Secure Data Transmission Using Qubits

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Abstract

A quantum protocol for secure transmission of data using qubits is presented. This protocol sends one qubit in a round-trip to transmit one bit of data. The protocol offers an improvement over the BB84 QKD protocol. BB84, in conjunction with one-time pad encryption, has been shown to be unconditionally secure. However its security relies on the assumption that the qubit source device does not emit multiple replicas of the same qubit for each transmitted bit. If this happens a multi-qubit emission attack can be launched. In addition, BB84 cannot be used to send predetermined bit strings as it generates a random bit string in the process. Our protocol does not have the above drawbacks, but requires an authenticated public channel in order to detect an intruder, in the way as BB84. Our protocol does not require a shared secret key.

1. Introduction

Since the publication of the BB84 protocol [1], a growing class of quantum cryptographic protocols has emerged. BB84 and its variants [3, 6] aim at providing perfect security in transferring classical data between two parties. However, these protocols are key establishment protocols rather than data transfer protocols. They provide ultimate data security by generating a random sequence of bit which is shared between Alice and Bob. The sequence is then used as a one-time pad or as a symmetric key. Because this sequence is generated in the process of protocol execution, it cannot be known in advance. This can be a drawback in applications where a predefined sequence of bits is to be distributed securely. Our protocol can be used to avoid this drawback. Also, though expensive, in some applications it may be justifiable to use the quantum channel to send confidential data as opposed to using the classical channel. Our protocol can be used in those situations as well.

It has been shown that BB84 is unconditionally secure [2, 4]. However this fact depends on the assumption that the qubit source does not emit multiple replicas of the same qubit. In BB84, Alice generates a sequence of qubits which have been chosen at random from one of two predefined bases. She then sends a random sequence of bits using those qubits. Bob makes measurement on the qubits upon receipt and then waits for the basis information from Alice. The basis information comes through a public authenticated channel. If the qubit source emits multiple replicas for each intended qubit, an eavesdropper (Eve) on the quantum channel can capture and preserve the qubits until the basis is announced by Alice. At that time, Eve can perform measurement in the correct basis and obtain the bits send by Alice. This is called a multi-qubit emission attack. Our protocol is not vulnerable to this kind of attack because information crucial to correct measurement of the qubits is not transmitted or broadcast.

In our protocol, as in BB84 and other key exchange protocols, the availability of an authenticated (though not private) channel is an indispensable element. This channel is the very essential means by which Bob can identify Alice and differentiates her from Eve. In key exchange protocols without an authenticated channel, Eve can launch a successful man-in-the-middle attack. In our protocol, qubits are exchanged between Alice and Bob, and they must make sure that the qubits are not altered or inserted by Eve. An authenticated channel is required for them to ensure this.

Our protocol has two major advantages over BB84 (explained above), but it comes at a cost: The qubits must make a round trip instead of a one-way trip. At a time when sending qubits over long distances is a technical challenge, this requirement may sound too troublesome. However, there is a trade-off: A round trip must be weighted against the challenge of making a single-qubit source.

This paper is organized as follows: In the next section, we present the key ideas and properties used in our protocol. Then in Section 3, the proposed protocols are presented. In Section 4, we discuss the correctness and security of our
2. Preliminaries

In this paper, we have borrowed some key concepts from BB84. One key concept which is not from BB84 is the following: Suppose Bob wants to send one bit to Alice. Alice sends a random bit to Bob and she remembers this bit. Bob performs an exclusive-or between Alice’s bit and his bit and sends the result to back Alice. Alice can recover Bob’s bit. This is perfectly secure if Eve cannot inspect Alice’s bit on the way to Bob. If Eve inspects the bit being sent from Bob to Alice, she will not know Bob’s bit. Of course, we should also prevent the possibility of a man-in-the-middle attack by Eve. It is hard to realize the above idea in classical cryptography. However, in quantum cryptography this can be realized at least in one way that is presented in this paper.

The whole idea of quantum cryptography revolves around the concept of a qubit. A qubit $|\psi\rangle$ is a quantum state vector in a two dimensional Hilbert space $\mathbb{H}_2$. A qubit can be measured with respect to any given basis in $\mathbb{H}_2$. In quantum computation, the basis $\{|0\rangle, |1\rangle\}$ is called the computational basis. Measuring a qubit $|\psi\rangle = a|0\rangle + b|1\rangle$ in the computational basis will change it to $|0\rangle$ or $|1\rangle$ with probabilities $|a|^2$ and $|b|^2$, respectively. The observed outcome is logic value ‘0’ with probability $|a|^2$ or logic value ‘1’ probability $|b|^2$. Hereafter, whenever a qubit is "measured", we mean it is measured in the computational basis.

In protocols discussed in this paper, Alice and Bob rotate qubits around a known fixed axis in the Bloch sphere [7, page 15]. Without loss of generality and for the sake of convenience, we choose this axis to be the $y$-axis. To perform a rotation around the $y$-axis by an angle $\theta$, a given qubit $|\psi\rangle$ must be operated upon by the following operator:

$$R(\theta) = \left( \begin{array}{cc} \cos \frac{\theta}{2} & -\sin \frac{\theta}{2} \\ \sin \frac{\theta}{2} & \cos \frac{\theta}{2} \end{array} \right).$$

It is easy to verify that for all angles $\alpha$, $\beta$ and $\theta$, the following statements hold:

$$R(\alpha)R(\beta) = R(\beta)R(\alpha) = R(\alpha + \beta),$$

$$R^2(\theta) = R(-\theta).$$

We will work with the following family of qubits:

$$|\psi(\theta)\rangle = R(\theta)|0\rangle = \cos \frac{\theta}{2}|0\rangle + \sin \frac{\theta}{2}|1\rangle.$$

Since $|0\rangle$ is the state vector coinciding with the unit vector along the $z$-axis in the Bloch sphere, then every $|\psi(\theta)\rangle$ is a rotated version of the qubit $|0\rangle$ rotated by an angle $\theta$ around the $y$-axis in the $xz$-plane. Also be reminded that any two qubits whose Bloch sphere representations are colinear and point in opposite directions, e.g. $|\psi(\theta)\rangle$ and $|\psi(\theta + \pi)\rangle$, are orthogonal to each other and hence they can be detected and distinguished with perfect certainty.

Suppose $|\psi(\theta)\rangle$ is known by Alice to encode one of two logic values 0 or 1. If she makes measurement in the computational basis on this qubit, she will obtain 0 with probability $\cos^2 \frac{\theta}{2}$ and will obtain 1 with probability $\sin^2 \frac{\theta}{2}$. However if Alice knows the value of $\theta$, and if she operates $R^2(\theta)$ on this qubit before making measurement in the computational basis, then she will obtain 0 with probability 1 (perfect certainty).

Now suppose that Alice receives $|\phi\rangle$ and she knows this qubit is either $|\psi(\theta)\rangle$, or $|\psi(\theta + \pi)\rangle$. Without knowing $\theta$, if she makes measurement, the outcome will be 0 or 1 at random, the probability of each depending on the actual state she received. On the other hand, if Alice knows the value of $\theta$, she can perform the unitary operation $R^2(\theta)|\phi\rangle$ and then followed by measurement in the computational basis. With probability one, she will obtain 0 if $|\phi\rangle = |\psi(\theta)\rangle$ or obtain 1 if $|\phi\rangle = |\psi(\theta + \pi)\rangle$. Therefore with known angle $\theta$, the states $|\psi(\theta)\rangle$ and $|\psi(\theta + \pi)\rangle$ represent 0 and 1, respectively, and can be distinguished with perfect certainty.

In what follows, we use the random variable $X$ to denote the binary information transmitted, the random variable $Y$ to denote the binary information received by an intended party, and the random variable $Z$ to denote the information bit obtained by an intruder. Adopting Shannon’s definition, we deem a protocol as unconditionally secure if $H(X|Y) = 0$ and $H(X|Z) = H(X)$. The first condition means that $Y$ reveals everything about $X$. The latter means that $Z$ reveals nothing about $X$; this is true if and only if $X$ and $Z$ are independent.

We now prove some propositions that represent our key ideas and will be used later. (To keep this paper within the size limit, we have omitted the proofs of the propositions. The interested reader should consult [5] which is available online.) Consider a set of distinct angles $\{\theta_0, \theta_1, \ldots, \theta_{n-1}\}$, all in $[0, 2\pi]$. Suppose Alice prepares a qubit $|\psi\rangle = R(\theta_k + \pi X)|0\rangle$, where $\theta_k$ was selected with probability $p_k$, and $X \in \{0, 1\}$ is a binary random variable (which is Alice’s data).

**Proposition 1** If Alice sends the qubit to Bob. If Bob knows $\theta_k$, he can recover $X$ without error.

**Proposition 2** Alice sends the qubit to Bob. Eve, who does not knows $\theta_k$, intercepts and rotates it by an arbitrary angle of her choice $-\alpha$, makes measurement on the qubit and obtains a binary value $Z$. There exist a probability distribution $p_k$ and a set $\{\theta_0, \theta_1, \ldots, \theta_{n-1}\}$ such that $H(X|Z) = H(X)$. 


Proposition 3  Suppose Alice sends the qubit to Bob. Eve who does not knows \( \theta_k \) intercepts the qubit and performs a rotation by an angle of her choice \( \alpha \). She then makes measurement on the qubit and then transmits the resulting qubit, denoted \( |\phi_1\rangle \), to Bob. If Bob knows \( \theta_k \), and if he performs the following unitary operation \( |\phi_2\rangle = R(\theta)|\phi_1\rangle \) followed by a measurement of \( |\phi_2\rangle \), then the channel between Alice and Bob has an error probability \( \text{Prob}(\text{error}) \) equal to:

\[
\sum_{k=0}^{n-1} p_k \left[ \sin^2 \frac{\theta_k}{2} \cos^2 \frac{\theta_k - \alpha}{2} + \cos^2 \frac{\theta_k}{2} \sin^2 \frac{\theta_k - \alpha}{2} \right].
\]

Proposition 4  In Proposition 3, suppose we set

\[
p_n = \frac{1}{n}, \quad \theta_k = \frac{2k\pi}{n},
\]

then

\[
\text{Prob}(\text{error}) \geq \frac{1}{4},
\]

with equality when \( \alpha = 0 \).

This proposition means that by certain choice of \( p_k \)'s and \( \theta_k \)'s (as prescribed above) we can be sure that Eve's interaction will be detected with probability at least 1/4. Also, from the point of view of Eve, who wants to minimize her probability of being detected, this means that her best strategy is to do measurement only without any rotations. This result will be used in the analysis of our qubit authentication protocol (Protocol 1).

3. Proposed Protocol

First we present a protocol for sending authenticated qubits. Then we present a protocol for sending secure data using authenticated qubits.

3.1. Sending Authentic Qubits

We define an authentic qubit as a qubit which has been sent by Alice and received by Bob such that Eve has not altered it in any way along the way. Suppose Alice wants to send authentic qubits to Bob. For convenience, we restrict our discussion to the family of qubits residing in the \( xz \)-plane.

Protocol 1  Suppose Alice has a sequence of \( N \) qubits \( |\psi_1\rangle, |\psi_2\rangle, \ldots, |\psi_N\rangle \), and wishes to send them to Bob in an authenticated way. We assume that a classical bidirectional authenticated channel exists between Alice and Bob. Also assumed is a set of publicly-known distinct angles \( \theta_k = \frac{2k\pi}{n}, k = 0, 1, \ldots, n-1 \).

1. Alice selects \( M \) integers uniformly at random in \( \{0, 1, \ldots, n-1\} \), denoted \( k_1, k_2, \ldots, k_M \).
2. Alice creates qubits \( |\phi_1\rangle, |\phi_2\rangle, \ldots, |\phi_M\rangle \), such that for each \( i \in \{1, 2, \ldots, M\} \)

\[
|\phi_i\rangle = R(2k_i\pi/n)|0\rangle.
\]

We call these the check qubits.
3. Alice generates \( M \) distinct random integers \( j_1, j_2, \ldots, j_M \) in \( \{1, 2, \ldots, N + M\} \). She then creates a frame of length \( N + M \) and inserts each \( |\phi_i\rangle \) at location \( j_i \) in the frame. Then the sequence of qubits \( |\psi_1\rangle, |\psi_2\rangle, \ldots, |\psi_N\rangle \), are inserted at the empty locations in the frame preserving their order.
4. Alice sends the frame to Bob. Bob receives the frame.
5. Alice sends the following data to Bob:

\[
(j_1, k_1), (j_2, k_2), \ldots, (j_M, k_M).
\]

These data are sent via the classical authenticated channel. Eve can read these data.
6. Knowing \( j_i \)'s, Bob extracts the sequence of \( |\phi_i\rangle \)'s from the frame, and for each \( i = 1, 2, \ldots, M \), he performs \( R^\dagger(2k_i\pi/n)|\phi_i\rangle \). Then he measures the resulting state. The outcome must be a logical ‘0’ for all \( i \in \{1, 2, \ldots, M\} \). If this condition does not hold for any \( |\phi_i\rangle \), the frame is said to have an authentication error.
7. If there is an authentication error, Bob notifies Alice and both drop the frame. Otherwise, the frame is considered unaltered and the sequence of \( |\psi_i\rangle \)'s is deemed to be authentic.

At a given level of certainty (determined by parameters \( N \) and \( M \)), this protocol uses a classical authenticated channel to create an authenticated quantum channel. This protocol is analyzed in Section 4. We use this protocol as a tool to prevent the man-in-the-middle attack in our confidential data transfer protocol (Protocol 2).

3.2. Sending Confidential Qubits

In this section, we present a protocol that enables sending confidential data over the quantum channel. In this protocol, qubits make a round trip from Alice to Bob to Alice and undergo a unitary operation by Bob along the way. The protocol is described below.

Protocol 2  Suppose Bob has a sequence of \( N \) data bits \( x_1, x_2, \ldots, x_N \) where \( x_i \in \{0, 1\} \). The existence of a classical bidirectional authenticated channel exists between Alice and Bob is assumed.
1. Alice generates a sequence of random integers 
   \(k_1, k_2, \ldots, k_N\) where \(k_i \in \{0, 1, \ldots, n - 1\}\). She keeps these integers confidential to herself.

2. Alice creates \(n\) qubits \(|\psi_{11}\rangle, |\psi_{12}\rangle, \ldots, |\psi_{1N}\rangle\), such that 
   \[\psi_{1i} = R\left(\frac{2\pi k_i}{n}\right)|0\rangle.\]

3. Alice sends the \(N\) qubits to Bob using Protocol 1.

4. Bob receives the \(N\) authenticated qubits from Alice. On each \(|\psi_{1i}\rangle\), without making measurement, he performs the unitary operation \(R(\pi x_i)\) to produce the qubit sequence
   \[|\psi_{21}\rangle, |\psi_{22}\rangle, \ldots, |\psi_{2N}\rangle\]
   where \(|\psi_{2i}\rangle = R(\pi x_i)|\psi_{1i}\rangle\). This sequence is sent to Alice in an authenticated way using Protocol 1.

5. Alice receives the \(N\) authenticated qubits. On each qubit \(|\psi_{2i}\rangle\), she performs unitary operation \(R^\dagger(\frac{2\pi k_i}{n})\). The resulting sequence denoted
   \[|\psi_{31}\rangle, |\psi_{32}\rangle, \ldots, |\psi_{3N}\rangle\]
   is then measured to produce bit sequence \(y_1, y_2, \ldots, y_N\). This sequence is deemed to be the sequence sent by Bob.

As shown in Propositions 1 through 4, there seems to be no advantage in selecting \(n > 3\). Therefore we propose setting \(n = 3\) in both protocols.

4. Analysis

In this section, we analyze the two protocols to show that they indeed serve their intended purposes. In our analysis, we take advantage of the propositions set forward in the preliminary section. Since our primary purpose in this paper is introducing a protocol for confidential data transfer, we analyze Protocol 1 first while assuming Protocol 2 serves its purpose perfectly (i.e., sending authentic qubits).

4.1. Analysis of Protocol 2

We analyze this protocol in two steps: First we show it is correct, second, we show it is secure.

Correctness

We show that Protocol 2 works correctly by invoking Proposition 1. Notice that Alice prepares each qubit \(|\psi_{1i}\rangle\) at a certain angle \(\frac{2\pi k_i}{n}\), which she only knows. Bob encodes his data bit in the qubit by performing \(R(\pi x_i)|\psi_{1i}\rangle\). Doing so means that Alice’s qubit either remains the same or is rotated by an angle \(\pi\). In Proposition 1, Alice encodes her data and sends to Bob. If Bob knows the original qubit’s angle, he can recover Alice’s data. In the case of Protocol 2 (which is slightly different), it is Bob who encodes his data, but since he does not know the qubit’s angle, he sends it to Alice who (by the reason of Proposition 1) can recover Bob’s data without error. Therefore, Protocol 2 is correct.

Security

We show that Protocol 2 is secure. This means that an intruder (Eve) cannot recover Bob’s data. We do this in the following:

a) Note that if Eve can find out the angle \(\frac{2\pi k_i}{n}\) for each qubit \(|\psi_{1i}\rangle\), she, like Alice, can recover Bob’s data. An invocation of Proposition 2 will prove that this is not possible.

First notice that Protocol 2 uses the specific set of \(p_i\)'s and \(\theta_i\)'s that satisfies Proposition 2 for security. (The values are given in [5] in Proof of Proposition 2.) Next, notice that the first trip of a qubit from Alice to Bob corresponds to the same trip in Proposition 2 with the exception that Alice’s data is set to a constant logic ‘0’. Since the condition for Proposition 2 is met by our specific choice of \(p_i\)'s and \(\theta_i\)'s, therefore:

\[\text{Prob}(Z = 0 | X = 0) = \text{Prob}(Z = 1 | X = 0) = \frac{1}{2}.\]

This means that when Eve (intercepts and ) measures each \(|\psi_{1i}\rangle\) (possibly after a rotation of her choice), then she observes logic ‘0’ or ‘1’ with equal probability, regardless of Alice’s choice of angle \(\frac{2\pi k_i}{n}\). Therefore, she can’t get any information about the qubit’s angle in its trip from Alice to Bob.

b) Although the conclusion in item a) is good news, note that if there are only two angles for Alice to choose from (i.e., \(n = 2\)) then that conclusion will break down because Eve know Alice’s data is ‘0’, and since Alice can only prepare one of the two states \(R(0)|0\rangle\) or \(R(\pi)|0\rangle\), then Eve can find out the angle with certainty because the two states are orthogonal. Therefore we have to impose the condition \(n > 2\) for the sake of security.

c) To show that performing Protocol 1 is essential in the first leg of the trip, we assume that Alice sends the qubits to Bob without performing Protocol 1 (thus modifying Step 3 in Protocol 2). While Eve can get no information about the specific choice of qubit angles by Alice, Eve is still able to launch the following man-in-the-middle attack:

Eve intercepts and performs measurement on Alice’s qubits. This allows her to know the state of each qubit...
d) On the return trip for qubits (from Bob to Alice), Eve can intercept and make measurement on the qubits. These qubits carry data, however a direct invocation of Proposition 2 shows that no data can be gained by Eve if she intercepts (Apply Proposition 2). However, if Bob does not use Protocol 1 (in Step 4) in transmitting the qubits back to Alice, a malicious Eve can intercept, drop the qubits and insert her own. In this case, Alice will receive gibberish instead of meaningful data. This is a disruption of communication as opposed to compromised security.

e) In this and the next items, we show security against multi-qubit emission attack. Suppose a qubit source used by Alice is imperfect and for each intended qubit it creates multiple replicas in exactly the same state as the original. This can create a severe security problem in BB84: Eve can capture and preserve a replica qubit and wait until the angle information is announced on the public channel. She then can perform measurement in the correct basis and recover the data. This cannot happen in Protocol 2 because no such information concerning the data carrying qubits is ever sent. Only in Protocol 1, angle information about the check qubits are sent on the public channel. This cannot give away information about Bob’s data. We will deal with the check qubits when we analyze Protocol 1.

f) Another attack using multiple qubits is the following: In Step 3, Protocol 2, Alice sends qubits to Bob. Because of the multi-qubit imperfection, Eve can capture and preserve a qubit replica for each original qubit Alice sends. During the execution of protocol 1, the check qubits are identified, therefore Eve can throw them away. She keeps the non-check qubits which are intended for carrying data. In the return trip, Bob sends the data carrying qubits encoded with his data. Not knowing the qubit’s angles, Eve cannot extract any information from the replicas she received from Alice nor from the originals or replicas she receives from Bob. (Now assume Protocol 1 is not perform in the return trip at Step 4.) Eve can drop Bob’s qubits and insert her own. These are the replicas she kept now encoded with her fake data. This data can be received and understood by Alice. This attack affects the integrity of data rather than its confidentiality.

However, this attack cannot succeed because of using Protocol 1 at Step 4. At Step 4, Bob sends his qubits (|ψi⟩s) along with the check qubits (|ϕi⟩s) he inserts in the frame. Eve who receives all these qubits has no information about the position of these qubits. Therefore she cannot replace the non-check qubits with her own. She can at best make a random guess about the position of N non-check qubits and attempt to replace them. Eve must be at least 1 in (N+M) choose N lucky to succeed. This means that by a choice of sufficiently large N and M, her luck can be made completely insignificant. Remember that these two parameters can be set to exceed any given numbers. If necessary, an appropriate padding algorithm can extend the length N of Bob’s data to a required minimum. Therefore, we have justified the use of Protocol 1 in Step 4, and thus removed the possibility of using multiple-qubit attack.

Up to now, we have discussed the various ways Protocol 2 can be attacked, and have shown that none can succeed. As it was seen, the security of Protocol 1 was a key assumption. In the next section, we turn to analyzing this assumption.

4.2. Analysis of Protocol 1

We show that Protocol 1 allows Alice to send Bob authenticated qubits. Authenticity of these qubits is essential for guaranteeing the security of Protocol 2. It is easy to see that Protocol 1 works correctly if Eve is not present.

Suppose Alice sends to Bob a frame of N + M qubits using Protocol 1. The idea is that Eve cannot interact with the qubits with vanishing probability of being detected by Bob. According to Propositions 3 and 4, because of the special choice of pk’s and θk’s, if Eve performs a measurement (possibly after an arbitrary rotation) on any one of the check qubits, the probability that her action produces an error detectable by Bob is at least Pr = 1/4.

Now suppose Eve decides to inspect L qubits at random in the frame. The probability that out of L qubits, k are check qubits is as follows:

\[ \text{Prob(Eve picks } k \text{ check qubits) } = \left( \frac{N}{L} \right) \left( \frac{M}{L} \right) \left( \frac{M}{L} \right)^{L-k} \] .

The probability that Eve goes undetected given she inspects k check qubits is as follows:

\[ \text{Prob(Eve undetected } | \ k \text{) } = (1 - P_r)^k . \]


Therefore the probability that Eve’s interaction is detected when she inspects $L$ qubits in the frame at random is:

$$\text{Prob}(\text{Eve undetected when she inspects } L \text{ qubits}) = \sum_{k=0}^{L} (1 - P_e)^k \binom{N}{L-k} \frac{\binom{M}{k}}{\binom{M+N}{L}}.$$ 

It is easy to compute, either by using the above equation or directly, the following extreme cases:

I. Eve decides to inspect all qubits in a frame. The probability that her action is not detected is:

$$\text{Prob}(\text{Eve undetected}) = (1 - P_e)^M.$$ 

If she succeeds, she has been able to measure all $N$ qubits that were supposed to be protected. This event can be made arbitrarily improbable by increasing the number of check qubits $M$.

II. Eve decides to inspect only one qubit in a frame. The probability that her action is not detected:

$$\text{Prob}(\text{Eve undetected}) = 1 - \frac{MP_e}{N+M}. $$

If she succeeds, at best she has been able to measure only one of the $N$ qubits. The probability of this event can only be made as small as $(1 - P_e)$ by increasing $M$.

In both cases, increasing $M$ implies decreasing the probability that Eve is not detected.

In another attack on this protocol, Eve does not measure the qubits but attempts to replace them with her own. Suppose she wishes to send $L$ qubits of her own. She must choose $L < N$ qubits in the frame to be replaced. Lack of any knowledge about the position of check qubits makes her guess randomly. She will be lucky if she selects none of the check qubits. The probability of this event is $\binom{N}{L}/\binom{M+N}{L}$. This probability can be made a small as desired by choosing a sufficiently large number $M$ of check qubits. In general, by increasing parameter $M$, we can make the probability that Eve’s measurement or replacement of $L$ qubits goes undetected as small as desired.

5. Conclusion

We introduced and analyzed two novel quantum protocols that together allow a secure transfer of classical data bits. The first protocol enables Alice and Bob to exchange authenticated qubits. The second protocol, which makes use of the first one, enables Alice and Bob to exchange data bits securely. The combined protocol has the following merits:

a) It can be used to send data over the quantum channel securely. This is especially useful in key distribution applications where keys are generated in advance rather than on the fly. BB84 and its variants cannot transfer predetermined keys.

b) In BB84, some information leaks out, therefore a process called privacy amplification is required by that protocol. In our protocol, no information about the data leaks out.

c) Our protocol, unlike BB84, is not vulnerable to multi-qubit emission attack.

One disadvantage of our protocol is its round trip requirement. This is a price to pay to protect against multi-qubit emission attack. While we have discussed most probable attack scenarios, there is more to be done to prove the unconditional security of this protocol.

References


