

## Direct torque and flux regulation of synchronous reluctance motor drives based on input–output feedback linearization

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### ABSTRACT

In this paper, a nonlinear speed tracking controller is introduced for three-phase synchronous reluctance motor (SynRM) on the basis of input–output feedback linearization (IOFL), considering the different control strategies (maximum torque per Ampere, high efficiency and minimum KVA rating for the inverter) related to this motor. The proposed control approach is capable of decoupling control of stator flux and motor generated torque. The validity and effectiveness of the method is verified by simulation and experimental results.

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### 1. Introduction

In recent years, the synchronous reluctance motor (SynRM) has received much attention for many applications due to its simple and rugged construction [1–3]. A SynRM is advantaged on induction motor by the absence of rotor copper losses, on brushless motors by inexpensive rotor structure, and on switched reluctance motor by a much lower torque ripple and low noise. Compared to Surface type Permanent Magnet Synchronous Motor (SPMSM), it is capable of high-speed operation and for use in high-temperature environments. From control point of view, a SynRM has some advantages such that it can be considered an alternative to induction motor in many applications, such as robotics, traction and low-cost drives. Also the SynRM is suitable for super high speed applications in machine tools and molecular pumps [4].

For high performance SynRM drive, it is desirable to achieve optimum operation at maximum torque per Ampere (MTPA), high efficiency and minimum KVA rating for the inverter [5–7]. Detailed discussions and analysis of the control of a SynRM is given in references [5,6]. The analysis is restricted to the ideal motor, in which saturation and iron losses are ignored. However, the control of the SynRM is highly affected by both magnetic saturation and presence of iron losses [7]. Accurate representation of saturation effects re-

quires detailed knowledge of magnetic behavior in both rotor  $d$  and  $q$  axes along with cross-saturation at different operating conditions. Due to the high reluctance associated with  $q$ -axis, it may be sufficient to consider magnetic saturation in  $d$ -axis only. The iron loss is considered in the SynRM by adding a shunt resistor in both  $d$  and  $q$  equivalent circuits [8] and authors' paper have considered aspects of the different control schemes when the effects of saturation and iron losses are taken into account. In [9], the motor parameters are online estimated on the basis of recursive least square (RLS) method, only using the proposed mathematical method and motor measured currents and voltages. In [10], the iron losses resistance is obtained by no-load test and the magnetic saturation is considered through a lookup table which shows the variation of direct axis inductance versus direct axis current while the little effect of magnetic saturation on parameter  $L_q$  is ignored.

In the past two decades many papers have been published which discuss the direct torque control (DTC) of induction motors [11–13], but a few papers have been reported regarding the DTC for SynRMs [14–20]. Although the conventional DTC [14–19] has merits of simple structure and excellent dynamic performance, but it shows some drawbacks such as switching frequency variation and a high sampling frequency is needed for its digital implementation. As a result, the high torque and current ripples which may deteriorate the performance of the drive system are produced [21].

To overcome the above drawbacks, in the last two decades, some researchers have tried to propose some different DTC space

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vector modulation (SVM) techniques or to improve switching state patterns [19,20]. In [19] a model-based predictive DTC has been presented for SynRM with constant switching frequency and relative long sampling time. To get that, the control algorithm calculates one step in advance the switching instants of two possible active voltage space phasors that build the demanding torque. Next, the trajectory of the stator flux is predicted with these two pre-selected voltage space phasors and the optimum of them, which leads to the best trajectory of the stator flux at the end of the cycle, is applied to the machine. The model-based of [19] is difficult to implement in practice and needs a lot of computation time and storage. In addition in [19], no any conventional strategy related to SynRM has been implemented. The iron loss has been ignored in the method described in [19]. Compared to [19], in this paper we introduce a new DTC–SVM scheme for SynRM in which the iron loss resistance is taken into account and can be applied for any control strategy (maximum torque per Ampere (MTPA), high efficiency and minimum KVA rating for the inverter) related to SynRM. In [20], a nonlinear method capable of high dynamic torque regulation and efficiency optimization of SynRM has been described based on input–output feedback linearization (IOFL) DTC–SVM. In [20], the SynRM efficiency is optimized by using Lagrange's theorem. Then, the efficiency optimization criterion and the motor torque are chosen as output variables.

The main purpose of this paper is to continue the research work described in [20] for the following gains:

- To achieve the SynRM direct torque and stator flux control.
- To eliminate two PI controllers employed in [20].
- To implement of MTPA and minimum input motor KVA rating control strategies, besides of efficiency-optimized strategy experimented in [20].

According to the authors little knowledge and search, this is the first time that the direct stator flux and torque control of SynRM is discussed based on IOFL DTC–SVM. To confirm the validity of the presented approach, simulation and experiments are carried out.

## 2. SynRM model including iron losses

In the synchronously rotating reference frame, the  $d$  and  $q$  axes equivalent circuits for the SynRM, including iron losses, have been described in [20]. Note that the resistance  $R_i$  represents the iron losses connected in parallel to both rotational and transient back EMF. From the equivalent circuit, we obtain that the electromagnetic torque  $T_e$  is proportional to the vector product of flux linkages and currents and can be obtained as (1), where  $P$  denotes the number of poles,  $L_d$  and  $L_q$  represent  $d$  and  $q$  axes inductances, respectively. Since  $R_i$  supplies an additional current path to each axis equivalent circuit, the torque depends not on measured terminal current,  $i_d^s$  and  $i_q^s$ , but on  $i_d^T$  and  $i_q^T$ . Therefore, the terminal currents can longer directly govern the torque.

$$\begin{aligned} T_e &= \frac{3}{2} \frac{P}{2} \cdot (\lambda_d \cdot i_q^T - \lambda_q \cdot i_d^T) = \frac{3}{2} \frac{P}{2} \left( \frac{1}{L_q} - \frac{1}{L_d} \right) \lambda_d \lambda_q \\ &= \frac{3}{2} \frac{P}{2} \cdot (L_d - L_q) \cdot i_d^T \cdot i_q^T = K_T i_d^T i_q^T \end{aligned} \quad (1)$$

Relation between  $(i_{dT}^e$  and  $i_{qT}^e)$  and  $(i_{ds}^e$  and  $i_{qs}^e)$  can be obtained as

$$\begin{bmatrix} i_d^s \\ i_q^s \end{bmatrix} = \begin{bmatrix} \left(1 + p \frac{L_d}{R_i}\right) & \frac{-W_e L_q}{R_i} \\ \frac{W_e L_d}{R_i} & \left(1 + p \frac{L_q}{R_i}\right) \end{bmatrix} \begin{bmatrix} i_d^T \\ i_q^T \end{bmatrix} \quad (2)$$

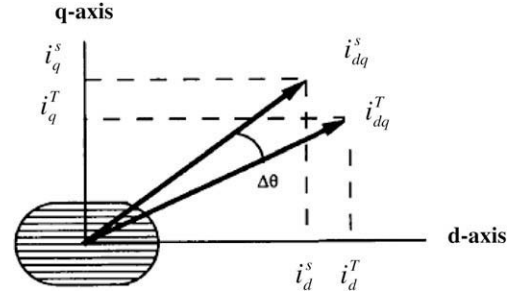


Fig. 1. The angle displacement between torque current ( $i_{dq}^T$ ) and terminal current ( $i_{dq}^s$ ) vectors.

Or

$$\begin{bmatrix} i_d^T \\ i_q^T \end{bmatrix} = \frac{R_i}{\left(p + \frac{R_i}{L_q}\right)\left(p + \frac{R_i}{L_d}\right) + W_e^2} \begin{bmatrix} \frac{1}{L_d} \left(p + \frac{R_i}{L_q}\right) & \frac{W_e}{L_q} \\ \frac{W_e}{L_q} & \frac{1}{L_q} \left(p + \frac{R_i}{L_d}\right) \end{bmatrix} \begin{bmatrix} i_d^s \\ i_q^s \end{bmatrix} \quad (3)$$

where  $p = \frac{d}{dt}$ . As shown in (3), the infinite  $R_i$  makes  $i_d^T$  and  $i_q^T$  identical to  $i_d^s$  and  $i_q^s$ , regardless of rotational speed  $\omega_e$ . Having ignored  $R_i$  the optimal angle for maximum torque per Ampere is equal to  $45^\circ$  [6]. However, non negligible  $R_i$  produces the cross-coupling effects between the  $d$  and  $q$  circuits in (2), resulting in an additional angle shift between the torque current and terminal current vector as shown in Fig. 1 [7]. This misalignment brings out the steady-state torque error and makes the optimal angle of each strategy different from that of the infinite  $R_i$  case. Consequently, for high dynamic torque regulation and every strategy of SynRM when the iron losses are included, the compensation of the cross-coupling term is required and the voltage equations for SynRM should be expressed using the torque currents, rather than the terminal currents, as

$$v_d = R_s i_d^T + \Re L_d \frac{di_d^T}{dt} - \Re L_q W_e i_q^T \quad (4)$$

$$v_q = R_s i_q^T + \Re L_q \frac{di_q^T}{dt} + \Re L_d W_e i_d^T \quad (5)$$

where  $\Re = \left(1 + \frac{R_s}{R_i}\right)$ . By assuming  $d$  and  $q$  axis fluxes as electrical states, (4) and (5) can be rewritten as

$$\dot{\lambda}_d = \frac{-R_s}{L_d \Re} \lambda_d + \omega_e \lambda_q + \frac{v_d}{\Re} \quad (6)$$

$$\dot{\lambda}_q = \frac{-R_s}{L_q \Re} \lambda_q - \omega_e \lambda_d + \frac{v_q}{\Re} \quad (7)$$

Choosing  $\lambda_d = x_1$ ,  $\lambda_q = x_2$  and  $\omega_e = x_3$  as states and  $v_d = u_1$ ,  $v_q = u_2$  as inputs, the nonlinear dynamic model for the SynRM considering iron losses can be described in the following standard state-variable form:

$$\dot{X} = f(X) + g(X)U \quad (8)$$

where  $X = [x_1 \ x_2 \ x_3]^T$ ,  $U = [u_1 \ u_2]^T$

$$\begin{aligned} f(X) &= \begin{bmatrix} f_1 \\ f_2 \\ f_3 \end{bmatrix} = \begin{bmatrix} -\frac{R_s}{L_d \Re} x_1 + x_2 x_3 \\ -\frac{R_s}{L_q \Re} x_2 - x_1 x_3 \\ \left(\frac{3P}{4J_m} \left(\frac{1}{L_q} - \frac{1}{L_d}\right) x_1 x_2 - \frac{T_l}{J_m}\right) / \frac{P}{2} - \frac{B_m \omega_e}{J_m} \end{bmatrix}, \\ g(X) &= [g_1 \ g_2] = \begin{bmatrix} \frac{1}{\Re} & 0 \\ 0 & \frac{1}{\Re} \\ 0 & 0 \end{bmatrix} \end{aligned} \quad (9)$$

where  $J_m$  is the rotor moment of inertia and  $B_m$  is the friction coefficient.

### 3. DTC-SVM of SynRM

According to the nonlinear model of SynRM, the linear control methods are not useful for wide range operation of SynRM. The Input–Output Feedback Linearization (IOFL) method is one of the nonlinear control methods that can be used to control of nonlinear plants such as SynRM.

Choosing the motor torque and the square of stator flux magnitude as output variables, output vector  $y = [y_1 \ y_2]^T$  can be defined as

$$\begin{aligned} y_1 &= T_e = \frac{3}{2} \frac{P}{2} \left( \frac{1}{L_q} - \frac{1}{L_d} \right) \lambda_d \lambda_q = \beta \lambda_d \lambda_q \\ y_2 &= |\lambda_s|^2 \end{aligned} \quad (10)$$

Taking the time derivatives of these outputs, gives

$$\begin{bmatrix} \dot{y}_1 \\ \dot{y}_2 \end{bmatrix} = \begin{bmatrix} L_f y_1 \\ L_f y_2 \end{bmatrix} + \begin{bmatrix} L_{g_1} y_1 & L_{g_2} y_1 \\ L_{g_1} y_2 & L_{g_2} y_2 \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \end{bmatrix} = \begin{bmatrix} L_f y_1 \\ L_f y_2 \end{bmatrix} + E(X)U \quad (11)$$

where  $L_f y_i$ ,  $i = 1, 2$ , is the Lie derivative of  $y_i$  with respect to  $f$ . From (9), a first internal dynamic can be recognized and its stability will be proved later.  $L_f y_i$  and  $E(X)$  are given in the paper Appendix I. The matrix  $E(X)$  is found to be nonsingular over all operating regions except null states.

Based on input–output feedback linearization the following control is introduced:

$$U = E^{-1} \begin{bmatrix} v_1 - L_f y_1 \\ v_2 - L_f y_2 \end{bmatrix} \quad (12)$$

Assuming the following state variables

$$\begin{aligned} \dot{y}_1 &= v_1 \\ \dot{y}_2 &= v_2 \end{aligned} \quad (13)$$

The system control efforts are defined by

$$\begin{aligned} v_1 &= -K_1 e_1 + \dot{T}_{ref} \\ v_2 &= -K_2 e_2 + |\dot{\lambda}_{sref}|^2 \end{aligned} \quad (14)$$

where  $K_1$  and  $K_2$  are positive constants and  $e_1 = T_e - T_{eref}$  and  $e_2 = |\lambda_s|^2 - |\lambda_{sref}|^2$ . Subscript ‘ref’ denotes the reference value.

In this paper, the nonlinear dynamics of the SynRM can be decomposed into an input–output part as (13) and an unobservable one by input–output linearization technique because total relative degree is not equal to the number of states. Since the stability of the whole SynRM dynamics is influenced not only by the input–output part, but also by the unobservable part, the behavior of the internal dynamics must be investigated. The corresponding internal dynamics of the SynRM in this paper can be given as (15), and the zero dynamics for checking the stability of internal dynamics is given as (16), where all outputs are maintained at zero. Although the zero dynamics are marginally stable as (16), the actual dynamics are supposed to be asymptotically stable due to the mechanical losses and viscosity damping [10]. Therefore, the whole system is said to be asymptotically minimum phase, because the zero dynamics of the SynRM system is stable.

$$\dot{x}_3 = \left( \frac{3P}{4J_m} \left( \frac{1}{L_q} - \frac{1}{L_d} \right) \lambda_{ds} \lambda_{qs} - \frac{T_l}{J_m} \right) / \frac{P}{2} - \frac{B_m x_3}{J_m} \quad (15)$$

$$\dot{x}_3 = \left( -\frac{T_l}{J_m} \right) / \frac{P}{2} - \frac{B_m x_3}{J_m} \quad (16)$$

### 4. SynRM control strategies

In this paper, the three well-known control strategies relating to SynRM (MTPA, efficiency-optimized and minimum KVA rating for the inverter) are considered under the constraint of constant tor-

que production. In MTPA strategy, the minimization of SynRM stator current, in efficiency-optimized scheme, the minimization of input active power and in minimum KVA, the minimization of SynRM input apparent power are selected as control objectives. Based on Lagrange’s theorem, it can be easily found that each strategy is satisfied when the torque curve and control objective curve are tangent at a point.

#### 4.1. MTPA control

The maximum torque per Ampere can be obtained by minimizing the expression for the stator current under the condition of constant torque production at a certain speed.

The square stator current  $I_s^2$  of the SynRM can be calculated as

$$I_s^2 = i_d^s{}^2 + i_q^s{}^2 = (i_d^T + i_d^I)^2 + (i_q^T + i_q^I)^2 \quad (17)$$

where  $i_d^I$  and  $i_q^I$  are the currents responsible for iron losses, which can be calculated as

$$i_d^I = -\omega_e \frac{L_q}{R_i} i_q^T, \quad i_q^I = \omega_e \frac{L_d}{R_i} i_d^T \quad (18)$$

Thus, the stator current vector can be expressed as (19) using (17) and (18)

$$I_s^2 = i_d^T{}^2 + i_q^T{}^2 + \frac{1}{R_i^2} (L_d^2 i_d^T{}^2 + L_q^2 i_q^T{}^2) \omega_e^2 + \frac{2}{R_i} (L_d - L_q) i_d^T i_q^T \omega_e \quad (19)$$

#### 4.2. Efficiency-optimized control

The maximum efficiency method can be obtained by minimizing the expression for the power into the machine under the constraint of constant power output. The input power  $P_{in}$  of the SynRM is obtained as

$$P_{in} = \frac{3}{2} (v_d i_d^s + v_q i_q^s) \quad (20)$$

Using (2)–(7) in steady-state condition,  $P_{in}$  can be expressed as (21)

$$\begin{aligned} P_{in} &= R_s (i_d^T{}^2 + i_q^T{}^2) + \frac{1}{R_i} \left( 1 + \frac{R_s}{R_i} \right) (L_d^2 i_d^T{}^2 + L_q^2 i_q^T{}^2) \omega_e^2 \\ &\quad + \frac{2R_s}{R_i} (L_d - L_q) i_d^T i_q^T \omega_e \end{aligned} \quad (21)$$

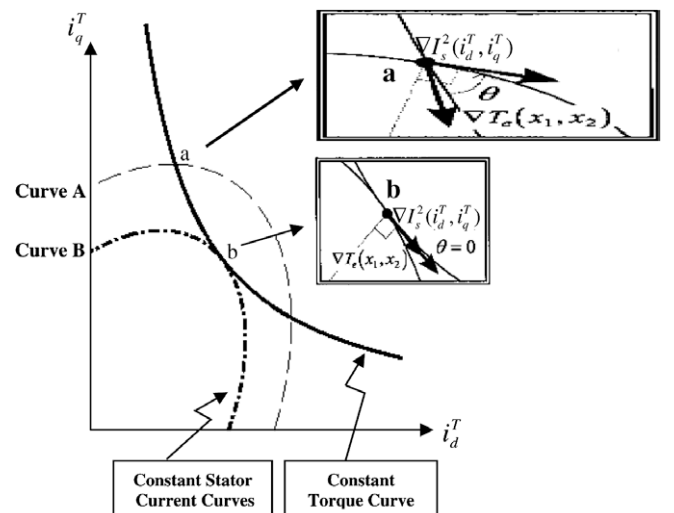


Fig. 2. Constant torque curve and stator current curve on  $i_d^T$ – $i_q^T$  plane.

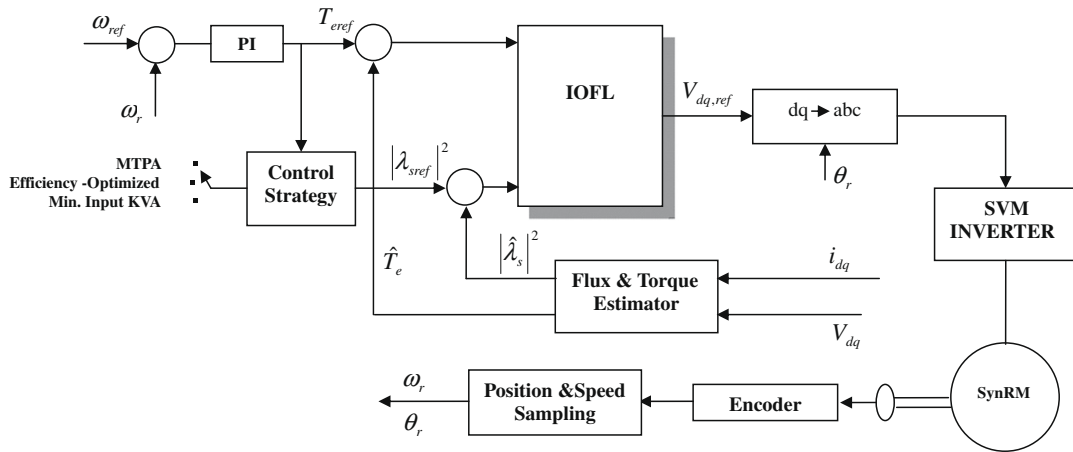


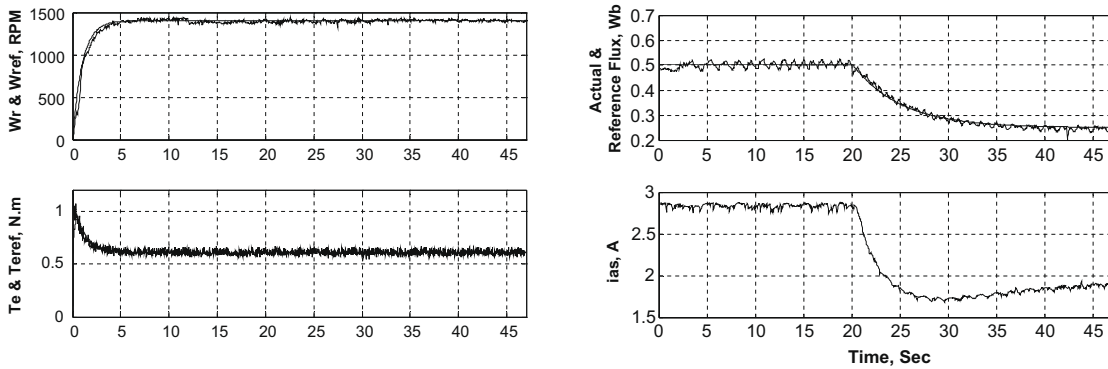
Fig. 3. Block diagram of SynRM drive system control.

4.3. Minimum input KVA control strategy

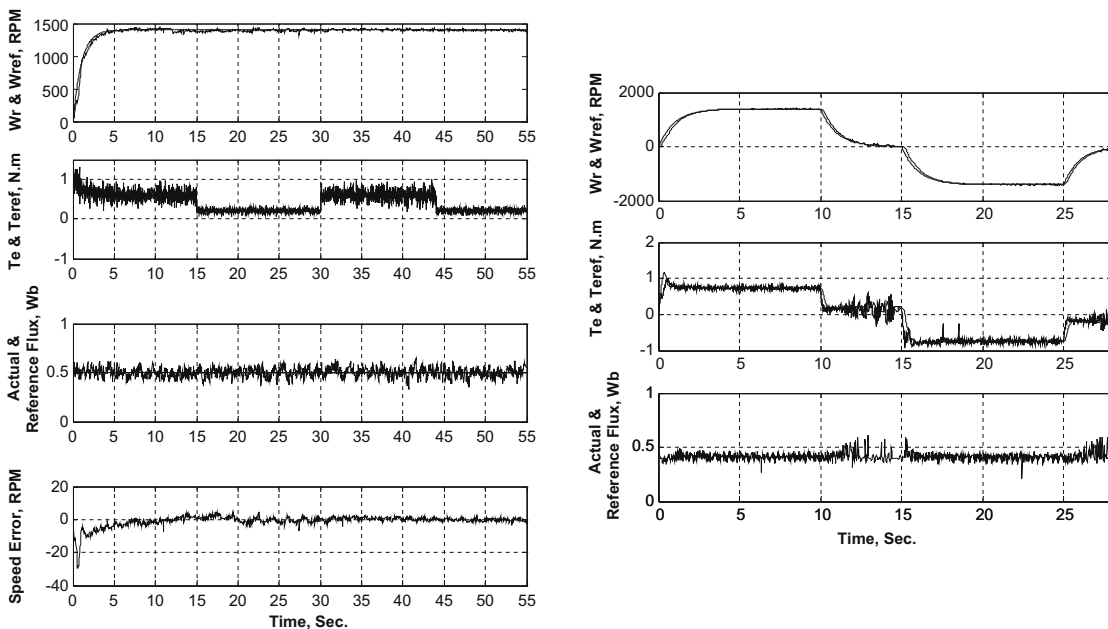
In order to obtain an expression for the minimum input KVA, one can minimize input apparent power  $S_{in}$  under the condition

of constant power output. The input apparent power  $S_{in}$  of the SynRM is obtained as

$$S_{in}^2 = V_s^2 I_s^2 = (v_d^2 + v_q^2) I_s^2 \tag{22}$$

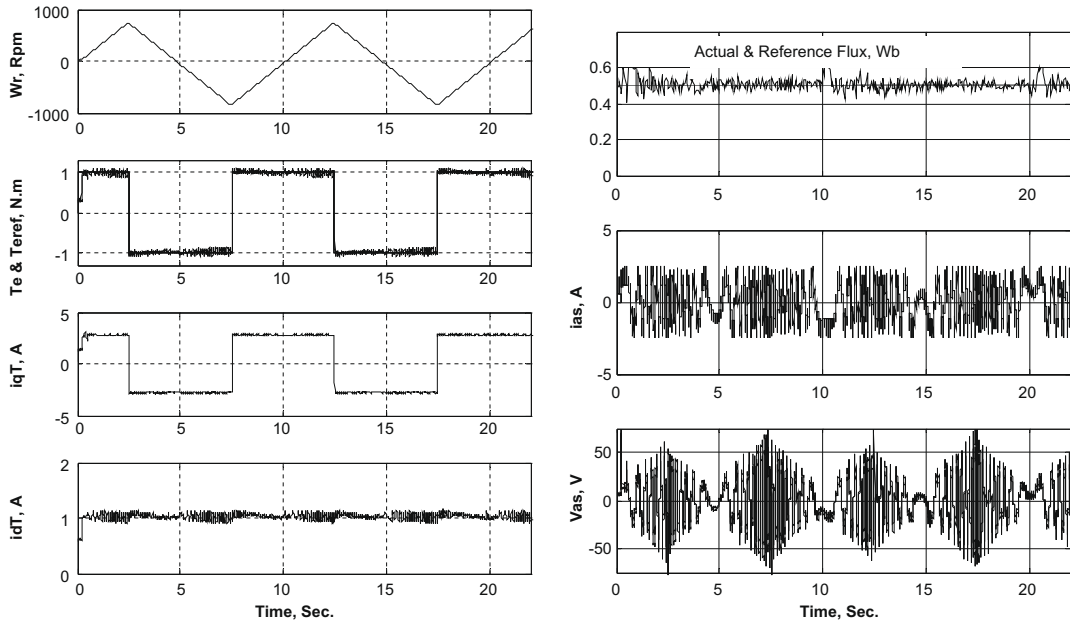


(a) Stator Flux Control

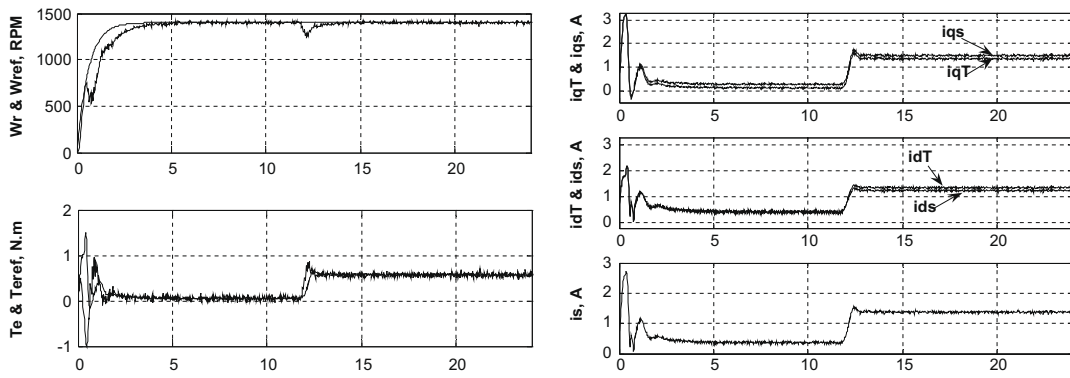


(b) Torque Control

Fig. 4. Simulation results.



(c) Efficiency-Optimized Control Strategy



(d) MTPA Control Strategy

Fig. 4 (continued)

Using (2)–(5), and (19) in steady-state condition,  $S_{in}$  can be expressed as

$$S_{in}^2 = \frac{\omega_e^4}{R_i^2} (L_d^4 i_d^4 + L_q^4 i_q^4) + \omega_e^2 (L_d^2 i_d^2 + L_q^2 i_q^2) + \frac{2\omega_e^3}{R_i} (L_d - L_q) (L_d^2 i_d^2 i_q^2 + L_q^2 i_d^2 i_q^2) \quad (23)$$

In this paper, the minimization of Eqs. (19), (21) or (23) is regarded as one of the control objectives under the constraint of constant production. In Fig. 2, according to Eq. (1), the constant torque curve can be drawn as a hyperbola on the  $i_d^T - i_q^T$  plane. On the same plane, at a speed, a curve representing every strategy, takes the form of an ellipse. Under the constraint of constant torque production, if an operating point is set at point “a” in Fig. 2, the curve A is supposed to be a control objective curve such as constant stator current curve. If an operating point is set at “b”, the curve B is another control objective curve. Based on Lagrange’s Theorem [20], it can be easily found that control objective is minimum when the torque curve and control objective curve are tangent at a point if and only if their gradient vectors are parallel. This means that  $\nabla T_e(i_d^T, i_q^T)$  must be a scalar multiple of  $\nabla(I_s^2, P_{in}$  or  $S_{in})$  at the point of tangency (see “b” in Fig. 2), so that

$$\|\nabla T_e(i_d^T, i_q^T)\| \|\nabla I_s^2(i_d^T, i_q^T)\| \sin \theta = 0 \quad \text{in MTPA} \quad (24)$$

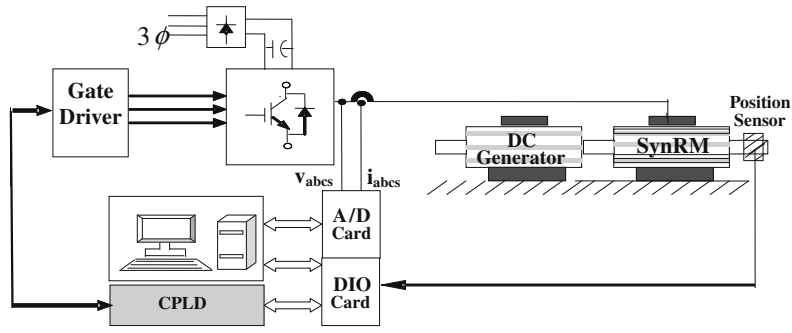
$$\|\nabla T_e(i_d^T, i_q^T)\| \|\nabla P_{in}(i_d^T, i_q^T)\| \sin \theta = 0 \quad \text{in efficiency-optimized control} \quad (25)$$

$$\|\nabla T_e(i_d^T, i_q^T)\| \|\nabla S_{in}(i_d^T, i_q^T)\| \sin \theta = 0 \quad \text{in min. KVA} \quad (26)$$

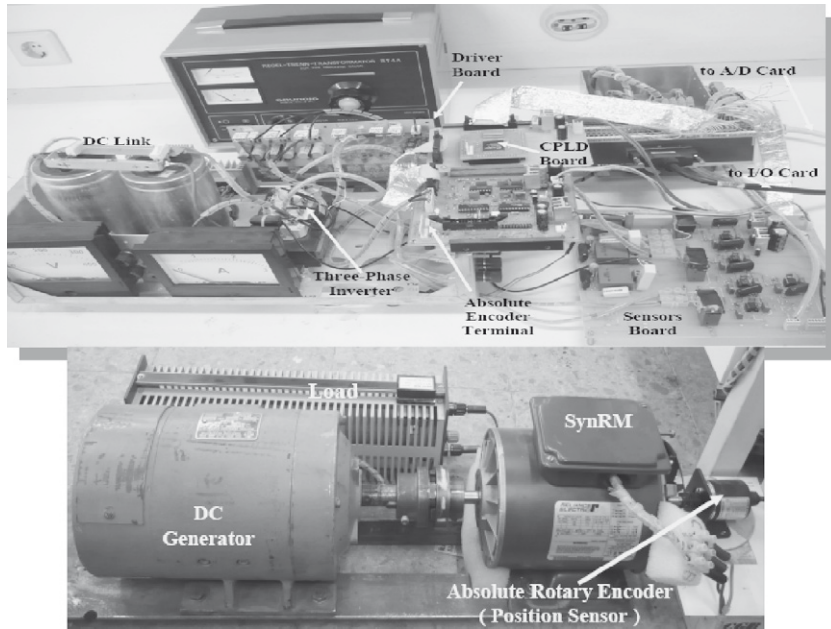
where  $\theta$  is the angle between  $\nabla T_e(i_d^T, i_q^T)$  and  $\nabla(I_s^2, P_{in}$  or  $S_{in})$ .

#### 4.4. MTPA strategy

$$\begin{aligned} & \|\nabla T_e(i_d^T, i_q^T)\| \|\nabla I_s^2(i_d^T, i_q^T)\| \sin \theta \\ &= 2K_T \left[ \left(1 + \frac{L_q^2}{R_i^2} \omega_e^2\right) i_q^T - \left(1 + \frac{L_d^2}{R_i^2} \omega_e^2\right) i_d^T \right] \\ &= 0 \Rightarrow i_q^T = \pm i_d^T \cdot \sqrt{\frac{\left(1 + \frac{L_q^2}{R_i^2} \omega_e^2\right)}{\left(1 + \frac{L_d^2}{R_i^2} \omega_e^2\right)}} \end{aligned} \quad (27)$$

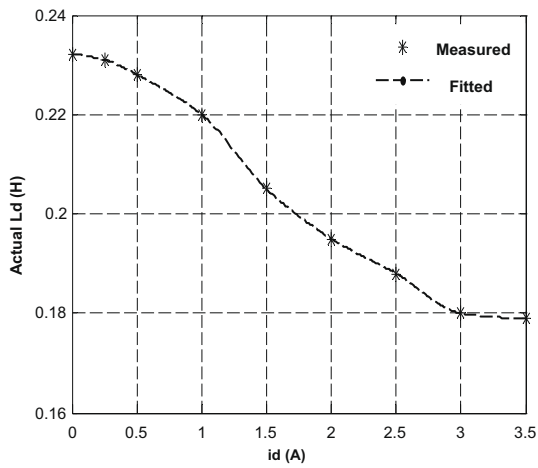


(a) Laboratory Implementation Block Diagram

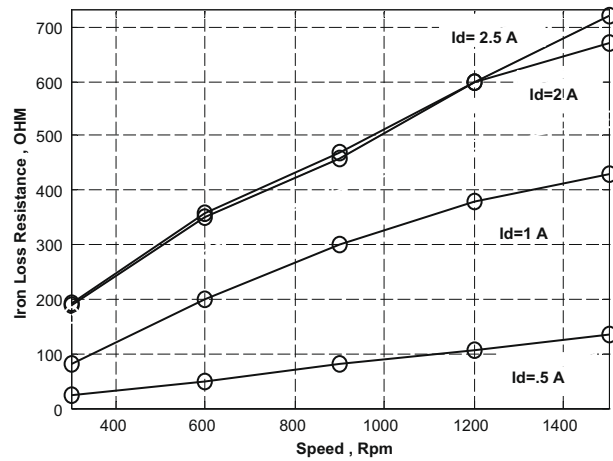


(b) SynRM Drive System Hardware

Fig. 5. Experimental setup.



(a) Variation of d-axis inductance  $L_d$  with d-axis current  $i_d$



(b) Measured Iron Loss Resistance  $R_i$

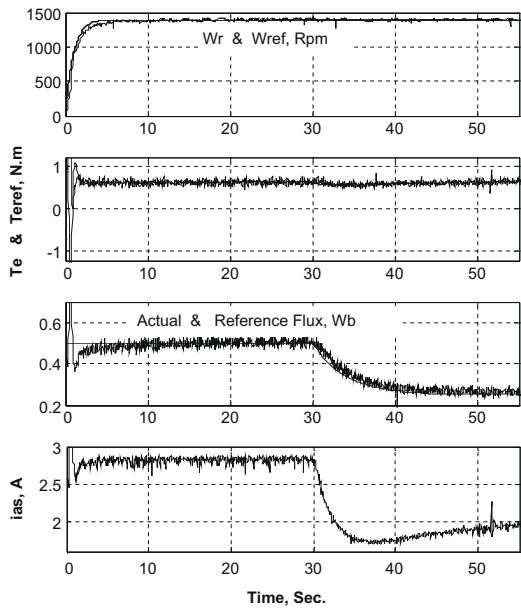
Fig. 6. Parameter variations: (a) d-axis inductance  $L_d$  with d-axis current  $i_d$  and (b) iron loss resistance  $R_i$ .

4.5. Efficiency-optimized control strategy

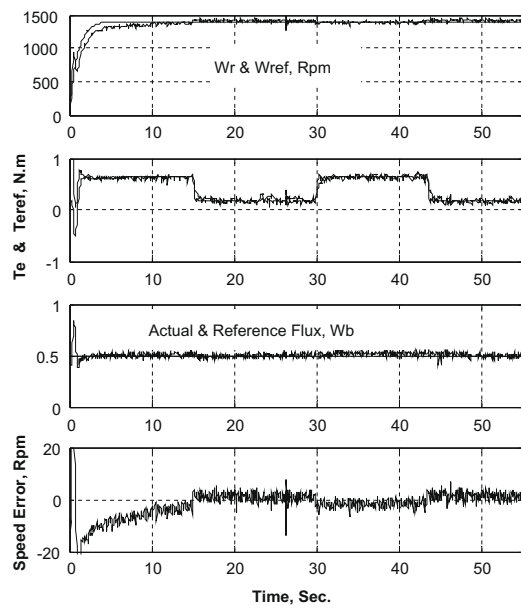
$$\begin{aligned} & \|\nabla T_e(i_d^T, i_q^T)\| \|\nabla P_{in}(i_d^T, i_q^T)\| \sin \theta \\ &= 3K_T \left[ \left( R_s + \frac{1}{R_i} \left( 1 + \frac{R_s}{R_i} \right) L_d^2 \omega_e^2 \right) i_q^{T^2} - \left( R_s + \frac{1}{R_i} \left( 1 + \frac{R_s}{R_i} \right) L_q^2 \omega_e^2 \right) i_d^{T^2} \right] \\ &= 0 \Rightarrow i_q^T = \pm i_d^T \cdot \sqrt{\frac{\left( R_s + \frac{1}{R_i} \left( 1 + \frac{R_s}{R_i} \right) L_q^2 \omega_e^2 \right)}{\left( R_s + \frac{1}{R_i} \left( 1 + \frac{R_s}{R_i} \right) L_d^2 \omega_e^2 \right)}} \end{aligned} \quad (28)$$

4.6. Min. KVA strategy

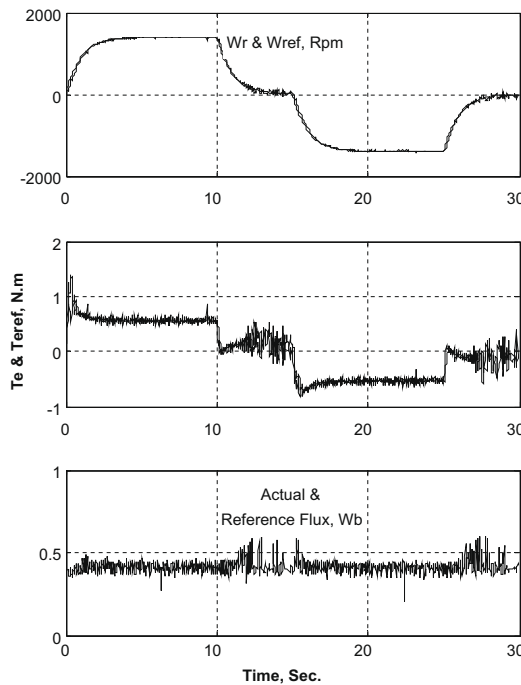
$$\begin{aligned} & \|\nabla T_e(i_d^T, i_q^T)\| \|\nabla S_{in}(i_d^T, i_q^T)\| \sin \theta \\ &= 0 \Rightarrow \frac{\omega_e^2}{R_i^2} \left( L_q^4 i_q^{T^4} - L_d^4 i_d^{T^4} \right) + \left( L_q^2 i_q^{T^4} - L_d^2 i_d^{T^4} \right) \\ &+ \frac{\omega_e}{R_i} (L_d - L_q) \left\{ L_q^2 i_q^{T^3} i_d^{T^4} - L_d^2 i_d^{T^3} i_q^{T^4} \right\} = 0 \end{aligned} \quad (29)$$



(a) stator Flux Control



(b) Direct Torque Control



(c) Direct Torque Control (with a Two-directional Speed Reference Signal)

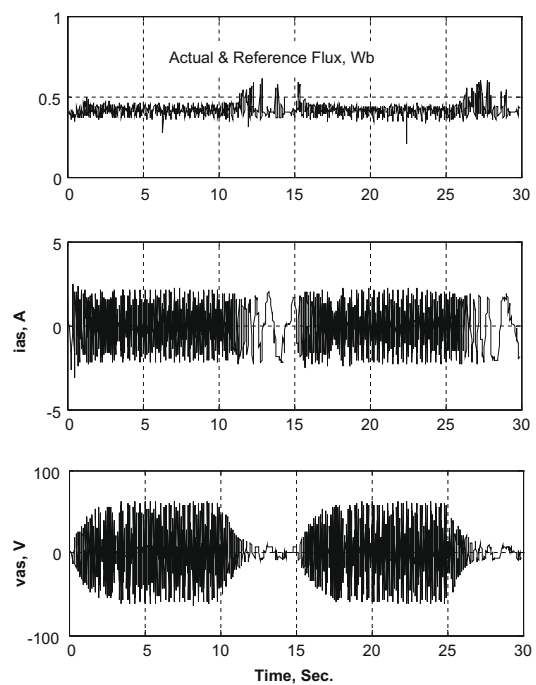
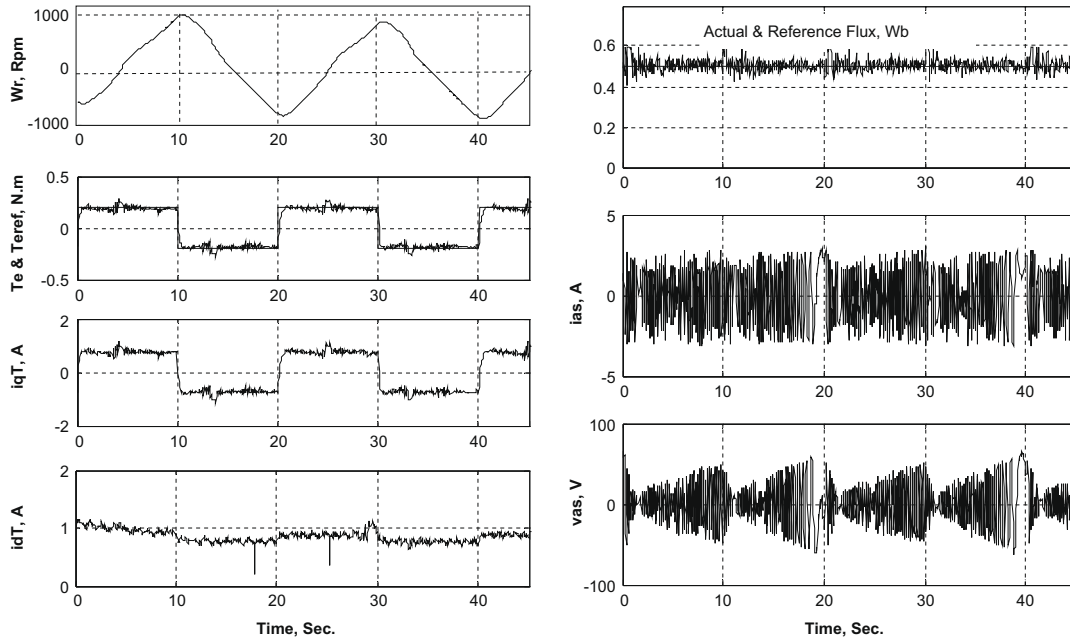


Fig. 7. Experimental results (Decoupled Stator Flux and Torque Control of SynRM).

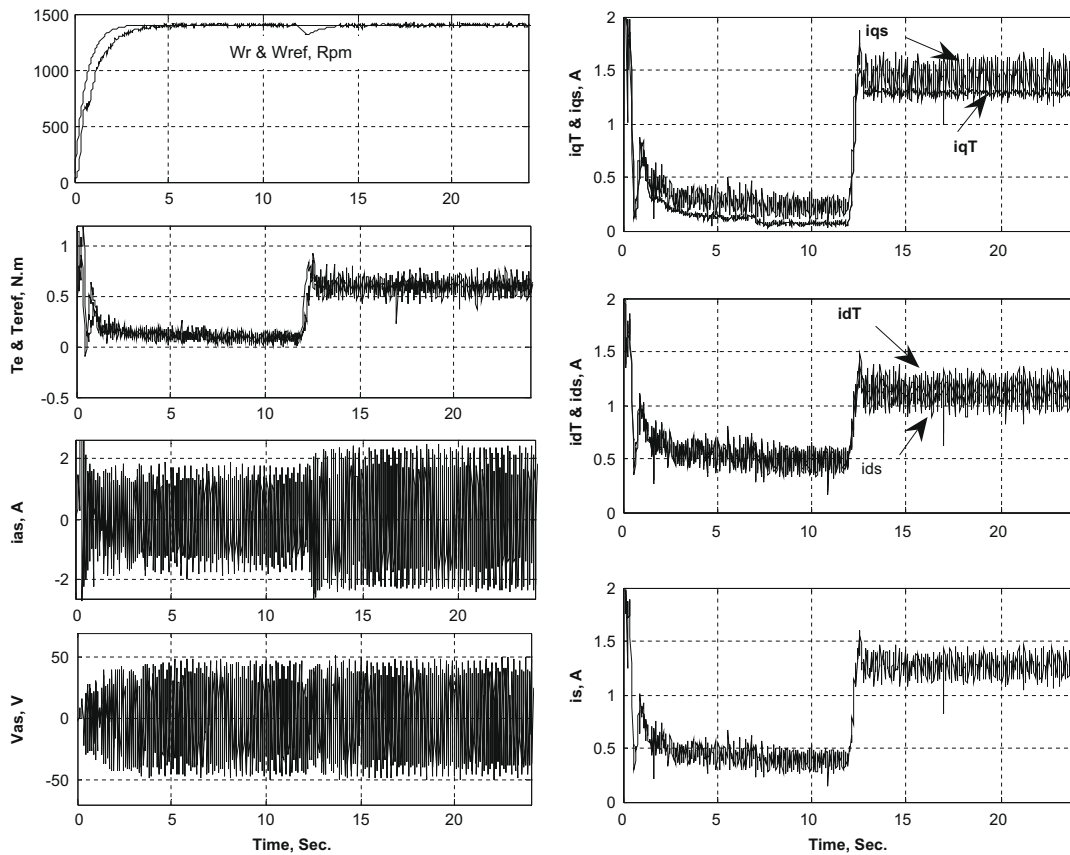
### 5. Simulation results

Overall block diagram of the drive system control is shown in Fig. 3. Based on IOFL the motor supply voltage is synthesized from stator  $d$  and  $q$  axis voltage commands ( $v_d^*, v_q^*$ ), using a two level

space vector modulation SVM-based PWM inverter. A C++ step by step computer program was developed to model the drive system control of Fig. 3. In this program, the system dynamic equations are solved by a static Range–Kutta fourth order method. In our proposed control approach the system controller gains are obtained



(a) Efficiency-Optimized Control Strategy



(b) MTPA Control Strategy

Fig. 8. Experimental results: (a) efficiency-optimized control strategy and (b) MTPA control strategy.



by trial and error method which are given by  $K_p = 0.3$ ,  $K_i = 0.05$  and  $K_1 = K_2 = 225$ . The specifications and parameters of three-phase SynRM used in our simulation program are given in Appendix II. Simulation results obtained for SynRM direct stator flux and torque control are shown in Fig. 4a and b. From these results one can see that for a chosen stator flux and torque reference signals, the SynRM rotor speed is properly tracked. Considering MTPA and efficiency-optimized control strategies relating to SynRM, the simulated results are presented in Fig. 4c and d. As shown in figures, the torque and flux references are well regulated to the respective commands and the internal states ( $i_d^r, i_q^r$ ) move to the optimal point along the demanded torque curves. The speed  $\omega_e$  increases and decreases rather linearly which means that the produced torque is regulated well to its desired value by the help of the proposed nonlinear controller.

## 6. Experimental setup and results

### 6.1. Experimental system setup

For practical evaluation of the actual system performance, a PC-based prototype system was built and tested. The experimental setup corresponding to overall system block diagram shown in Fig. 3 is depicted in Fig. 5 and consists of the following sections.

A 0.37 kW three-phase SynRM and a 1.1 kW DC generator as its load; Three-phase voltage source inverter and its isolation board; Voltage and current sensors board; 96 bit Advantech digital Input–Output card; 32-channel Advantech A/D converter card; CPLD board and a personal computer (PC) for calculating required signals and viewing the registered waveforms. The 0.37 kW SynRM parameters are reported in Appendix II.

The SynRM is supplied by a three-phase inverter with a symmetrical two level space vector modulation. A Xilinx XC95288xl CPLD has been selected for real time implementation of switching patterns using a switching frequency of 5 kHz.

The CPLD board communicates with PC via the digital Advantech PCI-1753 I/O board. CPLD in experimental setup realizes the following tasks: Switching pattern generation of IGBT switches based on SVM technique, providing a useful dead time in the so-called switching patterns of power switches, generation of the synchronizing signal for data transmission between PC and hardware and shutting down the inverter in the case of emergency conditions such as over current or PC hanging states. The inverter has been designed & implemented specifically for this experiment using SKM75 GD 124 D SEMIKRON module.

The required drive board has been designed by hcPL 316 J which is fast and intelligent IGBT driver and guarantees a reliable isolation between the high voltage and control boards. The DC link voltage and stator phase currents and voltages are measured by Hall-type LEM sensors. All measured electrical signals are filtered using the separate analogue second order low pass filters with 1.5 kHz bandwidth which is enough higher than our operating frequency and then converted to digital signals using an A/D card with 10  $\mu$ s conversion time. The rotor position is measured in respect to axis of stator “A” phase using an AUTONICS absolute encoder with 1024 pulses per round. The output pulse of position sensor is sent to the PC via I/O card.

### 6.2. Experimental results

Using the same conditions adopted to get SynRM simulation results as described in previous section, the experimental results were obtained as shown in Figs. 7 and 8. The motor  $d$ -axis inductance  $L_d$  versus  $i_d$  has been obtained from a practical test, considering Fig. 6a. The iron loss resistance  $R_i$  can be acquired by measuring

**Table I**

Specifications and parameters of three-phase SynRM for simulations and experiments.

$P_n = 370$ W	$V_n = 230$	$I_n = 2.8$ A
$L_{md,unsat} = 232$ mH	$L_{md,sat} = 178$ mH	$L_{mqn} = 118$ mH
$R_{sn} = 2.95$ $\Omega$	$f_n = 60$ Hz	No. of poles = 4
$T_{en} = 1.9$ Nm	$J_m = .015$ Kg m <sup>2</sup>	$B_m = .003$ Nm/rad/s

the input power under no-load condition and the measured results has been plotted in Fig. 6b. Since  $R_i$  varies with operating frequency and magnetizing current, this value is updated to the controller in real time according to the load condition and speed.

Experimental results obtained for SynRM direct stator flux and torque control are shown in Fig. 7. From these results one can see that for a chosen stator flux and torque reference signals, the SynRM rotor speed is properly tracked. Considering Efficiency-Optimized control and MTPA strategies relating to SynRM, the simulated results are presented in Fig. 8a and b, respectively. A close agreement can be seen between simulation and practical results and a little disagreement seen between these two set of results can be described by inaccuracies that exist in our data acquisition system, SVPWM voltage source inverter effects and the dead times of inverter switching signals.

## 7. Conclusion

In this paper, at the first, the SynRM direct stator flux and torque control has been discussed using input–output feedback linearization. In addition, based on proposed control approach, the control strategies of MTPA, optimized-efficiency and minimum input KVA related to SynRM have been adapted. A close agreement can be seen between simulation and practical results and a little disagreement seen between these two set of results may be because of inaccuracies that exist in our data acquisition system, SVPWM voltage source inverter effects and the dead times of inverter switching signals.

## Appendix I

$$L_f y_1 = -\beta \left( \frac{R_s}{\Re} \lambda_d \lambda_q \left( \frac{1}{L_d} + \frac{1}{L_q} \right) + \omega_e (\lambda_d^2 - \lambda_q^2) \right) \quad (A1)$$

$$L_f y_2 = -\frac{R_s}{\Re} \left( \frac{\lambda_d^2}{L_d} + \frac{\lambda_q^2}{L_q} \right) \quad (A2)$$

$$E(X) = \begin{bmatrix} \beta \lambda_q & \beta \lambda_d \\ 2 \lambda_d & 2 \lambda_q \end{bmatrix} \quad (A3)$$

## Appendix II

See Table I.

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