Both marginal utility and global utility functions are positive, non-decreasing, and one-to-one functions, and they belong to the set of real numbers. Global utility function lies within the interval $[0,1]$ while marginal utility function is a fraction of this interval, and we have:

$$u_i : [g_i^*, g_i^*] \rightarrow [0,1] \quad \forall i$$

$$U(g(a)) > U(g(b)) \Leftrightarrow a > b$$

$$U(g(a)) = U(g(b)) \Leftrightarrow a \approx b \tag{A2}$$

- Assuming that Global utility function is an additive function, we have:

$$U(g(a)) = \sum_i^n u_i(g_i(a))$$

$$\sum_i^n u_i(g_i^*) = 1$$

$$u_i(g_i^*) = 0, \quad \forall i = 1, 2, \dots, n \tag{A3}$$

- As shown in Fig. A, any marginal utility function is regarded as a continuous piecewise linear function, meaning that it consists of a series of linear functions that are interconnected.
- We assume that $[g_i^*, g_i^*]$ can be divided into $(\alpha_i - 1)$ equal parts such that the ending point of each interval for criterion i and sub-interval j is equal to:

$$g_i^j = g_i + \frac{j-1}{\alpha_i - 1} (g_i^* - g_i^*) \quad \forall i = 1, 2, \dots, \alpha_i \tag{A4}$$

Where using linear interpolation, $u_i(g_i(a))$ is equal to:

$$u_i(g_i(a)) = u_i(g_i^j) + \frac{g_i(a) - g_i^j}{g_i^{j+1} - g_i^j} (u_i(g_i^{j+1}) - u_i(g_i^j)) \tag{A5}$$

This method uses a linear programming to achieve utility functions such that the rankings obtained from these functions are as consistent as possible with the initial rankings performed on the A_R reference set. Since the answer obtained from the model may be exactly in accordance with the initial preferences of the decision maker, some errors are considered in the model such that the utility function defined in Equation (3) changes into Equation (6).

$$U'(g(a)) = \sum_i^n u_i(g_i(a)) + \sigma(a) \quad \forall a \in A_R \tag{A6}$$

Where $\sigma(a)$ is potential error of $U(g(a))$.

Considering the ranking done in A_R and assuming that a_1 is at the highest rank and a_n is at the lowest the rank, in each pair of alternatives (a_k, a_{k+1}) , it is possible (i) a_k takes precedence over a_{k+1} ($(a_k > a_{k+1})$) or (ii) the two alternatives are indifferent to each other ($(a_k \approx a_{k+1})$). In other words, we have:

$$\begin{aligned} \Delta(a_k, a_{k+1}) &= U[g(a_k)] - U[g(a_{k+1})] \geq \delta \text{ for } a_k > a_{k+1} \quad \forall k \\ \Delta(a_k, a_{k+1}) &= U[g(a_k)] - U[g(a_{k+1})] = 0 \text{ for } a_k \approx a_{k+1} \quad \forall k \end{aligned} \tag{A7}$$

Where δ is a very small value appropriately showing significant difference between two consecutive alternatives. Given the aforementioned explanations, marginal utility function is equal to:

$$\text{Minimize } F = \sum_{a \in A_R} \sigma(a)$$

Subject to:

$$\Delta(a_k, a_{k+1}) = U[g(a_k)] - U[g(a_{k+1})] \geq \delta \text{ for } a_k > a_{k+1} \quad \forall k$$

$$\Delta(a_k, a_{k+1}) = U[g(a_k)] - U[g(a_{k+1})] = 0 \text{ for } a_k \approx a_{k+1} \quad \forall k$$

Table A1
Normalized score of candidate crops across decision-making criteria.

| Crops | C ₁ | C ₂ | C ₃ | C ₄ | C ₅ | C ₆ | C ₇ |
|-----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|
| A ₁ | 0.059 | 0.334 | 0.84 | 0 | 0.948 | 0.4 | 0.039 |
| A ₂ | 0.096 | 0.334 | 0.875 | 0 | 0.918 | 0.8 | 0.056 |
| A ₃ | 0.071 | 0 | 0.858 | 0 | 0.823 | 0.8 | 0.039 |
| A ₄ | 0.046 | 0.667 | 0.929 | 0.334 | 0.888 | 0.2 | 0.022 |
| A ₅ | 0.096 | 0.334 | 0.858 | 0 | 0.777 | 0.4 | 0.056 |
| A ₆ | 0.31 | 0.667 | 0.822 | 0.334 | 0.896 | 0.6 | 0.009 |
| A ₇ | 0.059 | 0.667 | 0.893 | 1 | 0.915 | 0.8 | 0.031 |
| A ₈ | 0.41 | 0.667 | 0.911 | 0 | 0.955 | 0.2 | 0.271 |
| A ₉ | 0.561 | 0.667 | 0.947 | 0 | 0.758 | 1 | 0.374 |
| A ₁₀ | 0.065 | 0.667 | 0.786 | 0.667 | 0.731 | 0 | 0.035 |
| A ₁₁ | 0.052 | 1 | 0.875 | 0.667 | 0.976 | 1 | 0.026 |
| A ₁₂ | 0.071 | 1 | 0.911 | 0 | 0.916 | 1 | 0.039 |
| A ₁₃ | 0.076 | 1 | 0.786 | 0.667 | 0.963 | 0.6 | 0.042 |
| A ₁₄ | 0 | 1 | 0.875 | 0.667 | 0.967 | 0.8 | 0.019 |
| A ₁₅ | 0.015 | 1 | 0.768 | 0.667 | 0.919 | 0.6 | 0 |
| A ₁₆ | 0.015 | 0.334 | 0.768 | 0.667 | 0.916 | 0.6 | 0 |
| A ₁₇ | 0.071 | 1 | 0 | 0.667 | 0 | 0.8 | 0.039 |
| A ₁₈ | 0.069 | 0.334 | 0.768 | 0.667 | 0.916 | 0.6 | 0.037 |
| A ₁₉ | 0.749 | 0.667 | 0.983 | 0 | 0.986 | 0.8 | 0.503 |
| A ₂₀ | 0.052 | 0.334 | 0.929 | 0 | 0.956 | 0.8 | 0.026 |
| A ₂₁ | 0.423 | 0.667 | 0.947 | 0 | 0.919 | 0.6 | 0.279 |
| A ₂₂ | 0.31 | 0.667 | 0.965 | 0 | 0.904 | 0.4 | 0.202 |
| A ₂₃ | 0.052 | 0.334 | 0.929 | 0 | 0.873 | 0.6 | 0.588 |
| A ₂₄ | 0.075 | 0.667 | 0.822 | 0.667 | 0.956 | 0.4 | 0.042 |
| A ₂₅ | 0.069 | 0.667 | 0.768 | 0.667 | 0.916 | 0.6 | 0.037 |
| A ₂₆ | 0.247 | 0.667 | 0.804 | 0.667 | 0.864 | 0.6 | 0.159 |
| A ₂₇ | 0.077 | 0.667 | 0.822 | 0.667 | 0.943 | 0.4 | 0.043 |
| A ₂₈ | 0.184 | 0.667 | 0.786 | 0.667 | 0.939 | 0 | 0.116 |
| A ₂₉ | 1 | 0.334 | 0.965 | 0 | 0.918 | 0.8 | 0.674 |
| A ₃₀ | 0.184 | 0.334 | 0.965 | 0 | 0.916 | 0.8 | 0.116 |
| A ₃₁ | 0.561 | 0.334 | 0.911 | 0 | 0.397 | 1 | 0.374 |
| A ₃₂ | 0.027 | 0.667 | 0.84 | 0.667 | 0.895 | 0.4 | 0.009 |
| A ₃₃ | 0.486 | 0.334 | 0.786 | 0 | 0.917 | 0.6 | 0.322 |
| A ₃₄ | 0.687 | 0.334 | 0.875 | 0 | 1 | 1 | 0.46 |
| A ₃₅ | 0.875 | 1 | 0.947 | 0.667 | 0.941 | 0.2 | 0.588 |
| A ₃₆ | 0.498 | 0.667 | 1 | 0 | 0.978 | 1 | 0.331 |
| A ₃₇ | 0.561 | 0.667 | 0.84 | 0 | 0.937 | 0.2 | 0.374 |
| A ₃₈ | 0.561 | 0.667 | 1 | 0 | 0.985 | 1 | 0.374 |
| A ₃₉ | 0.473 | 0.667 | 0.911 | 0 | 0.896 | 0.6 | 1 |
| A ₄₀ | 0.661 | 0.667 | 0.893 | 0 | 0.915 | 0.8 | 0.443 |
| A ₄₁ | 0.096 | 0.334 | 0.822 | 0.667 | 0.866 | 0.8 | 0.056 |
| A ₄₂ | 0.04 | 0.334 | 0.822 | 0 | 0.866 | 0.8 | 0.018 |
| A ₄₃ | 0.096 | 1 | 0.858 | 0 | 0.87 | 0.8 | 0.056 |
| A ₄₄ | 0.037 | 0.334 | 0.822 | 0 | 0.866 | 0.8 | 0.016 |
| A ₄₅ | 0.077 | 0.334 | 0.822 | 0 | 0.889 | 1 | 0.043 |
| A ₄₆ | 0.109 | 0.334 | 0.893 | 0 | 0.866 | 0.6 | 0.065 |

$$\sum_i^n u_i(g_i^*) = 1$$

$$u_i(g_i^{j+1}) - u_i(g_i^j) \geq 0 \quad \forall i, j$$

$$\sigma(a) \geq 0$$
(A8)

If $F^* = 0$, then it means that we have found a solution set for the final utility such that the ranking resulted from the model perfectly matches the initial ranking presented by the reference set; otherwise, it means that there is no set of values to accurately create the same initial ranking of the A_R . Therefore, the ranking obtained from the model is created with some error in relation to the decision-maker's point of view.

Model 8 considers only positive errors, whereas since this error is not defined as an absolute value, it may have a negative value. For this purpose, an improved version of UTA was proposed by Siskos et al., (Siskos, Grigoroudis, & Matsatsinis, 2016), called UTA STAR (Model 9).

$$\text{Minimize } Z = \sum_{i=1}^m \sigma^+(a_k) + \sigma^-(a_k)$$

Subject to:

$$\Delta(a_k, a_{k+1}) \geq \delta \quad \forall a_k > a_{k+1} \quad \forall k$$

$$\Delta(a_k, a_{k+1}) = 0 \quad \forall a_k \approx a_{k+1} \quad \forall k$$

$$\sum_{i=1}^n \sum_{j=1}^{a_i-1} w_{ij} = 1 \quad \forall i, j$$

Table B1
Parameters of linear optimization model for group A.

| Crop | D_i | a_i | p_i | w_i |
|-----------------|--------|---------|--------|---------|
| A ₁ | 9000 | 11,000 | 0.1459 | 0.864 |
| A ₈ | 41,666 | 2400 | 0.1859 | 0.164 |
| A ₉ | 1170 | 85,400 | 0.3257 | 27.77 |
| A ₁₁ | 47,619 | 0.21 | 0.5256 | 0.086 |
| A ₁₃ | 17,857 | 5600 | 0.4730 | 0.32 |
| A ₁₄ | 55,248 | 0.181 | 0.4913 | 0.095 |
| A ₁₇ | 9624 | 10,398 | 0.3505 | 13.611 |
| A ₁₉ | 600 | 166,600 | 0.3574 | 4.83 |
| A ₂₄ | 2702 | 37,000 | 0.4242 | 2.51 |
| A ₂₇ | 4000 | 25,000 | 0.4240 | 2.125 |
| A ₂₈ | 1751 | 57,100 | 0.3564 | 5.139 |
| A ₃₅ | 2481 | 40,300 | 0.5699 | 3.52277 |
| A ₃₆ | 1175 | 85,100 | 0.3312 | 3.319 |
| A ₃₇ | 2500 | 40,000 | 0.2058 | 3.68 |
| A ₃₈ | 1004 | 99,600 | 0.3452 | 2.988 |
| A ₄₀ | 1169 | 85,500 | 0.3329 | 10.39 |

Table C1
Parameters of linear optimization model for group B.

| Crop | D_i | a_i | p_i | w_i |
|-----------------|--------|-------|--------|--------|
| A ₂ | 45,454 | 0.22 | 0.2074 | 0.256 |
| A ₃ | 38,461 | 0.26 | 0.1917 | 0.26 |
| A ₄ | 20,000 | 0.5 | 0.2509 | 0.78 |
| A ₅ | 23,255 | 0.43 | 0.1414 | 1.29 |
| A ₆ | 26,315 | 0.38 | 0.3606 | 0.554 |
| A ₇ | 32,786 | 0.305 | 0.6215 | 0.786 |
| A ₁₀ | 7032 | 1.422 | 0.3130 | 5.119 |
| A ₁₂ | 6024 | 1.66 | 0.2331 | 1.99 |
| A ₁₅ | 50,505 | 0.198 | 0.4526 | 0.229 |
| A ₁₆ | 6896 | 1.45 | 0.4445 | 1.74 |
| A ₁₈ | 3508 | 2.85 | 0.4598 | 3.42 |
| A ₂₀ | 700 | 14.28 | 0.2011 | 9.71 |
| A ₂₁ | 1533 | 6.523 | 0.2541 | 7.56 |
| A ₂₂ | 3003 | 3.33 | 0.2008 | 4.49 |
| A ₂₃ | 800 | 12.5 | 0.2332 | 21.875 |
| A ₂₅ | 6301 | 1.587 | 0.4644 | 1.9 |
| A ₂₆ | 3974 | 2.516 | 0.5117 | 4.7 |
| A ₂₉ | 925 | 10.81 | 0.3929 | 12.648 |
| A ₃₀ | 1388 | 7.204 | 0.2273 | 8.64 |
| A ₃₁ | 3484 | 2.87 | 0.2908 | 22.81 |
| A ₃₂ | 51,020 | 0.196 | 0.4069 | 0.287 |
| A ₃₃ | 2403 | 4.16 | 0.2615 | 4.91 |
| A ₃₄ | 2617 | 3.82 | 0.3621 | 0.37 |
| A ₃₅ | 1404 | 7.12 | 0.3370 | 10.38 |
| A ₄₁ | 20,325 | 0.492 | 0.4984 | 0.91 |
| A ₄₂ | 19,880 | 0.503 | 0.1910 | 0.93 |
| A ₄₃ | 35,714 | 0.28 | 0.2104 | 0.5 |
| A ₄₄ | 28,328 | 0.353 | 0.1905 | 0.65 |
| A ₄₅ | 23,809 | 0.42 | 0.2211 | 0.65 |
| A ₄₆ | 31,250 | 0.32 | 0.1787 | 0.592 |

$$\begin{aligned}
 w_{ij} &\geq 0 \quad \forall i, j \\
 \sigma^+(a_k) &\geq 0 \quad \forall k \\
 \sigma^-(a_k) &\geq 0 \quad \forall k
 \end{aligned}
 \tag{A9}$$

where

$$\Delta(a_k, a_{k+1}) = U[g(a_k)] - \sigma^+(a_k) - \sigma^-(a_k) - U[g(a_{k+1})] + \sigma^+(a_k) - \sigma^-(a_k)
 \tag{A10}$$

$$w_{ij} = u_i(g_i^{j+1}) - u_i(g_i^j) \geq 0 \quad \forall i = 1, 2, \dots, n, j = 1, 2, \dots, \alpha_i - 1
 \tag{A11}$$

Note that m in the objective function of model number 9 is equal to the number of alternatives of set A_R .

To calculate the optimal weigh of criteria contributed to decision making problems, we should solve optimization model 12 (Siskos et al., 2016).

$$\text{Minimize } (u_i(g_i^*)) = \sum_{j=1}^{\alpha_i-1} w_{ij} \quad \forall i$$

Subject to:

Table D1
Parameters related to common parameters of crops.

| City (j) | AT _j | PT _j | WT _j |
|----------|-----------------|-----------------|-----------------|
| 1 | 67,721 | 4284 | 47129.2169 |
| 2 | 26,805 | 1695 | 18654.4596 |
| 3 | 57,862 | 3660 | 40268.0224 |
| 4 | 23,088 | 1460 | 16067.6800 |
| 5 | 16,275 | 1029 | 11326.2947 |
| 6 | 17,541 | 1109 | 12207.3447 |
| 7 | 1580 | 99 | 1099.5727 |
| 8 | 5581 | 353 | 3883.9970 |
| 9 | 16,249 | 1028 | 11308.2005 |
| 10 | 44,824 | 2835 | 31194.4599 |
| 11 | 16,267 | 1029 | 11320.7273 |
| 12 | 30,717 | 1943 | 21376.9459 |
| 13 | 15,622 | 988 | 10871.8511 |
| 14 | 15,631 | 988 | 10878.1145 |
| 15 | 20,831 | 1317 | 14496.9613 |
| 16 | 17,840 | 1128 | 12415.4284 |
| 17 | 17,128 | 1083 | 11919.9248 |
| 18 | 30,588 | 1935 | 21287.1707 |
| 19 | 96,603 | 6111 | 67229.1274 |
| 20 | 35,231 | 2228 | 24518.3834 |
| 21 | 48,330 | 3057 | 33634.3978 |
| 22 | 38,459 | 2433 | 26764.8521 |
| 23 | 25,026 | 1583 | 17416.3964 |
| 24 | 8729 | 552 | 6074.7912 |
| 25 | 6693 | 423 | 4657.8735 |
| 26 | 44,609 | 2822 | 31044.8345 |
| 27 | 20,026 | 1266 | 13936.7360 |
| 28 | 6275 | 396 | 4366.9738 |
| 29 | 18,176 | 1149 | 12649.2616 |

Table E1
Optimal cultivation magnitude in detail for crops in group A.

| City (j) | A ₇ | A ₁₁ | A ₁₄ | A ₁₅ |
|----------|----------------|-----------------|-----------------|-----------------|
| 1 | 10640.5473 | 0.0000 | 0.0000 | 0.0000 |
| 2 | 4210.0205 | 0.0000 | 0.0000 | 0.0000 |
| 3 | 0.0000 | 0.0000 | 0.0000 | 11669.7159 |
| 4 | 3626.3303 | 0.0000 | 0.0000 | 0.0000 |
| 5 | 0.0000 | 4640.1469 | 0.0000 | 0.0000 |
| 6 | 2754.5208 | 0.0000 | 0.0000 | 0.0000 |
| 7 | 0.0000 | 0.0000 | 414.3600 | 0.0000 |
| 8 | 876.7771 | 0.0000 | 0.0000 | 0.0000 |
| 9 | 2553.3339 | 0.0000 | 0.0000 | 0.0000 |
| 10 | 0.0000 | 0.0000 | 11865.7636 | 0.0000 |
| 11 | 608.5280 | 3535.3500 | 0.0000 | 0.0000 |
| 12 | 4825.9998 | 0.0000 | 0.0000 | 0.0000 |
| 13 | 0.0000 | 0.0000 | 4135.2291 | 0.0000 |
| 14 | 0.0000 | 0.0000 | 0.0000 | 3150.1856 |
| 15 | 0.0000 | 0.0000 | 5512.2436 | 0.0000 |
| 16 | 0.0000 | 0.0000 | 4721.1927 | 0.0000 |
| 17 | 2689.9423 | 0.0000 | 0.0000 | 0.0000 |
| 18 | 0.0000 | 0.0000 | 8098.8545 | 0.0000 |
| 19 | 0.0000 | 0.0000 | 15691.2691 | 7531.1117 |
| 20 | 0.0000 | 10046.8875 | 0.0000 | 0.0000 |
| 21 | 0.0000 | 0.0000 | 0.0000 | 9747.0824 |
| 22 | 0.0000 | 0.0000 | 0.0000 | 7757.4915 |
| 23 | 0.0000 | 7138.3406 | 0.0000 | 0.0000 |
| 24 | 0.0000 | 130.7719 | 0.0000 | 1667.5578 |
| 25 | 0.0000 | 1907.4656 | 0.0000 | 0.0000 |
| 26 | 0.0000 | 12725.4563 | 0.0000 | 0.0000 |
| 27 | 0.0000 | 5708.8687 | 0.0000 | 0.0000 |
| 28 | 0.0000 | 1785.7125 | 0.0000 | 0.0000 |
| 29 | 0.0000 | 0.0000 | 4809.0873 | 0.0000 |

$$\begin{cases} \sum_{k=1}^m [\sigma^+(a_k) - \sigma^-(a_k)] \leq Z^* + \epsilon \\ \text{all the constraint of linear program (9)} \end{cases} \tag{A12}$$

where Z^* is the optimal value of linear program 9 and ϵ is a very small positive number.

Table F1
Optimal cultivation magnitude in detail for crops in group B.

| City (j) | A ₈ | A ₁₃ | A ₁₇ |
|----------|----------------|-----------------|-----------------|
| 1 | 0.0000 | 0.0000 | 3123.4255 |
| 2 | 0.0000 | 352.8561 | 1007.6036 |
| 3 | 0.0000 | 0.0000 | 2668.4727 |
| 4 | 0.0000 | 0.0000 | 1064.4727 |
| 5 | 0.0000 | 0.0000 | 750.2345 |
| 6 | 0.0000 | 0.0000 | 808.5618 |
| 7 | 0.0000 | 0.0000 | 72.1800 |
| 8 | 696.4062 | 0.0000 | 0.0000 |
| 9 | 2028.0610 | 0.0000 | 0.0000 |
| 10 | 5592.9503 | 0.0000 | 0.0000 |
| 11 | 2030.0338 | 0.0000 | 0.0000 |
| 12 | 3833.1931 | 0.0000 | 0.0000 |
| 13 | 1949.1481 | 0.0000 | 0.0000 |
| 14 | 0.0000 | 1113.8078 | 0.0000 |
| 15 | 0.0000 | 1484.7013 | 0.0000 |
| 16 | 0.0000 | 1271.6348 | 0.0000 |
| 17 | 0.0000 | 1220.9047 | 0.0000 |
| 18 | 3817.4105 | 0.0000 | 0.0000 |
| 19 | 0.0000 | 6889.1494 | 0.0000 |
| 20 | 0.0000 | 2511.7043 | 0.0000 |
| 21 | 6030.9168 | 0.0000 | 0.0000 |
| 22 | 4799.8759 | 0.0000 | 0.0000 |
| 23 | 0.0000 | 1784.5727 | 0.0000 |
| 24 | 1088.9977 | 0.0000 | 0.0000 |
| 25 | 834.5037 | 0.0000 | 0.0000 |
| 26 | 3418.9005 | 1227.6688 | 0.0000 |
| 27 | 2497.5926 | 0.0000 | 0.0000 |
| 28 | 781.2375 | 0.0000 | 0.0000 |
| 29 | 2266.7724 | 0.0000 | 0.0000 |

Table G1
Time complexity of the mathematical model presented in this research.

| Model | Execution time (in seconds) |
|--|-----------------------------|
| Calculating Range of Weights of Criteria | 30.12 |
| Calculating Optimal Weights of Criteria | 42.34 |
| Calculating Optimal Amount of Crops | 71.04 |

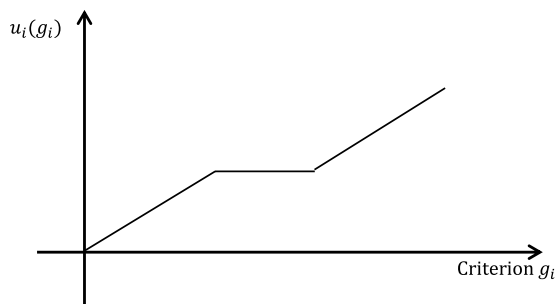


Fig. A1. Marginal utility function.

Appendix B

See [Table A1-G1](#).
See [Fig. A1](#).

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